# The Works of John Dee MODERNIZATIONS OF HIS MAIN Mathematical Masterpieces 

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## THE WORKS OF JOHN DEE



[^0]
## Dedication

To John Dee,
who had the courage to share his wisdom even during timultuous times.

## Table of Contents

page
11558 (and 1568) Propaedeumata Aphoristica (in Latin)
19 Propaedeumata Aphoristica (translated into English)
511564 Monas Hieroglyphica (in Latin)
67 Monas Hieroglyphica (translated into English)
1231570 Preface to Euclid (in Elizabethan English)
145 Preface to Euclid (in Modern English)
1991573 A Certain Essence of Parallax
2051577 General and Rare Memorials pertaining to the Art of Navigation
2091580 Map of North America
2111583 Calendar Treatise
215 Calendar Treatise (in Modern English)
2251592 Compendious Rehearsal
2391594 Discourse Apologetical
245
Discourse Apologetical (in Modern English)

## Introduction

These translations and modernizations of Dee's major works are organized chronologically. However, I recommend reading the 1570 Preface to Euclid first. It was written for the common Elibethan gives a good feel for Dee's voice.

Then look over his works on Time and Navigation from the 1570 's and 1580 's. From 1575-1583 Dee taught navigational techniques to England's top explorers. He was also busy trying to convince the Queen to settle colonies in North America and to Reform the Calendar. (She took his advice, but both efforts ultimately failed for other reasons)

From 1583 to 1590 , he was on the continent with his family, from Poland to King Rudolph's Court in Prague.

In the 1590 's, he wrote two lengthy appeals to the Crown to be granted a rectorship and for a life devoted to the service of England. In these autobiographical texts (the Compendious Rehearsal and Discourse Apologetical), Dee lists the books and treatises he has written, providing valuable insight into his career.

Finally, return to the beginning of the book. The Propaedeumata Aphoristica (or Preparatory Aphorisms) are meant to lay a groundwork for the Monas Hieroglyphica. Read the first 20 Aphorisms and browse the other 100. Don't be concerned if you don't follow all the astronomical geometry. Much of is not directly applicable to the Monas (but he has tucked important clues every here and there).

Then to be really confounded, read the Monas Hieroglyphica. You may not understand what it means, but you will certainly sense how important it was to Dee.

## Latin original


[Title page of the 1558 Propaedeumata Aphoristica]

[Title page of the second edition 1568 Propaedeumata Aphoristica]

CLARISSIMO VIRO D. GERARDO MERCATORI, RVPELMVNdano, philosopho et mathema. tico illuftri: ac amico fuo longe charifsimo loannes dee londinensis. S.D.P.



NDECIMVS iam agitur annus (humanifsime, docifismeć;,mi GERAR DE‘ab illo, quo noffris egarelictis Academijs,cmnibusq́q; noffrarū fcholarum, in artium feptem(libcraliū dictarui profefsione, percurfis ordinibus: finc fubere (vt in prouerbio cft nare: \& in Regiones tranfmarinas coperam peregrinari :ad iplos inuefligandos fontes, à quibus hac noftra xtate, plurimi ad nos optimarum quarumq; Artium deducebatur canaliculi : \& cum illis vitam ducere familiarem, quorum vel leuifsimus quifq; vnius diei in feriberdo, labor, nobis antea domi defidentibus, per anni fere vnius fpatium, fatis(ad intelligendum)faceret negotii. Atq; in ifto primx mex peregrinationis inchoato curfu, quoniam in te, primum omnium, Louanii tum agentem, incidere, maximo mihi fummi Numinis obtigit fauore: \& ex tuis mecún difceptationibus, tum primas tú altifsimas ve radices ageret tota mea peregrina philofophädi ratio:Núc proinde Ego effe xquũ cenfeo, rationiq́; maximè confentancū, vt iam primò peregrinantes, laborū ctiam tu meorum primitias, iure tibi vendices meritifsimo. Et maximè, cum mutux noftrx amicitix, familiaritatisq́; cöfuetudo ea erat, toto vt triennio, vix totos tre's fimul dies, alter alterius lubens careret afpectu: \& ea veriufque noftrûm difcendi, philofophandíq; auiditas, vt poffquä conueniremus, tribus vix hore minutis, ab arduarum \& vtilifsimarum rerum indagatione abftincremus, An non huius noffrę tam fincerx amicitix, \& tam fuauiter continuatę philofophandi rationis, gratia, aliquod faltem $\sigma v i \tau \alpha \gamma \mu \alpha$, vel monumentum, fcmpiternx hominum memorix commendare debuimus: vt inde
$\forall \mathrm{i}$ uauils.

EPISTOLA
Suauifsimum illudamicitix vinculum, quo noftri in perpetuum copulantur animi, fuis quoque nectere difputationibus, poftera ftudooorum exc.tetur ętas? Et non alter alterius vel côternnere ftudia, vel eruditioni inutdere:capita fed fimul conferre, ad veri iaquifitionem, \&e vilifsimas amplficandü difciplinas. Atq; ve hanc potifsimum materiam, hoc tempore mihi traCtandam, eligerem : penultimx tuę ad me hiterx, in quibus, de nobili illa, inter nos olim agitata, controuerfia, memoriam mihi velle refricare, videbaris, occafionem dedere. Nec in iftius enodatione, feu pocius demonftratione, longiorem me nunc effe, vel valetudo, qux iam perintegrum annum periculofifsime labefaitata fuit (etiamfi voluifem maximè) tolerauit : vel ipfa, de Caleftium corporum virtute, Difciplina, defiderare videtur. Ex his enim quax in medium attulimus, tum ad infinitos particulares, in Arte cafus, Apodicticè procedédi haberi facultas poteft: rum ipfa pręterea difciplinx prẹcipua, in his funt ia $A 2$, confirmataq; fundamenta: vnde de aliis eius Artis quid fit flaruédum prexecptis, induftrio facile conftabit artifici. Non tamen infini-
 creta: qux, nec ipfitalum Ceriptores, rationum ftablire momentis pofsint, nec vllus vnquam alius, à Naturx viribus talia proficifci, obferuando intelligere. Tu ergo qui N A TVR AE obfruantifsimus effe Cultor foles: NATVRAE, in iftis Aphorifmis, ferutare virtutes veras, virtutes magnas, virtutes paucis vix credibiles Sapientibus, at paucifsimis notas. Et
 contendat, qua illi non fint fcripta, tu cum R E C E PE R IS, edicas publicè. Atq; hxe hatenus. Cáautem in litetis ruis ad me, fuè omnibus, quid ıpfe prę manibus habcam, à me fcirc, foIes contendere:S in illis certé, quas ante nominaui, penultimis mecum egifti maxime, ut magnum illad opus meum A podiatcum, de Arte noua (vt tu vocas) quàm primum vel in lucem darem, vel eius te vt participem facerem : me Scias, preter periculofifsimum, quo toto iam proxime clapfo anno laboraui, morbum, ala actinn multa (abillis, qui. \&c.) effe perpeffum incommoda, qux mea fudu plutimum retardauere: Viresque etiam meas, nondum polfe tantü fultinere ftudiilaborif́; onas, gnantumillud, Herculeum penè(vt perficiatur) requiret opus. Vnde
fis mea

## NVNCVPATORIA.

fi mea haud queat opera, vel abfolui, vel emitti, dum ipfe fim fupertes:Viro illud Legaui cruditifsimo, grauifsimoq́;,qui Artium Mathematicarum vnicum nobis eft relittum \& decus \& Columen: nimirum D. D. Petro Nonio Salacienfi: illumq; obntxe nuper ordui, vt, fi quando pofthumum, adillum deferetur hoc neum opas, benignè humanitérq; libi adopret, modifque ommbus, tanquam luo, vtatur: abloluere denique, limare,ac ad publicam Philofophantuum veltatem parpolire, tua dignetur, ac fi fuum effer maxime. Et non dubito, quin ipfe ( $\mathbf{i}$ per vitam valetudném $q$, illi eritintegrum) voti me faciet compotem : cum \& me tamamer fideliter: \& in artes, Chriftian $x$ Reip. fummè neceffarias, gnauiter incumbere, fit illi à natura infitum : voluntate, induftria, vfíq; conficmatum. Tuis igitur votis, de laborum meorum cuulgandis monumentis, nondum me pofe fatisfacere, licer iam clare fatis docui, Si tux tamen petituoni de fcriptorum meorum habenda Catalogo, non refponderem,meritòme maximx damnares ingratiudinis: En tibi ergo corum Titulos, quę per medias meas,maximáf ; difficultates, ita à me mihi cópofita, (criptaq; extant, vt eadem (cura viribus valeam corporis, dulcíq; fruar ocio) in publicum producere(non mihi tantum effe cognita,) exoptem maximè.

opus mathematice demonftratum. lib.16.
2 De Planetarum, Inerrantium fellarum, Nubiumq; à centro terrę diffantiis : \& ftellarum omnium veris inueniendis magnitudinibus.

- DeSpeculis comburentibus 4 De Pecrais comburenteres.
4 De Perfpectiua illa qua peritifsimi illuftriffimíq; vtuntur pictores. lib.2.demöft.
5 De terria \& prẹcipua Perfpectiue parte,que de radiorum fractione cractat.
De Caleftis Globi amplifsimis comoditatibus. $\mathrm{l}: \mathrm{b}$
7 Speculum vnitatis:fiue Apologia pro Fratre Rogerio Bachone Anglo: in qua docetur, nihil illum per Dxmoniorum auxilia feciffe, fed Phulofophum fuifie maximum: na-


## Clarissimoviro D. Gerardo

Typographus Lectori.
Habes hic Candide Lector, hanc fecundam ifforum $\Omega$. phoriimorum adifionem, longè emendatifimam, ex ipfius Authorix autographo, accuratifime imprefam. Ille enim que Anno. 1 ; 58 emi§a erat,magnaTypographi inewria permultis clasdicabas locis, nelutitu ipe. ex dilizenei noftrorum laborum collatione,
facillime isdicare poßis. Ets igitar ufaris, fruari $\int_{g_{0}^{\prime}}$ : Vale.
snno àpartuvirgineo 1567
Menfe Decembri, Londins;

EPISTOZA
regrina pbilofopbandi ratio: Nunc proinde ego effe aquum cenfeo, rationiqg maximé con Entaneum, ut tiam primó peregrinantes, , borum etiam tu meorum pris mitits, iuretibi uendices merit!\}imo. Et maximé, cim mutuce noftracamicitie, famtiaritatt क्षि confuetudo ea erat, toto ut triennio, uix totos tres finul dies, alter alterius lubens careret afpectu: Grea vtriusiue no, frû̀m difcendi,philofopbandiq̆; auiditas, ut poftquam conueniremus, tribus uix bor a minut is, abarduarum $\mathcal{F}$ uthll ßimarü rerum indagatione abftineremus. Ant non huius noftra tam fincera amicitio, $\mathcal{O}$ tam funui ter continuatapbilofopbandi rationis, gratia, aliquod faltem ovvacu ye, uel monumentum, fempiterna bos minum memoria commendare debuimus: ut inde fuas ui Simum illud amicitia uinculiim, quo noftri in perpes tuum copulantur animi,' fuis quoque nectere difputas tionibus, pojtera fudio forum excitetur atas? Et now alter alterius uel contemnere ftudia, uel eruditioniths widere:capita fed fimul conferre, ad ueri inquilitionem Or utilyßimas amplificandum difciplinas. eAt tque ut. banc potißimuim materiam, boc tempore mbi tra ctandam,eligerem:penultima tua ad me litera, in quis bus, de nobili illa, inter nos olim agitata, controuerfia, snemoriam mibi uelle refricare, uidebaris, occafionem dedêre. Nec in iftius enodatione, feu potuus demone fratione, longiorem me nunc effe, ucl lualetudo, qua

MERCATORI, RVPELMVNDANO,
Philofopho \& Mathematico
illuftri, ac amico fuo Ion= gè charifsimo,
IOANNES DEE, LONDINENSIS, S. D. P.

$N$ decimus iam agitur annus(bumanifo fime, doctijsime ${ }^{2}$, mi Gerarde) abillo, quo noftris ego relictis Academijs, om? nibus $\%$; noftrarum fobolarvm, in artium feptem(liberaluim dictarü)profeftione, percurfis ora dinibus: fine fubere (vt in prouerbio eft) nare, ơ in Regiones tranfmarinas capperam peregrinari, ad ips. fos inueftigandos fontes, a quibus bac noftra cetate, plurimi ad nos optimarum quarumos Artium deducebans tur canaltculi: ©ুcum illis vitam ducere familiarem? quorum uelleutStmus quifque vnius diei in fcribendo, labor, nobis antea domi defidentibus,per annifere us nius Patium, fatis (ad intelligendum) faceret negotij. Atque in ijtoprima mea peregrinationts inchoato curfu,quontiam in te, primtim omnium, Louanij tum as gentem, incidere,maximo mibi fummi $N$ uminis obs tigit fauore: - ex tuis mecum difceptationibus, tum primas tum alty Simas ut radices ageret tota mea ped

$$
\text { A.ij. } \quad \text { regrins }
$$

NVNCVPATORTA.
que tatn per integrum annum periculofif Sime labefaid data fuit (etiamt fi uoluiffem maximè) tolerauit: uel it) 1 , de Caleftium corporum uirtute, Difciplina, de. fierare videtur. Ex bis cnim quae in medtum attulis mus, thim adinfinitos particulares, in Arte cafus, $A 0$ podictice procedendi baberi facultas poteft:tum ipfa praterea difciplina pracipua, in bis funt iacta, confirmataq; fundamenta:unde de alijs eius Artis quid fitfatuendum praceptis,induftrio facileconftabit ar
 tao probo nug:ts, uel futilia decreta: qua nec ipfitas lium fcriptores, rationum ftabilire momentis poßint, nec ullus unquam alius, a Naturacuiribus talia profis cif ci,ob ertiandointelligere. Tuergo qui N $\mathcal{A}$ T $V$ R $A E$ obferuatifsimus effe Cultor foles: $x \mathcal{A} \times V R \wedge A F$, in iffis Aphorymis, fcrutare uirtutesueras, uirtutes mas ghas, uirtutes paucis uix credibiles Sapientibus, at pauc!ßimis notas. Et ne $\tau \tilde{\omega} \nu \grave{\alpha} \mu v x \tau \omega \mu \pi i \sigma ;$, fuo fibi mas lo,ea binc expifcari,eliceréue contendat, qua illinon funt fcripta,tucum Receperis, edicas publice. At $\$$ biac bactenus. Cum autem inliteris tuis ad me, fer $\dot{e}$ omnibus, quidip厄e pra manibus babeam, a me ficire, foles contcndere: - in illis certe, quas ante nominau, penultimis mecum egifti maximeं, ut magnum illudo, pus meum © Apodicficum, de Artenoua (ut tu uod cas) quadm primim uel in lucem darem, uel einste
$\mu \mathrm{n}$.

## EPISTORA

ut participem facerem: me Scias, prater periculofifisis mum, quo toto iam proxime elapfo anno laboraui,mor bum, alta etiam multa(ab illis,qui.-テc. $c_{*}$ ) e fle perpeffü incommoda, que meaftudiaplurimiom retardauere: uiréfque etiam meas, nondum poffè tantum fuftwere ftudijlaboris\%́, onus, quantum illud, Herculeum pené (ut perficiatur) requiret opus. I nde fi mea band que, at opera uel abfolui, uel emitti, dü ipfe fimfuperftes, Viro illudlegaui erudttifimo, grauifimoq́, qui Ara tium Matbematicarum unicum nobis eft relictum wo decus ©rcolumen : nimirum D. D. Petro Nonio Salacienfi: Illímque obntxe nuper oraui, ut, $\sqrt{\text { i }}$ quand do poftbumum, ad illum deferetur boc meum opus, benignè bumanitérque fibi adoptet, modifque ommbus; tanquam fuo, utatur: ab foluere denique, limare, acad publicam Pbiloofophantum utilitatem perpolive, ita dignetur, ac fil fum efet maxime. Et non dubito, đuin ip $\ell\left(\int\right.$ éper uitam ualetudinémque illi erit integrü) uos ti me faciet compotem: cuim $\mathcal{\sim}$ me tam amet fideliter, Noinartes, Cbriftiance Reip. fummenecefarias, gnauiter incumbere, fit illi a natura infitum:uolunta" te, induftria,ufüve confir matum.'Tu is igitur wotis, de laborum meorum eumlgandis monumentis, nondum me pofe fatiffacere, lucet iam claréfatis docui, Situe tamen petitioni de friptoruin meorl:m babendo Cas talogo, non rofponderem,merito me maximadamna' resingrstitudinis. Entibiergo cornm Titulos, qua per

## EPISTOLA

- umń', bominumt referat iudicia, uotaq́, bac à meranta tractari, liciquepromitti argumenta. Vtexiftius Exploratoris relatione, mecum $\mathcal{O}$ doctis cumt amis cis, rationem ineam, num iftas meas (qualefcunque) copias, in peregrinos actuitum producere campos, ul domi, id/buc diligentius,in militarieducare difaplina, debeam. Iam reftat ut te maximeंorem, egregiatua
 te, qua. Pby/ica uocatur, quadm in geometricís, Orgeo $^{\text {gen }}$ grapbicís rebus, publicis (quaim primim queas) ut committas bominüftudijs: fic enim Rempub. literá riam (de qua annos ante multos, multis magnifop tuis labortbus, es optime meritus) iftis utilif simis tus, no. uifque Inuentis, eximieprofecto amplificabis. Vales. as: Coptifque tuis pulcherrimis, Deus Opt, $M_{a x}$. exitus largiatur forlicißimos. IterumV ale.

Londini, anno noftro nato Redemptore is s 8, Iulij. 20.

NVNCVPATORIA.
per medias meas, maximáfque difficultates, ftad me mibicompofitar, criptáque extant, ut eadem (cum uis ribus ualeam corporis, dulcíque fruar ocio) in publis cumproducere (non mibi tantuime efe cognita) exops tem maximè.
 cè demonítratum.lib, 16.
2. De Planetarum, Inerrantium ftellarum, Nubium'q; à centro terra diftantiis: \& ftellarum omnium veris inueniendis magnitudinibus.lib.2.demonf.
3 De Speculis comburentibus.lib.5.demonft.
4 De perfpectiua illa qua peritiffimi illuftriffimíg vtuntur pictores. lib.z. demonft.
5 De tertia \& precipua Perfpectiue parte, quae de ras diorum fractione tractat.lib.3. demont.
6 De Coeleftis Globi ampliffimis commoditatibus. lib. 2.
7 Speculum vnitatis : fiue Apologia pro Fratre Rogerio Bachone Anglo, in qua docetur, nihil illum per Damoniorum auxilia feciffe, fed Philofophum fuiffe maximum : naturalitérq; , \& modis homini Chriftiano licitis, maximas feciffe res: quas, indoctü folet vulg' in Dxmoniorum referre facinora. lib. ${ }^{-}$
8 De noua Nauigationum ratione. lib.2.
9 De Anuli Aftronomici multiplici vfu, capita centü. liber vnus.
to De Itinere fubterraneo. liber vnus.
"De Trigono Circinóg Analogico. lib:3.
Aliorum adbuc tacebo nomina: quitamen antcifon rum quo)dam (annuente Deo) publica fruiluce pof fint. Hoc autem opufculum, (numero duodecimum) leui munitum armatura, tanquam Exploratorem, in. uarias emitto regiones: ut uer a mihi doglorum probos . A.iiij. rumy

## Lectori

Pbilofopbiafinceriorisftudio fo,
IOANNES DEELONDINENSIS
S.D. P.


PHORISMOSENTIBINOSTROS, fecunda iam emittimus confultatione: Numero eo $=$ rundem, Ordine, vel Materia, haud mutatis quic: quam. Aphorifmos, eo dem cgo quidem, Prouetti* oribus effe cio : At in multarum magnarumq́q; Sci* evtiarum cognitione non adeó progreßis, longiufculos profecto, diffi2 cile $\tilde{q}$; libros. Ex Communi, tritáue philofophandi via, qui hûc (Mi= fer)diuerterit, Labyrintheum e efe diuerforium, actûtum exclamabit. QHodcunq; eniwe egregium, in Antiquorum vel Vcrorum quorums cunq; philofophorum experientia Theoriáue fuiffe aliquandopofia tum,vel legendo, vel meditando, vel periclitando, vel peregrinaris do, ipfemet intelligere, excogitare, inuenire, audire, videreq́; olim potui, Id omne, vel Sisesctissima Quaeqvepor tius, IN CORPVS VNVM SOLIDVM $\dot{\text { águovbins }}$ CONGLOBATA, tuishic commififtudijs. Et preter omnium Maiorum nofirorum Inuenta preclarißima, quam Mirificis, Hono= rificisq; ornamentis boc fit confertum $\Sigma \omega \tau \pi \alpha y<c e$, frequenti fitu perquiras leatione (accuratius queq; penfitando) certifimè confpici=
cs. Sed tamen que ego veritatis illuftrande, amplificandeq;
ftimulatus defiderio(quò foli tibi effent plenißimè perpes
(ti) neruos mei contenderim ingenioli, tu noli indig.
nis profunifó; manifffta reddere:nc ev tibi er mi=
bitum dedecori, tum dameo vertatur maxi=
mo. Vale amice: Manibusq́; benc pre= cator meis.
Ex Mufeo noftro Mortlacenfi, Amo 1.567. Decemb. 24.

# Ioannis Dee Londinenfis,de 

praftantioribus quibufdam NATVRAE


## Aphorifmus 1.


t devs, ex nihilo, contra rationis\& naturæ leges, cücta creauit:ita in Nihilum abire,rerum cre atarumaliqua nunquam potêt, nif contra rationis Naturæópleges, per Supranatu ralem Dei potentiam fiat.
2.

MIrabiles ergo rerum naturalium Metamor. phofes fieri à nobis, in reiveritate poffent, fi artificiofe Naturam ex pyronomix Inftitutis vrgeremus.Naturam autem ego dico, Rem Cre atam quamcunç.

$$
3 .
$$

$\mathrm{N}^{\text {Onfolum eaEffeafferendum eft, qua } \mathrm{A}}$ Ctu in rerum natura funt confpicua, noti¢\%:Sed \& illa quoç qua quafi Seminaliter, in n2: turx latebris Extare Sapientes docere poffunt.
4.

Q Vicquid Actu exiftit, Radios orbicula riter eiaculatur in fingulas múdi partes, qui vniuerfum mundum fuo modo replent. Vn , de omnislocusmundi radios continet omnium

## PROPAEDEVNATA

## X.

QVxcunç resfunt fibi mutuo coordinatç,cô, ueniẽtes,vel conformate, vna aliam tưfpon, te imitatur fua,tum etiam aliquădo vna ad aliam localiter accurrit:vnáq aliam(quantum poteft) tuetur \& munit,etiamfí interea vis fibi inferrivi deretur.Per harum ergo rerum naturalium(mo dis variis) in mundo Separatim exittentium, $V$, nionem : \& aliarum Seminaliter tãtum prius in Natura pofitarum, Actuationem, mirandamagis, verè, naturalitercŕa, (nec violata in Deumfi. de, neqg Chriftiana lefa religione) pręfari pof funt,quàm quis mortalis,credere queat.
xt.

MVndusiftetotus eft quafi lyra, abexcellen tiffimo quodam artifice concinnata : cuius chordx,funt huius vniuerfitatis, Species fingulx, quas qui dextrè tangere pulfaréq́ nouerit , mirabiles ille eliciet harmonias.Homo autem,perfe, Mundanx ifti Lyrx,omnino eft Analogus. xII.
$S$ Icutlyra, conftitutio quaxdam eft tonorum confonãtium atç diffonantium, aptiffimata menad fuauiffimam \& infinita varietate mira bilem exprimendam harmoniam:Sic Mundus ifte partes intra fe complectitur, interquasarctiffima confpiciatur Sympathia:alias autemin ter quas diffidium acre, atç Antipathia notabilis:itatamen, vt tum illarum confpiratio mutua,

## APHORISTICA.

rerumineo Actu exiftentium.

$5+$<br>$T$ Am Subftantia quàm Accidens, fuamà âe Speciemexerunt : Sed Subftantia omnis, excellentius multòquàm accidens.Et Subftantiarum quidem, illa qux incorporea\& fpiritalis eft, (vel qux Spiritalisfacta eft) in hoc munere longèfuperat illamqux eft corporea, acex fluxis coagmentata elemẽtis. Licet quantò resfint nobiliores, tantò incompletiorem fuam Speciemfaciant:Species enim completa,idem obtine bitnomen cum principali agente.

VI.

S Icut vna res differt ab alia, ita \& earundem radij differunt in efficiendi virtute, $\alpha$. effectus conditione, dum circa eandem omnino remoperantur.

V 11.
$R$ Adiorum quorumcunća ab vna re in díuerfasemanantium, diuerfifunt effectus. 8.

Viequid inaliud agit,fimile quodam modo eft,at alio quidem modo diffimile prorfus illi eft in quod agit, aut nulla eft actio.

## 9.

Q Vicquid in mundo eft, ad aliud quid ordinem, conuenientiam, \& conformitatem

## APHORISTICA.

rum iftarum lis atç diffenfio, ad Totius confen fonem atq̧̧ Vnionem admirã̃dam egregie faciat. xiIf.
$S^{\text {Enfus noftri, nonfunt fenfibilium radiorum à }}$
rebuseffluentium caufe,fed teftes.
XIIII.
Seccies non folum fipiritales, fed etiam alix na$S_{\text {turales à rebuseffluunt , tum per Lumen, tum }}$ finclumine:non ad vifum folü, fed ad alios inter, dumfenfus, $\&$ preccipué in Spiritu noftro imaginali,tanquam Speculo quodam coalefcunt, fe. léç nobis oftendunt, $\&$ in nobismirabilia agũt.

N Vllus Motus perfectior orbiculari, Nec vlla forma humanis expofita fenfibus, $L$ V CE eft vel prior vel praftantior. Corporum igitur preftantiffimorum \& perfectiffimorum, hac duo maximè propria erunt.
16.
$\mathrm{Q}^{\text {Vicquidin mundoeft, continuè mouetur a- }}$ liqua motus Specie.

$$
17+
$$

P Roratione motuu primorum, quifunt cceeleftium corporum maximè proprï, cateri inferiorum motus omnes naturales \& excitãtur \& ordinantur. Mouentur autem ipfa Cocleftia aliquando furfum, aliquanco deorfum:in ante riorem aliquando partem, aliquando in pofteB.iii. riorem

## PROPAEDEVMATA

riorem, aliquando verfus vnum Mundi, velE. clipticx polum,aliquando verfus alterum. 18.

I N fingulis quatuor, Maioris Mundi magnis
Matricibus, funt tres diuerfẹ partes:fimul tame concrete, conformatex'ǵ, \& iuftisfuis contempe. ratæ ponderibus:quasiam Notariacè $\dot{A}$ ös, fiue $\dot{\circ} \dot{s} \dot{A}$, fiue $\dot{s} \dot{O} \dot{A}$ appellare libet (Sic me enim Pyrologi intelligunt) Harum Trium proprie tates effectus'̛̣̂ naturales tum principales tumfe. cũdariostum etiam tertios, quàm potes exactif fimè difcas: Modum'́s reducendi tertiosadfe, cundos, \& fecundos ad primos : Itidem tibieft fummopere examinandum, quibus cafibus, ear dempars, diuerforum, immo contrariorumnõ nunquameffecturum effe caufa poffit. S I duo,tria, vel quatuor Elemêta, \& in quaciiv q quantitate commifceantur, vt de compoii. ti illius vera natura, Complexione fiue Tempe ramento fias certior, per artem quandam, $\mathrm{Gr}^{2}$ duationum dictam, tibi eft elaborandum.

$$
20
$$

E Xquaelementorum proportione, firgule
humani Corporis partes, humores, 8 (fpi, ritus conftent (quàm propè fieri poteft) Aftrologoeft peruidendum. In alĭs etiam rebus natu talibus idem experiri, atç intelligere eft fumme neceffarium

APHORISTYCA. neceffarium, $\&$ valde iucundum.

## 21.

$S$ Emenquodqsin ine potentia habet generatio, nis cuiufq, integrum \& conftātem ordinem: eo quidem modo explicandum, quo \& concipientis loci natura, \& Circumfufic colifuperuenientes vires, cooperando confpirant.
 Formæ fenfibilis, ( cultas, vt fine ea cætcræ formæ omnes agere nihil poffint.

## XXIIY.


 quis philofophorum non decantat" quis mortalium nô in feipfo id ferè quotidie experitur! Vt
 fiverdat. Vnde Medicus percorpusfanat animam atç temperat. Muficusautem per animam,corporimedetur \& imperat. Qui ergo quàmplurio mis modis tü medicitư mufici poterit fupplere munus, is hominum \& corpora \& animos pro fua feré gubernaret voluntate. Verum hoc eft à modeftius philofophantibus,myfterijcuiufdam inftar tractandum.
B.iiij. XXIMI,

## APHORISTICA。

## XXVII.

$T^{\text {Am folida quâm diaphana cuncta, quẹ intra }}$ mundi ambitum exiftunt, penetrandi vis, cocleftium radiorum maximè propria,magnam illis influendi, fue fuas imprimendi vires facilitatem ineffe demonftrat. Vt autem cum elegantiaquadam, deinde cum tenacitate, vel ad infinitum fere tempus retineatur immiffa virus, idex materix in quam influitur difpofitione naturali vel pręparatione artificiofa, tam in vifibili forma quàm in elementaribus qualitatibus \& alijs, prouenire debet.

$$
28 .
$$

P Rimümobile eft inftar fpeculi fpharici côcaui, cuius qualemcí̛q foliditatem nullus ftellarũ radius fenfibilis penetrare poteft : cum eti am nullus effet talis penetrationis vfus apudfupe ros;fint \& alix perplures demonftrationes.
$\mathbf{X X I X}$.
$\mathrm{Q}^{\text {Vafcunḉs vires per fenfibiles radios, ftelle ef- }}$ ficiendo exercent, non folum directis, fed etiam fractis $\&$ reflexis illis radijs, tales fuas vires ad effectus oportunos promouere poffunt. xxx .
$M$ Agnitudines verę non folùm terreftrisglobi, fed \& planctarum fixarumó́ omnium ftellarum,aftrologo debent effe notx.
C. $i_{0} \quad \mathbf{x} \times \mathbf{x}$.

## PROPAEDEVMATA

 XXXI.DIftantix verretam fixarum, quàm fingulorü planetarum à centro terrex, quocuní pro. pofito tempore, aftrologo conftare debent:ficut \& nubium, fiue craffioris aëris, varix à terraalit tudines.

$$
\mathrm{xx} \times \mathrm{x}
$$

QVibusterrę locis, quecunç ffella fiue fixafi. ue erratica quocunç dato tempore perpen, diculariter immineat:\& quantum incidentię di recte angulum, cum omnibus alijslocis, fupra quorum horizontes,eadem ftella, eodem tem. poris momento eleuatur,efficiat, cum primis eft cognitu neceffarium.

$$
\mathrm{xxxili}
$$

S
Enfibilem omnem radium, â feelle alicuius corpore ad punctum aliud quodcunq̧ externum emanantem, ac cum ciufdem fella conue xa fuperticie æquales vndiq; efficientem angulos,circüftat conus rectus, radiofus, fenfibilis'q: cuius Axis, ipfe dictusradius erit: Vertex verò, punctum illud externum: Bafis denique, conue xæ fuperficiei ipfus fellix ea portio luminola qux dicto verticieft proxima, terminatur'̣́ per circuli circumferentiam, ab illo termino linex rectx (à dicto vertice ad ftellam ducta) qui ip famftellam contingit tantü, defcriptam.

## PROPAEDEVMATA

portione radios illos directos ad terră demitṻt, XXXVII.
$\mathrm{O}^{\text {Mnes ftellę terram minores, quanto terree pros }}$ pinquiores fuerint, tãto fortiores, eidem fui Luminis radios infundunt: licet minorem eiufe dem portionem fenfibilibus illis fuis directifque radips afficiant, quàm quădo funt remot $x$ magis.
XXXVIII.

OMnes ftellaterra maiores, quäto terrx vicis niores fuerint, tanto fortiores illi fuos imprimũt radios: \& terræ etiam maiorem portionem fenfibilibus iftis fuis, directifque radij̣s illuminăt, quàm quandolongiori funt femotx interuallo.

## XXXIX.

P Erpendendę tibi funt cum fumma diligentia
Terre\& ftellarum quarumcunç tum terra maiorum, tumterra minorum, portiones ille Superficiales, Sphæricę conuexitatis, inftellis quidem luminofę, at in terra ab ipfis luminofis illuminate,qux pro varijisftellarum àterra inters uallis, diuerfarum fiunt quantitatum. Ettamin terra quim in ftellis terminantur per terminos fuperficiei conice curte, à linea recta, tum ipfam terram, tum ipfarum ftellarum corpora contin' gente, defcripte. Attq de his portionibus egimus progofitionibus. $35+36 \cdot 37.8$. 38 .

APHORISTICK。
XXXIII.

R Adiorum àbafi luminofa alicuius ftellx, ad aliquod externum punctum effluentium, A xiseft fortiffimus:\& reliquorum,quò ipfi axi fú erint propinquiores, eò erunt remotioribus, fortiores,refpectu dicti pũcti. De radî́s ex profun. ditateftellicorum corporum egredientibus, alius nobis erit dicendilocus.

## xXx.

A Stellisterra minoribus, fenfibiles cunctiqui exeunt radij directi ad terrenę conuexitatis, quantam maximam poffunt portionem,abipfarum conuexarum fuperficierum (quę tales ftellas ambiunt) portionibus veniunt, qua funt dimidị̂s maiores. Et quò terræ propiores fuerint,ed à maioribus illis portionibus, radios fuos directos terrex communicant: Nunquam tamenterrenę conuexitatis dimidium fuis illis fenfibilibus radijs attingere queunt, fed portionem, eiufdem dimidiominorem.

$$
\mathrm{XXX} \times \mathrm{Y}
$$

OMnes ftelle terra maiores, plus quàm dimidium terrenæ conuexitatis, omni tempore fuis fenfibilibus $\&$ directis radijs illuftrant:Semper etiamà fux conuexæ fuperficiei portione dimidio minore, illos terrx impertiunt radios. Et quò terrępropinquiores fuerint, eò à minore tali C.ii nortione

## APHORISTICR.

又2.
$A^{D}$ quodcunç punctum totius mundi venit alicuius ftellx conus rectus, radiofus, fenfis bilis $\ddagger$, eiufdem coni bafis,minor quidemfemper erit, , पuàm dimidium conuexx fuperficiei ipfius ftellx, cuius ille fuerit conus. Videant ergo aftronomi, qua ratione ftellarū metiantur diametros. $\mathrm{xL}_{\mathrm{I}}$.
$Q$ Vanto eadem ftella ab aliquo puncto totius mundiremotior fuerit, tantofui radiofi coni recti fenfibilif̧̧̧ bafis,maior cuadit, $\&$ quã̃ to Propinquior, tanto minor.

XLIT.
E Xaminãdatibi crit quãtitas huius bafis conio $E_{\text {ce, in omni pofitu cuiuff ffelle,refpectu vnius }}^{\text {ren }}$ alicuius puncti, vbicunçillud punetuffatuatur.

## XLiti.

E Iufdem ftellę Coni recti luminofilongiores, $\mathrm{E}_{\text {funt ipfis breuioribus, }}$ quibufdam de caufis fortiores:at alias ob caufas,lolgè debiliores: fortiores quidem eò videri poffunt,tùm quod eorü̆ bafes luminofx, maioresfunt, tum quia anguli adverticem,minores fiant. Ex hisduabus caufis fimul iunctis, hare nafcitur ratio: Quòd in longioribus conis, copiofioresradí, non incidentes folum fed etiam reflexi,magis vniútur: vnde mas

PROPAEDEVMATA
ior vis circatalem verticem exercetur . Sed natur raliter \& fimpliciter, propinquitas agentisadid in quod agit,breuiores conos,fortiores efficit.

## XLIIIf.

QVantitatem illius conuexæfuperficiei Luna ris, qux quocunqz dato tempore, nobis illu minata conuertitur, accuratè elicias.

$$
\mathrm{x} \mathbf{L} \mathrm{~V}
$$

$\mathrm{H}^{\text {Orizontem noftrum verum , illum appella: }}$ mus circulum, qui circumductu eius linex defcribitur, cuius quiefcens terminusin Mundi centro fuerit, alter verò in fummo ftatuatur cxe lo:ita vt à noftro vertice in huius circuli centrü demiffa rectalinea, eidem circulo perpendicu, larisexiftat. At Senfibilem noftrum Horizon, tem, alibi demonftrauimus effe illam terreftris fpherre conuexam portionem, quxe (omnibus fuper terre vniformem conuexitatem, remotis impedimentis ) nobis eft confpicua tota:terminatur'̣́ per circuli circumferentiam, abillotermino linex rectx (ab oculo noftro adterrę contactum ductx) qui ipfam terram contingit , de fcriptam.Hanc'̣̆ portionem aliquãdo maiorem, aliquando minorem à nobis poffe conficici, pro varia noftrę altitudinis ratione fupra vniformem terreniglobi conuexitatem, ibidem docuimus, Exhac quidem confideratione plurima pendêt, quæ tư in Optica, tum in Aftrologia,tum in Mx

## PROPAEDEVMATA

magnitudinem:qux etiam mutabilis eft. xtvitr.

SOlem infra noftrum verum horizontene exis ftentem, accidentarij fui luminis radios ad nos ab aëre procurare, Crepufculinę eius Luces demonftrãt : Tresigitur Superiores \& fixarum plurimæ, cum magis fub horizonte latent,quàm ipfe Sol, in Crepulculi matutini principio, vd vefpertini fine, nobis, fui accidentarij Luminis virtutem, (licet perfenon tam fenfibilemquàm Solis)communicabunt, inftar quorundam fuorü crepufculorum . Planetas etiam Sole inferiores hoc modò confiderandos moneo . Fit̛́y hoc (vt dixi) non er principalem aliquem radium, (cis, licet vel directum fractum vel reflexum) fed per
 vulgariter loquuntur philofophi . Qua ratione Solaria Crepufcula inxqualiafiant, vide: \& de aliorum planetarum Crepufculis (vii nos nunc illa appellamus)(imili perquiras methodo.

## $\mathbf{X L I X}$.

$Q^{\text {Va ratione ftellx fix } \& \& \text { finguli planete, tam }}$ infra horizontem, quàm alibi conftiuuti, ad nos vel alia terrex loca, radiosfuiluminis,non ab ipfo ccelo folum, fed aëre, nubibus, aqua, mõ, tibus, $\&$ fimilibus corporibus reflectât, perfcru tare:radiorumós coeleftium fractiones multipli,

## APHORISTICA.

gia,magni effemomẽti, experientes percipient. $\pi \rho^{\prime} \rho \mu \boldsymbol{\sigma}$
Quxcunçigitur duo cocli puncta ex diame. trofunt oppoita, vnoquog temporis momento in infinitis extant veris Horizontibus: Sed quar cunq; duo coli puncta, minus Semicirculo difiterint, in vnico tantum haberi poffunt Hori. zonte vero,eodemtemporisarticulo.

## XLVI.

$\mathrm{O}^{\text {Mnes ftellęmaiores terra, ab aliqua fui por, }}$ tione radios fenfibiles directos, ad nos mittere poffunt, antequam earundem centra ad noftrum verum horizontẽ oriendo peruencrint: Atque ratione eadem, in occafu, fub ipfo vero horizonte depreffis earundem centris, nostamen illuminare fuis directis radijs poffunt.
XLVII.

OMnes felle, cum in horizonte vero alicuius loci terreftris fuerint, plus in recta linea, ab illo loco diftant, quàm cùm fupra illiusloci horizontem funt eleuata : fiue vno codémque die, fiue quibufcunque diuerfis:modò eiufdem ftelle, in illis varijs temporibus, equalisfuerit diftantia àcentro terrex. Alióqui enim Sol in Capricorni principio oriens, longènobis propinq̣uioref, quàm quorum imminet capitibus, inCancroverfans: \& hoc propter fuæ eccentricitatis
C, iiij): magnitüdinem

## APHORTSTICA.

 ces attende in aëre, nubibus, $\&$. aquis: Et infini; tam Dei bonitatem Sapientiamó admirari \& laudare cogêris.L.

VT Stella quelibet proprium habet nomen ex ipfius Dei impofitione, Sic \& naturam in fe habet virtutem'́ propriam, qualis in nulla alia, eadem omnino inueniri poteft.
A quodlibettotius mundi punctum, 8 quo, libet temporis momento, ab omn bus fellis fixis \& planetisfit talis radiorum côcurfus, qualis,ex omni parte fimilis,ad nullũaliud punctum, nec vllo alio tempore, naturaliter côftitui poteft.

> LII.
$K^{\text {a } \quad o \pi i f g \mu \tilde{x} \sigma}$ fi fuerisperitus, cuiufcunq̧ Stellix radios in quamcunç propofitam materiam fortius tu multo per artem imprimere potes, quam ipfa per fe Natura facit. Haecquidem Antiquorum Sapientum multo maxima naturalis Magix pars erat: Ereft Arcanum hoc, non minoris multo dignitatis, quàm ipfa auguftiffìma



 D.i, ซigioncto ragtybbice

PROPAEDEVMATA $\pi \operatorname{mog}_{\delta \sigma \mu x}$.

HInc obfcurx, debiles, \&quafi Latentes re. rum Virtutes,arte Catoptrica multiplicata, fenfibusfient noftrismanifeftiffima. Vnde non inftellarum folùm, fed aliarum quoç rerū pros prïsexaminãdis viribus,quas perSenfibiles ex. ercent radios, diligens Arcanorum Inueftiga . tor, maximum fibi oblatum auxilium habet. LIII.

SIquid vel Solislumen per Lunam efficiat, vel quid ipfaex fefola, nullis imbuta $S$ o $\frac{1}{}$ I radijsfenfibilibus preftare poffit,cognofcere quis cupiat:ex plenilunio, \& Lunæ eclipfi totali cum mora, artificio catoptrico, elicere poteft. $V_{t a d}$ alia autem, eũdem traducat experiendi modum, nonopus eft vt moneam.

LIIII.

QVò magis ad perpendicularitatem fuperali, quam elementarem fuperficiem accedita xis radiofus alicuius ftellx, eò fortius circatalem fux incidentięlocum, fuas vires illa fella impri, met:directoquidem modo,proptermaiorem 2 gẽtis vicinitatem: reflexo autem, quia reflexitaz lesradij, ad incidentes, vicinius conduplicantur. Eccẽtricitatis ratio, in diuerfis zodiaci locis,pla netas propioresnobis exhibere poteft, cum acur rifimusprorfus erit incidentix angulus cumno-

## PROPAEDEVMATA

tiquatuor $æ$ qualium horarum $f$ patio, æquatoris conficit peripheria:atque hunc Diurnum Toti, us motum vulgariter vocant.
LIX.

QVò equatori funt propiores parallelícircu li,eò citatiore motuverfus occafum, illorum circumferentix, $x$ quatoris fequuntur motum.

$$
L X .
$$

$Q^{\text {Vam inter fe rationem habuerint, circuloriu }}$ duorum quorumcunq xquatori parallelo, rum, circumferentix, eandem rationem habe. bunt, 8 earundem velocitates, indiurno Totius motu: Hoc tuad planetas \& ftellas fixastrãsfer, diurnorum arcuumrefpectu.\&c. Circumferë, tixautem eam inter fe habent rationem, quam ipforumDiametri Circulorum.

$$
\mathbf{L X I}
$$

PEriodos quafcícg videmusn a t v rab prx potentis inuiolabili lege, à cocleftibusipfis abfoluicorporibus,maxima cum diligentia , à nobis animaduertendas afferimus: PERIO D V m hocloco vocamus, planetx, ftelle fixæ, vel alicuius toeleftis puncti, ad priorem locum vel priori valde fimilem, per circularem motum, completam reftitutionem. Tempúfleq quod in terea fluit, huiufcemodi Conuerfionis, Perio' dumnominamus.

L×I.

APMORISTICA.
ftro vero horizonte, vel aliafuperficie . At nos, \& fupra de hac re diximus: \& nunc fignificamus, in xqualibus à centro terræ diftâtijs, generalem hunc nos enuntiare aphorifmũ : effe tamen tum veiliflimum, tum iucundiffimum confiderare ex. ceptionis huius rationem, in varï's eccentricorum circulorum locis.

## LVo

$\mathrm{Q}^{\text {Vò ftellaceiufdem Mora,fupra horizontem }}$ maior fuerit,eò ad fux virtutis fortiorem faciendam impreffionem, per directosfuos radios,eft accomodatior.

$$
L_{\mathrm{V}}^{\mathrm{I}} .
$$

E Xhorum tantùm trium diuerfa contempe ratione, fcilicet Vicinitatis, Anguli incidentix, \& Morax, ô quàm multiplex confurgit ratio pro viribus eiufdem ftellx exercendis, fupra 2 licuius loci horizontem.

## LVIT.

M Omentaneus quilibet coeli ftatus, tum effectus fuosmetit infinitos,tum in aliorum euentuü Semina (cõgruis maturanda conftellationibus) vires intendit ac imprimit efficaces.
LVIIIt

Mnium cocleftium motuum, ille velociffmus eft,quem, verfus occafum, femper, vigin D.i.7.

APHORISTICA.
LXII.

A Natura omnes hos illuftriores recipimus circulos:Horizontem,Meridianum,,Equatorem,,$\&$ illi parallelos omnes: Eclipticam: Ec 3 centricos planetarum: Epicyclos , \& alios, quos ex Theoricis planetarum, Aftronomicífqe Cas nonibus, accuratè difcendos,monemus.

## LXIII.

$C^{\text {Irculi omnes, Pofitionum (vulgariter fic dis }}$ cti) funt circuli naturaliter definiti: $\mathrm{Cũ}$ om= nes illi quorundamaliorum locorumfint horis zontes veri:ctiamfi infinititales, inter horizons tem tuum 8 meridianum ftatuerentur. At quò propiusverfusmundi polos accedis, Naturam vides quafi pedetentim iftos recufare: duas'̣́ tãs tumex tribus illis generaliffimis, Cocleftia The mata defrribendi vijs, fibi fub polis affumere: vt \& fub $x$ quatore duas precipueadmittit:in locis autem intermedî̀s, tres: per meridianos filicet: circulos,eclipticx longitudinem ad rectosfecãs tes angulos: \& per iftos horizõtales: licet infinis, tisalijs modis, Natura, fuarum diftinguat virium proprietates.
LXIIII.

PEriodus $x$ quatoris, eft alicuius in $x$ xuatore, vel alterius puncticceleftis, ad eundem mes, ridiannm, reftitutio: viginti quatuor xqualium horarum fpatio, per motum Totius diurnum, D. iij. abfoluta.

PROPAEDEVKATA
abfoluta. Hxc autem omnium coeleftium peris odorum, eft fimpliciffima, fibíq̧ femper xqualis,

> Lxv.

DIes naturalis, fiue periodus Solis diurna, eft tempus quod fluit, dum per Totius motum diurnum, Solis centrum ad eundum reducitur meridianum : Ifta quidem periodus, valde inx. qualis exiftic longitudinis.

## LXVIO

ANnus tropicus folaris, eft tempusperiodis cum, quo Sol, per proprium fuum motum, adeundem eclipticę fummæ locum reftituitur. Huius magnitudo hac noftra xtate, obferuata eft, dierum effe 36 , horarum 5 , \& f frupulorum primorum 59 , fecundorum autem, ferè 20 . Mus tabilem etiam huius effe longitudinem, obferuar tiones excellentium Mathematicorum exactiffic ma, demonftrant.

## LXVII。

$A^{\text {Nnus Solaris fiderius, eft têpus periodicum }}$ quod labitur interea dum Sol per propriiu motum fuum, ad eandem ftellam fixam redit: vel ad $æ$ qualem prorfus diftantiam (fecundū eclips ticx longitudinem) ab eadem ftella fixa. Cuius magnitudinem, Thebites, Choræfilius, inuenit dierum naturalium 365 , horarum 6 , fcrupulos rum

APHORISTICA.
rum primorum 9 , fecundorum autem 20. CO pernicus autem aliquanto maiorem, hoc noftro feculo effe, demonftrauit : per 20 circiter fes, cunda, frilicet.

$$
L X V I I f \text {. }
$$

L Vnares periodos veras, tũ ad eandem eclips ticx longitudinem, tum ad Solis coniunctis onem, exacta ratione per numeros examinatas, proquocunç dato tempore, habeas. Sunt enim inequales valdè.

## IXIX.

PEriodus Lunx diurna, fiue dies Lunaris, eft per motum Totius diurnum, lunaris centri ad eundem meridianum reftitutio perfesta: fins gulis penè diebus, hęc, fuam mutat quantitatem. Similesetiam reliquorum planetarum reftitutis onesad eundem meridianum, confiderantes, $e^{1}$ afdem appellabimus corundem Dies : videlicet vel Saturni, vel Iouis,vel Martis, vel Veneris, vel Mercurij.Fixarum ftellarum tardiffimusmotus, dieivniusfpatio , parum exhibebit difcriminis interfuam \& Æquatoris diurnam periodum.

## $\mathbf{L X X}$ 。

VT Luminariū fecundũ eclipticam, ita reliquorũquinç planetarũ omnes, quas verè \& naturaliter côficiunt periodos, tibiomnitẽpore D.iiij. perpendendas,

## APHORISTICA.

aftrologorum vt vtamur phrafi)poffit cenieri. Iftam autem Imitationẽ varij́s poffemodis fieri, cuiutis conftarecredo philofophanti. Non me ergo cft vel in Motufolo, Forma vel Figura, fed in alijsetiam proprictatibus \& qualitatibus, hāc obleruari velle putandum.

$$
\text { Confectarium. } \mathbf{x} \text {. }
$$

$M_{\text {Agus proinde induftrius, Microcofmi A. }}^{\text {A }}$ nalogis ftellaturis, ita Signata, applicando, Harmoniam experiretur maximam. Qux enim Vni Tertio côueniunt, 8 interfe conuenientiam habere neceffe eft.

$$
\text { Confectarium. } 2 .
$$

$H_{\text {tis, quale }}^{\text {Orum ergè Trium, duobus quibufcürs nos }}$ tis, qualequarendum eft Tertium, confta, repoteft.Horum'́s Trium Anatomix, fingulos xum proprix, fu: tin reliquis duobus: Sed modo quidem diuerfo, fcilicet Colefti, Terreftri, vel Microcofmico.Exempligratia,Solem, Aurum, \& Cor hominis, tibi proponimus ex Anatomi $\varepsilon$ Magicx confideranda Legibus.

$$
\mathrm{Lx} \times \mathrm{ifit} .
$$

INqua fignificatione aliquis planeta,ftella fixa, 1 plurium ftellarum commixtio, vel coelilocus, precipuè excellit, ad illum Significatorem, oms nes reliqui tum planete tum fixx, in illa quidemfignificatione comparari debent: vt quid vel au,

PROPAEDEVMATA xilij, vel impedimẽti abillis recipiat infui mune ris adminiftratione,artificiofa eliciatur indagine.

L XXV*

: QVòd Fixarū mutua interualla, exomnitem; poris æeternitate nunguam funt mutata, hut ius elementaris mundi illis rebus, quax \& fuit etiam ftatus conftantem valde retinent conditio. nem, iftasmaximè præeffe demonftrat. Cäm ta. 2 men, \& ifta, Motuquodam(frilicet tardiffimo) fecundum Eclipticę longirudinem verfus orientem, tam ferantur vniformiter, ac fi omnes vnoe. odem'̆́s agerentur fpiritu, hoc quidem 8 ©maxi marum noftrarum rerum, feu illarum quasiam, è noftris, maximè conftantes, fuićç fimiles maxi mè, iudicamus, mutationes, viciffitudines'fieri 3 Tignificat. Iftarum denics perDiurnum Totius motum, Circunductio:ad totam illam coleftem conftantem'́s Harmoniam, ex omnibus fellisfif xisrefultătem, qua fibi mutuò funt colligatę (queg etiam rerūomnium quafi Forma Prima exiftit) toti elementari regno, 8 totam cuilibetciufdem particulx, per principales partim fuos radios, partim per accidẽtarios, abundãtiffimo quidem modo impertiendam, (ita ordinante Totilis beneficentiflimo \& Sapientiffimo Opifice) eft inftituta.Et hoc ni effet, Nullum, ne vno quidf die( naturaliter) praferuaretur Indiuiduum.
$\pi \times X V$

## PROPAEDEVMATA

nobis maximè diftent) terra plus octodecim vis cibusmaiores exiftant: tum eciam, velquòd ma. terix, in quam agunt, aptiffimam inueniunt difs pofitionem : vel quòd ab aliquo planeta, earuns dem corroborati radï, viuacioresquafi, firmio. resćp in terram torquentur : vel ab accommoda. tiffimo aliquo Tov $\pi$ tegeveross ad ftellarum expri mendas vires loco, adiur $\ell$, tam exiguo temporis interuallo, fuarum repetant virium effectiones. Quid de illis ergò fixis cogitare debemus,quauü alix totum terreftrem globum fua mole trigefi. es, alix quinquagefies quater, alix feptuagelies, alix octuagefies excedunt? Sed illarum (teque, fo) qux terrex foliditatem, centies feptiesq́ fua complečtuntur magnitudine, quantam credere debemus effe efficientiă: Ab omnibusergò onv nium ordinumfixis, diuiniflima per coelum diftributis harmonia, quantam quafi diuinitatem fimulinterras deriuari cenfendum :

## LXXIX.

SIex Diei naturalis tempore, deducatur vna xquatoris periodus,refiduumós tempus inx: quatoris partes refoluatur, clariffimè apparebit quanta æquatoris portio, verfus occafum, ver' naturaliter'́ć, (preter fuã integram periodum) intra vnius diei naturalis fpacium, per afcenfio, nes(Rectas, nominatas) promoueatur. Atç hee eft vera \& propria demonftratio, illius vtilifi,
LXXVI.

V T Motus Fixarü proprius, generaliternobis demonftrat, eafdem talium effectuum effe caufas, qui longo temporis curfu incrementa at $\mathcal{F}$ alterationes fufcipiant fuas: Sic pro nature proprietate, quę duabus quibufcū̆q vel pluribus fixis (tam ex fenfibili earum radio, quàm ex virtute fpecifica) ineft, ipfus naturam euentus, qui àduabus, vel pluribus ftellisfixis efficitur, figni, ficaturúe propriè,diuerfam effe, eft neceffe.

## 77.

A Gens debile, vt actionısfortioris fpecimen
edat, quàm Agens fimpliciter reftimatũ fers tius,fępè vfuuenit: $\&$ hoc, aliquãdo propter di= uerfitatem Subiectorum, (in que agunt) in difs pofitione fua natiua, fiue artificiofa: aliquădo aus tem, propter alias caufas. Hoc maximè norũt, qui Artis Sanctex Limina Salutîrunt. Quodritéenim Septies eft Separatū , Prxparatū fft, vt $\mathrm{Se}=$ pties quocs Coniungatur : ad celeberrimam ila lam philofophorum Gamexam conficiendam.
 reaudeo: quod ita nobis Dualiter exprefsûeft. LXXVIII.

NOneftergòmirum, fixarum Stellarũ, quał dam, qua inter illas minimx iudicantur, annis fingulis certas atq̧ fenfibiles in aëre \& allijsre, bus,eftectus producere : Tùmquòd illx (licet à E.ij. nobis

## APHORISTICA.

męacadmirabilis Aftrologice Praxeos, quę cö. muniter DIRECTIO appellatur DIVRNA. LXXX.

QVando illum Æquatoris progreffum Dires Ctorium, quolibet die naturali, fecundum afcenfiones Solaris loci rectas, examinaueris, tunc vnàetiam totius cocleftis Machine, alium quemcunqq libet, contuere locum:cuius quanta fit facta promotio Directoria, fuper vel meridianü circulum, vel horizontalem, tali loco accommodatum, intereatemporis, dum illam principalem, inSolis loco metimur, diligenter annotabis. Di, reftorijautem motus quantitatem, nunc per afcenfionesvel rectas vel obliquas, definimus.

## LXXXI。

EXDie Lunari,fubtrahas Æquatoris periodü, \& quâtum, illo modo,in die vna Lunari, cunEta cocleftia loca, pro ratione fuarum vel reĉtarū vel obliquarum afcenfionum, Directorič (vt ita dicam) protrudantur, clarum euadet.

## LXXXIf.

PEriodus Horizontalis Diurna, planetre,ftels lauíefixx, eft tépus quod fluit, dum illorum centra per motũ Totius Diurnum, ad cundem reftituuntur horizontalem circulum.
LXXXIII.

EXHorizontali Solis vel Lunę periodo,vnam: E.iij. aquatoris

PROPAEDEVMA舀
xquatorisperiodum fubtrahe : refiduum, illam xquatoris portionem monftrabit, qux (prater vnamfui integram reuolutionẽ) verfus occafum, talis periodi fpatio, Directoriè promouetur.

## LXXXIIII.

LIcet Solis \& Lunx, generaliffimx fuerint \& clariffimę vires, in hocDirectionũ artificio, Reliquorum tamen quinç planetarum(maximè in eorum proprís fignificationibus) \& Fixarū, multiplices efficientix, fimili debent obferuari difçiplina: tam in eorum diurnis ad meridianos reuerfionibus, quìm ad horizontales quofcungs circulos. Nüllis autem nos, alīs quàm veris, nüc vti ftellarum motibusmemineris. Caucantergò quivel ingulis diurnis planetarũ Directionibus vel annuis(dequibus alibi agemus)certam, cant demóq profcribunt vel graduum vel minutorum quantitatem.

## $\mathbf{L} \times \mathrm{xXV}$.

PEriodidiurnx quinç planetarum,quãdore trogrado feruntur motu, xquatoris periodo funt minores.Vnde per iftos, tum $\begin{aligned} & \text { equatorem, } \mathrm{u} \\ & \text { ü }\end{aligned}$ alia fingula mobilia coeli loca, verfus orientem poftponi eft neceffe. Hancóp requatoris periodi anticipationem, Veteres, Directionem conuerfam appellabant. Hanc autem tamad Meridia nos quàm etiam Horizontes referri, non eft ne ceffepluribus docere:aut ex xquatoris periodo, retropedantium

## PROPAEDEVMATA

periodum complecti,eundemfacit: \& ad precipuûffuum deniç munus conficiendum (fecûdum Ecliptiç̧ fcilicet Longitudinẽ)multò reddit ha: biliorem, fignificamus. PLANBTA sergò, curfu DIRECTO progredientes, generaliter iudicare fortiores, fortunióq quodă affectos, noneft ìratione alienum. Vnde motu Latos v E LO C 1 , cer. tiffimü eft,plus tühabere forticudinis, fuas'̧̧ t tum forlicius peragere fignificationes. Quando cum planetarum veloci curfu,eciam concurriteorundemad terram propinquitas maior, ex Theori sis conftare tibi poteft.
LXXXVIII.

PLanetaretrograd vs, Naturecone ftăs decretumquodam modo perfringere vis detur : periodum fuam diurnam breuiori abfoluēdo tempore,quàm ipfe Æquator:cuiusmotus, è quod citatiffimus eft, fibi'g femper xqualis, Temporis fit nobis norma.Secundò, cum exge nerali Naturx inftituto, Coeleftia cücta, in mo, tus diurni ratione, primum fequi Mobile debe rent, Retrogradus autem ifte planeta, (quafif bicommiffishabenis) fuo nifu,primo Mobilia liquam huius fui muneris particulam praripere videtur. Tertió, ex Diurna fua quaç periodo, atiquam illius vniuerfalis Harmonix particulam excludit: \& poftaliquot elapfos dies, notabilem Totius portionem, verfus ortumrepuliffe vide

APHORISTICA.
 ferri debere,cùm fatis per fe fint clara.

## LXXXVI.

EXiovis periodis diurnis, adxquatoris periodos comparatis, vera patet \& phyfica demôftratio Directionis cuiufdam,ab Antiquis, PROFECTIONIS ANNVAE, nuncupata: In cua, coeleftia nonnulla loca, per vnum circiter Dodecatemoriü, verfus occafum promoueri tradunt. Verùm, fi vel Profectionisiftius partes, ad Iouis verum diurnum motum : vel ipfam annuam Profectionem integram, ad Iouis verum motü in vno annoSolari, referre velis(vt Naturate facere vrgebit) clariflimè tunc cernes, nee directo femper modo ifta dirigi : nec eandem effe (fingulis annis) graduũ multitudinem, qux vel fupermeridianos, vel horizontes varios, pro ratione Iouialis motus veri, integre Profectioni annux refpondet: Deniç non folùm quing vel quindecim loca ita confiderari poffe aut debere, fed infinita ferè, tam planetarum fcilicet, quàm fixarum. \&c.

## ixXXVIT.

$Q_{\text {Vomodo Direct vs Planctecmotus, nõ }}^{\text {Von }}$ folũ ad eiufdem maiorem fupra noftrũ Horizontem exhibẽdam Moram, confert, effe perpendendû:fed quactiam ratione, intra fuam Diurnamperiodữ, Harmonicam illam æquatoris

E, iiij) $^{\text {periodum. }}$

## APHORYSTICA。

bitur:quandam'̛́ magnã xquatori Iniuriam in tuliffe : cùm ille,verfus occafum,perpetuò rotari debeat. Quintò, pertinax ifte planeta, munus fuum proprium, precipuum ${ }^{\beta} \neq$ deferere videtur. Propria cnim cuiulq planeta periodus, verfus ortum abfolui debet. Sextò, opporunitatem illam qua ad fuas fortius exercendas vires, vti po, terat, (obmoram fupra noftrum horizontem maiorẽ) recuarare iudicabitur. Nec Solem igiur, néque Lunam (omnium corporearum creaturarum praftantiffimas, mundóg elementari beneficentiffimas, immò rerum hic omnium quafiParentes) iftisimplicari retropedationibus, voluit Deus. Neq̧ reliquos quidẽ:nifi ad breuequods dam tempus (fiad integras eorü periodos, illud conferas) tali vtitergiuerfatione, patitur. Verùm nullo cum natvrae vifversalis incommodo, hoc ab iftis patratur.. Nonmagis quàm acerrimæ illx infinitarum pené rerũ Antipathix, NATVRAE VNIDERSALTS ftatum vilo modo labefactant: quín ad gratiffi, mum potius ornatum egregiè faciunt: Xad N A= TVRAE perpetuandamincolumitatem, conducuntvel maximide x retrogradatione tamen, parricularis aliquis effectus (quem fcilicet talis planeta infereceperat perficiendum) interim non promouetur, fed quafi retroagitur:FaCtaćs Infecta fieri videntur. At quiseft, qui hac, F.i. tum

## PROPAEDEVMATA

tum in Politicis, tum œconomicis negotijs effe neceffaria, fumméǵ interdum vtilia, nõ cernat:' Satius'q́ efferecurrere(ve dicitur)quàm malè cur, rere** Luuat ergò interdum planeta retrogradus, licet non directo ordine, fed quafi fortuitò, \& ex abrupto:\& in contraria ferè fignificatione. 89.

P Lanetr in maximisfuis à Terra diftãtifis(cir cafua fcilicet Apogra versãtes) in rebusquarum tunc fuerint proprij Significatores, fortius magnificentiúfç fuas exercē̃t vires, quàm incif dem faciunt, quădo Terrę, circa fua nimirũ̃ Pe s rigaca, proximi feruntur. Contrì autem, in alī̆s fibi fubiectis rebus, viuacius efficaciúfy operang tur, in fua maxima ad Terrã propiqquitate,quàm in eifdemoperari poffunt, quãdo à Terra, quàm queantlongiflimé diftant. Huius Aphorifmi de, monftratio ex $41,43,73,77, \&$ alijs prius explicatis aphorifmis, maximum fuum \& lumen \& robur habet. Vt ergò ineadem, rexum per cundem planetam fignificatarü, fpecie, diftinctèex actég iudicium proferas, loca maximarum \& minimarum a Terra diftãtiarum, pro vnoquoc planeta,fint tibi prius nota. Per artificium autem Catoptricum,quinç planetarum Aliquem,(id'g paucorum dierum Spacio) longiffimè à terra diftare facies: Et denuò(ictu ferè oculi) ad Peri, gẹum,q̧uafi Noum, deducere poffis. Quofdam

APHORISTYCA.
meolimlegiffe memini, in SoleLuná̛́ idem fu.
 90.

QVoniam Solisnon eft femper acqualis potētia, nec eadem fignificandi ratio:fingulorự̛̣ etiam planetarum fint diftinctę fignificationes, ac alix alięg corundem fiant vires, non debet idem de vniufcuiufq planctę COMBVSTIONE, pro. nuntiari Iudiciü. Licet autem Solis excellentiff. mafuerit \& potẽtiffima virtus, nõ tamẽ femper 1 ledet, dü alium planetã combvrere Aftrologi dicüt. Fieri quidem poteft,vtille, Côbufti pla netæ naturã ad amplitudinem quãdam \& mage nificentiam euchat:eiufdem omne ius, in fuas virestrãsferēs.Sed dü lędit, varia eft ratio. Ex Graduationü regulis, de quibus fuprìaphorifmo 1 \% egimus, quid fit omnitẽpore de tali Côbuftione ftatuendư (quantum ad fenfibilium radiorum o, perationem) fimplicibus femel definitis planetarum naturis, clariffimè depromi potef..
xc .

NVllus eft terreftris globi locus,quem Sol,Saturnus, Iupiter, Mars, aut ftella fixa quęcü ©, nôo illuftrat fuo directo fenfibilíq radio,fpatio vnius fuarum diurnarũ periodorü̆düfub Æquas tore,fecundum fua veraferantur loca.Maximum igitur eft huiusloci priuilegium: exquo, tantillo tempore, totusterrx orbis fenfibilibus directif $\boldsymbol{\beta}_{3}$
F.ii. horum

## APHORISTICA.

fub Meridiano inueniri, cuiuis, vel mediocriter in Aftronomicis verfato, notiffimum effe fcio. Hinc in locis, quorumV Vertices inter xquatore $\&$ Mundi polos fuerint, illa Eclipticx pars, qux fubMeridians, quocưç propofitotempore reperitur, Cor cocli, appellari cxpta eft : Nonagefima autem pars ab afcendente loco, Domus decima. xciili.
S Tellhomnes, vt funt Luminis participes, ita (prater fuorum infenfibilium radiorum $\& C$ fpecificas fuas vires) caloris cuiufdam funt efficientes caufx.
95.
$V^{T}$ s o $\frac{1}{}$ fingula coeleftia corpora, fua fupe rat magnitudine,Sic coeleftis Luminisquay fifons perennis ac immenfus eft : calorisóq́ nobis fenfibilis, ac vitalis, preccipuus effector.
$x \subset \vee 1$.
I Llum Calorem, quem Solis radiofi Coni tota 1 Bafis (ipfotunc Sole, in fui circuli Perigxo, \& inminima Eccentricitate verfante) inillud ter= renx Superficiei naturale punctum, quod tum fui radiofi coni vertex fuerit, tum etiam cui Sol perpendiculariter imminet, efficiendo exercet, (Deftrinę huius noftra illuftrandxegratia) cffe potentix cuiufdam, inftar Sexaginta, fiue Centū graduum, ponere folemus.
E.iï. XCVIS.

NOn poteftergò nobis ignotum effe，quanto calore fuo proprio，aliud quodeunç terreni globi punctum，cui sol inquouisaliofui Cir－ culiloco，perpendiculariter imminere poteft，aff： ficiet：refpectu illius fui maximi caloris．

## XCVIIT－

ETquiSolis fibi impendentis calorem，in ali， qua conuenienti materia aptè experiri noue． rit，Is，non fecundum proportionem folim，fed etiam fecundum rei veritatem，intelliget，quâtum calorem omni alteri punctoterreftri，cui immi nereporeft，impertiet．

$$
\mathrm{xcIX} .
$$

DAta próportione inter duos caloris gradus， quos Sol in duobus diuerfisf fui Circuli locis， in terrena loca，illi perpẽdiculariter fubiecta，ex． ercet：Si，quocunç datotempore，（lucente nobis Sole）per aliquod artificium noltrū，à nobis fenti－ biliter excitari poteft Calor，qui vni dictorũ fiv erit æqualis，poffibile eft etiam，per artificữ\＆ induftriam noftram，vel codem momento，vela－ lio quocunç（LucenteSole），talem calorisgradü fenfibiliter excitari，qui illi alteri ift æqualis．Ad quantã autẽ diftãtiam，hîc nõ eft explicãdi locus，
$\mathbf{P}^{\text {Erhoseofdem Canones，accuratius examina，}}$ quantum

## $P R O P A E D E V K A T K$

 CII。VTLVx\＆mOTVS funt coeleftiü cors， porum maximè propria，ita inter planetas， SOL，L VCE propria omnes alios fuperat：\＆ L V NA，proprijo M O TV $s$ pernicitate，reliquos omnes vincit．Hi ergo duo，omnium planetarum excellentiffìmi，meritò cenfentur．

$$
103
$$

L v NA，potentiffima eft humidanü rerû mode ratrix：humiditatifp excitatrix \＆effectrix． 104.
$V^{T}$ Tolis excellentem LVCEM，procipuut vitalis caloris moderamen comitatur：iacuiu LVNAE mot V ，miraquadam analogia，cons iuncta eft eius vis，humiditatis effectiua $\&<$ mo． deratrix．

$$
105
$$

I $V$ NA quò terrex propinquior，\＆proprio motu，quò fertur velociori，eò fuum in reshu： midas，potentius exercet dominium．

$$
106
$$

Solem \＆Lunam omniūjn clemẽtali muns do nafcentium \＆viuentium，tum procreatio， nis tum conferuationis，preccipuas（poft Deum） \＆verè phyficas effe caufas，ex his fit manifétiffi， mũ．Per Calidū enim \＆Humidũ，$\pi$ स̉vra $\sigma u y \times$ gíns


APHORISTICA．
quantum reliqui planete，à Solis virtute calefacti－ ua deficiant，ratione bafium fuarum Conicarum， refpectualicuius punctiterreftris，cui perpendi－ culariter imminere poffint，in minimis corundẽ àcentro terrx $x_{2}$ diftantrís．Iftorum bafes $\&$ diftä－ tias，adSolis．bafim \＆diftatiam comparabis：\＆ Calores ab iftis procreatos intelliges．н о c tamẽ memoria tu femper teneas firma ：vnumquem $\boldsymbol{c}_{\beta}$ Planetam，ex fui proprii corporis ratione，fenfi－ bilem aliamqualitatem，generali caloris comis fcere virtuti．Et qualis illa fuerit，non in omnibus folum planetis，fed ftellisetiam fixis，（ Si $_{53}$ apho． rifmum experiaris）per Lunam expifcari potes： \＆alị̂s eciam vijs．
c1.

VArietas Lunaris caloris，in quodcunç cui perpendiculariter imminere poteft puns Atum，per Solis etiam canones cognofci poteft． Scilicet，finon folum eius，ì terra diftantiam，fed fux etiam illuminatę partis conuexx，quxad ter， ram conuertitur，quantitatem，（inftar ipfarum conicarum bafium in alijs planetis）quocunque propofito tempore examinemus．Non tam aptè tamen Lunares fefe（ad operandum）coadiuuare radios，in Corniculari cius figura，quàm cìm ad orbicularem magis accedat，Cauti \＆diligentis Aftrologi iudicio，relinquo confiderandum ：vt \＆aliain iftis Aphorifmis multa．

C．I．

APGORISTICA。
Ifta enim duo folum，joviux funt．

## 107.

A Nniconftiturionem generalem，ex quolibes certè die，per quãdam analogiam，efle demō． ftratan videmus．Habet enim quilibet Dies na－ turalis，fuum，tum ver，tum $£ f$ fatem，tū Autump ，num，tum Hyemem．Ex folo ergò Solis calore， ，perfe parim，partim per accidens，omnes pris ，mx produci poffunt qualitates， 8 neceffarioors ，dine．In quibus，fi principia，media，fincíq ftants ＂amus，Duodenarii cuiufdam rationem cernemus Etpulchrum eft confiderare，quo modotandem fubipfis Mundipolis，ipfe Annuseft nifi inftar Diei vnius naturalis．Aphorifinum iftumad al－ tiora traducas，\＆maximum Secreuūhabes，Tu， qui Trinitatis in vnitate，mylteriatractas phyis ca：\＆ad Noctismulticoloris Nigredíne，Opus inuoluendum tuum，anhelas．

## CVIII．

V Igintifex diuerfas habinudines，qua inter fixa fidera \＆C Solem effe poffunt，prodiuct， fo iftorum \＆Solis in quatuor Angulis pofitu，ad alios etiam planetastrāsfer ：maximéad Lunam． Sic＇p confurgẽt，exomnibus planctis，cum ftellis fixis，hocmodo comparatis， 182 diverfar ratio－ nes côfiderandę．Ex magnę côftructionis Ptolo－ męi，libro octauo，has dilces ad Solê habitudincs， G．i．

CIX。

$\mathrm{C}^{\circ}$Orporis imperfectio, proxima \& maximé propria Mortis phyficx caufa eft,non Ani. ma.Mortis ergo naturalis, caufaquoque naturalis: Ex Nature igitur generalibus Gubernatoris bus, generaliter pẽdet \& pręlignificatur. In $\mathrm{H}_{u}$ mario certè genere, Nemo vltimum fibia Deo prafinitum viuendi Terminũ pręterire poteft: Negligẽtia autem, pauciffimi illû̃ attingût : Du plices vnde côftathumanx vitx effe Terminos. cx:
A Nima humana, \& Forma vniufcuiuf̧ rei fpecifica, multò \& plures 8 preftantiores virtutes, operationéf $\mathscr{C}_{\mathfrak{p}}$ habet, quàm vel iplü Cor pus, vel ciuldem rei Materia.
cxi.

INenfibiles, Intelligibiléfuc planetarum radij; ad corumfenfibiles, funt inftar Animę cuiufdă ad fuum Corpus.
CXII.
$S$ Iderum quacdam, eatenus mal e f i C A ali-, quando vocantur, quatenus corundem vires in corruptâ Naturam, vel malè difpofitam Ma. teriam immittuntur: (Hocnos docente Aphorif moSeptimo) Ipfa enim Sidera, per fe, nihiloperantur mali.


APHORISTICA.
tium, quecunquefuerit diuerfitas naturalis, eaex duabus prexcipué procedit caufis :filicetex Materiarum diuerfitate, \& varia ftellicorum radio, rum operatione.

$$
C \times I 1 I I
$$

OMnis res, quantumcunç exigua, in mundo elementorum exiftens ,totius coeleftis Hars monix eft Effectus:fiue Exemplū quoddam \& Imago. At in quibuflam rebus,hoc clarius quìm in alijs apparet.

$$
c \times v
$$

EXanalogia corporum cocleftiũ,tam infeïpfis, variè confideratorum, quàminter fe mutuò comparatorum : \& illorũ omologafem per, in ifto Elementorum regno, (exarte anobisfuprìtradita) accuratèfecernendo, ampliffimam tutibiviam, ad perfectam Aftrologix fapientiam, Iternes.

$$
C \times V I
$$

$Q^{\text {Voniam Septem planetx, } 12 \mathrm{C} \text { diuerfas Con- }}$ iunctiones nobis exhibere poffunt,(fcilicet dum bini coniunguntur, 21 : dum terni, 35: dum quaterni 35 : dum quini 22,8 dum feni $, 7: 8$ dum omnes fimul copulantur, ${ }^{\text {) }}$ ) veriffiméq́qum-

 $\rho_{\tilde{\alpha} \sigma}$ : Circaillas 120 Coniunctiones, generaliffimam hanc nos proponimus Methodum. Quan, G.ij. do

## APHORISTYCA。

nes, quantùm advirium differẽtias. Verùm,frin ${ }^{-}$ terdum duos, xqualibus fortitudinis numeris af. fici, interdum tres, interdum quatuor, interdum quinch, interdum fex, \& interdum omnes (licet rarifiimé confideremus:xqualitatemó iftam vel in fupremo vel infimo, vel intermedijs poffe in ueniri gradibus:varios inde modos,per methos dum prous explicatam, eliciemus 2029 s:quibus fiiügamus inęqualitatis abfolutę modos 5040 , confurgent modi 25335 , generaliffimi quidem: in quibusper Graduationü regulas, philofopho eft digniffimum exerceri: vilifitatem enim repor tabit, \& voluptatem immenfam. Etquò iftorum duorum Aphorifmorum veritatem, rationem'̣ Logifticam intelligas, praxeos noftrx quandam formulam tibi preponcmus, in multis alijs etiam rebus vtiliffimam. Facilés poterit indus ftrius arifex , hanc Methodum ad infinitatem quandam extendere : \& non pati in Septenario folùm confiftere numero.

Praxeos Formula.
G.iif. Pri Aphorijuo


Quoniam ratio conftructionis fecundx partis iftius tabellę difficilior videri poffit:vtftudioff in hac re aliquătulum iuuentur, exemplo adhibito, eandem explicabo. Sibini planetre tantum(ex feptem) equalis ftatuantur effe fortitudinis:inde inten

APHORISTICA.
inter omnium fortitudines, fex gencraliffimę ho bebunturdifferentix: (vt ex quinta \& fexta Co lumna patet) Atpertertiam columnam, binaria coniuctio inter feptem planetas, 2 2variis modis,alia aliạ́́ effe poreft : Etperfecundam cos Lumnam, planetarum fex inęqualesfortitudines, 720 modis diuerfis confiderari poffunt. Multiplicoigitur 720 per 21,8 prodeût 15120 .quem numerum in vltimx columnx fecundo deficendente loco inuenies: Eadem eft operandi ratio, cùm tres, quatuor, quinq, vel fex , equali fupponantur effe prediti fortitudine : Deniçad ampliorem huius rei explicationem, en tibibreuifa fimam operis formulam.

$\mathrm{C}^{\mathrm{Vm} \text { in anni alicuius Solaris Reuolutione, } \mathrm{al}=}$ terius planetx periodi notabilioris principio, velquocun'̨́ alio tempore, fortisaliqua \& rara in coclo fuerit vel planetarum inter $\mathrm{fe}_{e}$, vel planetarum cum fixis, configuratio:vel Phænomenum invfitatum Meteorologicum, Per totum terrę orbem aftronomicè Circumfpice, Quister- *
seftris.

## PROPAEDEVMATA

reftris locus fortiffimam propriamós coeli figu. ram, inquocun'̣́ velisfignificato, talis configu rationis, Apparitionífue primæ momento, obtineat, vel obtinere poffit. Hincenim nonfolum à ftellarum, aliorum's' coeleftium, \& Sublimium naturis, euẽ̃us illius Loci proprios maximè, fed ab euẽtibus egregïs Locorum terrẹparticulari, um, proprias planetarum, fixarúmue $\&$ aliorum cceleftium,Sublimium ${ }^{\text {g }}$ eliciendi naturas, mo dus datur infignis,fecretúsq. Hinc etiam Sapiês, (modò Cofmopoliteseffe poffit) nobiliffimam Scientiam haurire poteft: fiue de profperis pro, curandis,fiue remouẽdis noxijs:vel econrra:tam fibi quàm alijs. Locorum terreftrium Opportu nitas, tantieft momenti.

Annotatio.

* S icillos Circumpexiffe Magoseft verifinile, qui olinn dixerunt, Stellameivs Vidimvs IN ORIENTE.

CXIX .
 $X_{\text {itiviverestivt nos Mercurius ille Termaximus }}$ docuit.

## 120 .




SOLI DEO HONOR ET
GLORIA.


> Excufum Londini apud Res. gtnaluum Vuolfuum, Regia Maief. in Latinis Typographum. ANNO DOMINI M.D.LXVII . Іавиагу. 9 .

## Propaedeumata Aphoristica


[This is a translation of the 1558 Title Page]

> Translator's Note
> Propaedeumata Aphoristica by John Dee
> Translated by Jim Egan
> guided by the original translations
> of Scott Barker (2009) and Wayne Shumaker (1978).

To put it simply, this book is about the geometry and arithmetic that connects Astronomy with Astrology. Propaedeumata Aphoristica, or "Preparatory Aphorisms" is meant to be an introduction to Dee's grand exposition of his cosmology, the Monas Hieroglyphica. Not only does it prepare the reader to understand what the heck the Monas is generally about, but it includes specific clues (strewn about in various places).

This translation is based on a preliminary translation by Scott Barker, with firm guidance from the 1978 translation by Wayne Shumaker (and essay by J.L. Heilbron.)

My main goal is for this fresh translation to make a clear path between Dee's mind (in the mid-1500's) and the modern mind (in the 2000's).

Though the work seems lengthy, Dee gave great consideration to every word of every sentence. To capture and communicate that intent to the modern eye and ear, I have taken some liberties.

Lengthy paragraphs have been split into smaller ones to make them bite-sized and allow for breathing room. Words whose chief meanings have dramatically changed over the past 450 years have been replaced with modern-day equivalents. Parts of sentences have been rearranged to give them better flow.

Commas and parentheses have sometimes been added for the sake of clarity. However, all words in parentheses belong to Dee. [All my comments, clarifications and definitions are in brackets.] Dee's frequent Capitalizations have been maintained, as he uses them for emphasis.

The Roman Numerals of the Aphorisms have replaced with HinduArabic Numerals (but be sure to look at to Dee's Latin original mixture of both systems, because he has hidden a mathematical puzzle in his arrangement).

# PREPARATORY APHORISMS JOHN DEE OF LONDON 

Regarding Certain Excellent

Virtues of Nature


## London

In the Year 1568
[This Title Page and all the following pages are translations of Dee's 1568 second edition]

## From the Author to the Reader

I present to you, Sincere Reader, this second edition of these Aphorisms corrected by the hand of the Author himself and printed most accrately.

The edition published in the Year 1558
(as you can easily see by comparing these works)
was imperfect in many places because of the negligence of the printer.
Enjoy and use them profitably.
Farewell.
In the 1567th year from the Virgin birth
In the Month of December,
In London.

# To that most renowned gentleman <br> Gerardus Mercator of Rupelmonde 

distinguished Philosopher and Mathmetician<br>(as well as my dearest friend, by far)<br>John Dee of London<br>Sends Many Greetings



It has been eleven years (my most humane and learned Gerardus) since I left the Academy, having run through everything professors can teach students about the seven arts (so called liberal).

Swimming without cork (as the proverb says) [without a life-preserver] I began to travel to Regions across the seas to investigate the sources from which (in our age) many channels of the best of these Arts have been led to us.
I have lived on familiar terms with men whose most casual single day of writing would have been provided enough material that, if sitting at home, would have taken me a year to comprehend.

By the highest favor of God, I was able to meet you at the beginning of my travels, while we were pursuing studies in Louvain. It is from your discussions with me that my whole system of philosophizing in these foreign domains laid down its first and deepest roots. Therefore I now think it's only just and reasonable that you as a first traveler should be the first to lay claim to my labors.

This is a right you deserve most of all, as it was the custom of our shared friendship and familiarity that, in that whole 3-year period, we didn't willingly lack each other's company for as much as 3 days.
We were both so eager to learn and philosophize that when we met we scarcely left off our discussions of difficult and useful things for 3 minutes of an hour.

For the sake of such a sincere friendship and sweetly continuous cooperation in philosophizing, should we not commit to the eternal memory of men some syntagma [Greek for a collection of well-arranged writings], or monument, so that a later age of scholars might be motivated by its considerations resulting from that most sweet bond of friendship by which we are perpetually joined?

Neither of us ever criticized the other's pursuits nor were either of us envious of the others learning, but instead we put our heads together for seeking out truth and the expansion of useful sciences.

In your next to last letter, you reminded me of that noble debate we once had. This gives me the opportunity to discuss the matter at hand.

I had hoped to write a longer explanation (or rather demonstration), but my health, which has been perilously shaken for a whole year now, has not permitted me to (even though I wished it). But the Discipline itself, the power of the Heavenly virtues, doesn't seem to require a lengthy explanation. From what I have written, one can find a way of proceeding to find Apodixes [Conclusive Proofs] in the Art, with regards to an infinite number of specific situations.

I have presented and established the foundations of this discipline in a way that other principles of the Art will be readily apparent to the diligent artificer.

I have ignored the infinite anaitiologêtas [Greek for "things that cannot be analyzed"] and the useless decrees of many who cannot support what they write about with reasonable explanations.

No one can start to understand the powers of Nature simply by observing them. To you who are accustomed to be Devotees in observing NATURE: be observers of the true virtue of NATURE in these Aphorisms. These virtues are great, but they are hardly believable, except to a few Wise Men, and are known by even fewer.

When you RECEIVE this work, I ask that you publicly declare that no tôn amnêton tis" [incautious or thoughtless person] should attempt to search out and draw out (to his own harm), things that were not written for him. But enough of this.

In nearly all your letters (which I have here at hand), and especially that next to last letter (mentioned previously), you have encouraged me to publish my Apodictum [Conclusive Proof] of this new Art (as you call it) as soon as possible (or at least to share it with you).

You should be aware that besides the extremely dangerous illness from which I have suffered for the last year, I have had many other inconveniences (from those who ...) which have hindered my studies. [Probably dealing with the false accusations made against him.]

At weakened strength, I have not been able to sustain my burden, the Herculean task of finishing my work.

Thus, if my work cannot be completed or published while I can still be a witness to it, I have entrusted it to the most learned and eminent gentleman, the sole relic, the only prop and ornament of the Mathematical Arts that is still alive, D.D. Pedro Nunes of Salamanca. [Shumaker suggests D.D. stands for "Dominus Dominorum" or "Master of Masters." This famous Portuguese mathematician wrote extensively on navigation, astronomy, cosmography, and algebra.]

Recently I appealed to him to kindly and humanely adopt this work if it was brought to him after my death. He is to use his own judgement in completing, correcting and polishing it (as if it were his own) for the public use of Philosophers, .

I do not doubt that he will become a partaker of my wish (if his life and health remain unimpaired), as he loves me faithfully. He has a natural inclination, strengthened by his will, industry, and practice, to apply himself diligently to the Arts most necessary to the Christian Republic.

I have clearly explained enough about why I have been unable to satisfy your wish that the monuments of my labors be published. However, if I were not to respond to your request to provide a Catalog of my writings, you might justly accuse me of grave ingratitude.

There are the Titles of the works I have composed for myself with what means I have and despite the greatest of difficulties. They are listed in the order I most wish them (when I have more bodily strength and enjoy sweet leisure) to be issued to the public (so they are not known only by me).

1. Peri Akribologias tês Mathêmatikês (a work of mathematical demonstration in 16 books)
[loosely translated this means Precision in Mathematics]
2. The Distances of the Planets, Fixed Stars and Clouds from the Center of the Earth and the Discovery of the True Magnitudes of all the stars (a demonstration in 2 books)
3. Burning Glasses, (a demonstration in 5 books)
4. Perspective Used by the Most skilled and Famous Painters (a demonstration in 2 books)
5. The Third and Chief Part of Perspective, which Treats the Refraction of Rays
(a demonstration in 3 books)
6. The Great Conveniences of the Celestial Globe (2 books)
7. The Mirror of Unity, or Apology for English Friar Roger Bacon, in which it is taught that he did nothing with the aid of Demons, but was among the greatest of Philosophers; and that he accomplished great feats naturally and in ways permitted to a Christian man which the unlearned crowd often attributes to the acts of Demons. (1 book)
8. A New System of Navigation (2 books)
9. Various Uses of the Astronomical Ring (100 chapters in 1 book)
10. Subterranean Tunnels (1 book)

## 11. The Triangle and the Analogical Compass (3 books)

[in Dee's earlier 1558 edition, the eleventh book was peri Anabibasmon Theologikon,
loosely translated this means "Fundamentals of Theology"]
I shall remain silent for now about the names of other works which may (God willing) enjoy the public light before some of these. This little work (Number Twelve) I send forth into various regions like an Explorer. Hopefully it will return to me the true judgements of learned and honorable men and their requests that I treat these matters and bring their proof s to light.

Depending on the report form my learned friends that the Explorer brings back, I will decide whether I should lead my forces into foreign fields or have them stay home and train themselves even more diligently in military discipline.

Gerardus, it remains now for me to urge you to commit to the public studies of men (as soon as you can) your own wonderful Discoveries in that most excellent part of Philosophy which is called Physics, as well as your works in Geometry and Geography.

With these most useful and new Discoveries, you will immediately enlarge the Republic of Letters (something you have deserved so much by your many years of hard work).

Farewell, and May the Good and Great God bestow fruitful results on your most excellent undertakings. Again, farewell.

To the reader who is eager to learn honest Philosophy JOHN DEE OF LONDON<br>Sends Many Greetings.<br>[Dee's introduction specifically for the 1568 second edition]



Here are our Aphorisms, published for you with some revisions, but unchanged in their number, order, and subject matter. Indeed, I realize that these Aphorisms are for the more Advanced.

Those of you have not progressed as far in your understanding of the many great sciences may find them rather long and difficult. He who turns to them from the Common and well-worn way of philosophizing (Poor Fellow) will immediately exclaim that he is lost in a confused Labyrinth.

I have here entrusted for your studies an assimilation of everything I have been able to understand, figure out, discover, hear and see (by reading, meditating, testing and through traveling) concerning all the remarkable things that have ever been put forward in the Theories and experiments of all the Ancient and true Philosophers.

All these things, or actually the Choicest parts, have been HARMONIOUSLY CONGLOBULATED INTO ONE SOLID BODY.
[Dee writes "harmoniously" in Greek, armonikos, to allude to the wisdom of the Greeks; Conglobulated is a rarely used word, but is in English dictionaries. Con means "together" and globulus means "in the form of a globe." Dee sees all the various parts of his cosmology working together harmoniously in a solid, spherical whole. And he is emphatic about it, as can be seen by his full capitalizations.]

Besides the most Illustrious Discoveries of our ancestors, this Syntagma [composition or body of work] is packed with Wonderful and Honorable ornaments. You will certainly find them if you search diligently, through repeated readings (paying close attention to and pondering certain things in particular). Nevertheless, you must not openly reveal to the unworthy or the profane all this which, driven by my desire to illuminate and enlarge the truth (so that it will be apparent only to you), I have stretched
the sinews of my little talent to make evident,
lest (to your shame and mine)
it be turned to great harm.
Farewell, friend.
Pray wish my soul well.

From our Library at Mortlake
Year 1567, December 24

# John Dee of London, <br> Preparatory Aphorisms <br> on the most excellent virtues of Nature 

## 1.

Against the laws of reason and nature, God created all things from Nothing. Thus no created thing can ever return to Nothing, unless it is done through the Supernatural power of God and against the laws of reason and nature.
2.

In actuality, if we artfully push Nature, using the Principles of pyronomia, we may produce marvelous Metamorphoses. By Nature, I mean any Thing that has been Created.
3.

Things which are visible and are known to perform in a certain way in the nature of things are said to Exist.

But wise men can demonstrate there are other things which exist in Nature's hidden recesses which act somewhat like seeds.
4.

Anything that actively Exists sends out its Rays in all directions, elegantly filling all the various parts of the universe.

Thus every place in the Universe contains rays of all the things that have an active existence.
5.

Both the general Substance of a thing and its Specific Individual Characteristics emit their own likenesses, but the general Substances of a thing radiate far more effectively.
Of these general substances, those which are incorporeal and spiritual (or become Spiritual) far surpass those which are corporeal (and composed of flowing elements) in this radiating function.

However, things may emit their own Likenesses less completely the more excellent they are. For a perfect Likeness is given the same name as its principal agent.
6.

Just as one thing differs from another, the rays of these things differ in their power to produce and perform their effect (provided they are working on the same thing).
7.

The same rays, emanating from the same substance, can cause different effects in different things.
8.

Sometimes a thing will act upon another thing which is similar in some respects.
Other times it will act on something that is quite dissimilar.
And sometimes there is no action at all.
9.

Whatever is in the universe has agreement, accord, and similar form with something else.
10.

Things that are of the same order or are harmonious or of similar form sometimes imitate each other of their own accord. Sometimes they move towards each other's location.

One protects and defends the other (as much as possible) even if they seem to be drawing strength out of each other.

Thus, through the Activation and Union of these natural things (with their differing manners), and also through more excellent, superior things which are like the Seeds of Nature, more marvelous things are able to be shown, truly and naturally, than any mortal could ever believe. (And all this is done without violation to faith in God and without causing any harm to the Christian religion).
11.

The whole world is like a lyre which has been skillfully designed by a most excellent artificer.

Its strings are like Separate Parts of the universe. He who can pluck them dexterously will be able to bring out wonderful harmonies.

Man, in himself, is wholly Analogous to this Lyre of the World. [Dee sees a human being as a Microcosm of the universe.]
12.

A lyre is an orderly arrangement of harmonious and disharmonious tones, perfectly suited to express the sweetest and most wonderful harmonies, with infinite variations.

In the same way, the World is an orderly arrangement of its many parts. Among some of these parts the closest sympathy can be observed. But among others, there is harsh dissonance and noticeable Antipathy.

When combined, the mutual concord of one and the strife and dissimilarity of the other produce a common Whole, a Union worthy of admiration.
13.

Our senses are not the causes of perceivable rays which flow from things, but instead are the witnesses of them.
14.

Spiritual likenesses as well as natural likenesses flow from things to us by way of light (through our sense of sight) but also without the use of light (through our other senses) [hearing, smelling, tasting, touching.]

Particularly in the Spirit of our imagination, things present themselves to us as if in a Mirror, and produce amazing things within us.
15.

No motion is more perfect than circular Motion. Nor is any quality exposed to the human senses more outstanding and extraordinary than LIGHT. Thus, these two will be especially characteristic of the most excellent and most perfect bodies.
16.

Whatever is in the universe is being continuously moved by some Effect of motion [from other things].
17.

All earthly things are ordered, set in motion, and continue to be moved by the prime motions, which are most characteristic of the Celestial bodies.

However, even Celestial bodies sometimes move up, or down, or forwards, or backwards or sometimes towards one pole of the World (or the Ecliptic) and sometimes towards the other pole.
18.

In each of the four separate great Wombs of the Larger World [Majoris Mundi magnus Matricibus] are three different parts.

However, at the same time, these parts take form and are equitably shaped by their own considerations.

They may be called by Notariacal design: $\dot{A} \dot{O} \dot{S}$ or $\dot{O} \dot{S} \dot{A}$ or $\dot{S} \dot{O} \dot{A}$.
(Pyrologians will understand what I mean.)
[Notariacal means when a letter stands for a word]
Learn as precisely as possible the natural properties of these Three and what they produce naturally.

Learn not only the primary, but also the secondary and tertiary productions.
And also learn the way of restoring the tertiary to the secondary and the secondary to the primary.

In the same way, you should give the greatest consideration to why the very same part may be the cause of not only differing effects, but sometimes opposing effects.
19.

When two, three, or four Elements are mixed together (in any quantity), you should endeavor to learn the true nature of the composition's Complexion [interrelationships] and Temperment [proportionings] by using what is called the art of Graduation.
20.

The Astrologer should investigate (to the best of his ability) the proportions of the elements in the various parts, humors, and spirits of the human Body.
It is important to test the proportions of the elements in other natural objects, as the conclusions you reach will be quite rewarding.

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21 .
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Potentially, every Seed has within itself the whole and constant order of each generation.

This orderliness is influenced by a combination of the place of the Seed's conception and the various powers in the Overarching heavens above that place.
22.

It is the privilege of the prime motion [the first motion of the heavens] that without it, everything else would be motionless.

A similar thing is true about the power of the prime [first] and most special perceivable Form which, most certainly, is LIGHT. None of the other forms could do anything without it.
23.

What philosopher does repeatedly sing this song: "Thoughts exist through bodily perturbances, so they obey bodies. They should not be grouped with things that cannot be perceived." [Dee writes this in Greek]

What mortal doesn't experience this nearly every day?
Everyone knows that the "Body is sensitive to the sufferings of the Soul." [This is also in Greek]

The Physician heals and regulates the soul through the body, but the Musician heals and controls the body through the soul.

Thus, he who is able to provide the many services of a doctor and of a musician will be able to govern the bodies and minds of men, almost as he wishes.
(Certainly discreet Philosophers will keep this a secret).
24.

What God has revealed clearly to the eyes of mortals in a Magnet, he has left to be discovered in other things through the more subtle investigations by the mind and throughdiligent experimentation.

First, I will remind you of its power to attract. Second, of its power to repel and separate. Third, of its power to orient itself in a certain direction [as in a compass]. And fourth, the ability of its rays to pass through solid objects. I shall explain other wonders of this stone of the Philosophers at another time (God willing).
25.

All stars radiate two kinds of rays. Some are luminous rays that can be experienced by the senses, but others have more Secret Influences.

This secret kind of ray instantaneously penetrates everything in the universe. But there are ways that the luminous kind of rays can be prevented from penetrating too much.
26.

The powers of the stars and celestial objects are like Seals whose characters are imprinted differently on various types of elemental material. The engraved forms of our seals are imprinted more easily and elegantly on one material than on another.

They cling more tenaciously to one material than they do to another, sometimes almost permanently. Thus you should consider Gamaaeas (and far greater things) more attentively. (Gamaaeas are a talismans-inscribed rings, seals, or stones with special powers)
27.

The power of celestial rays to penetrate everything that exists in the universe (whether the thing is transparent or solid) proves their great ability to influence and impress their energies on everything.

This might happen with such fastidiousness that the imparted power will be retained with much tenacity, in some instances almost permanently.

Thus, the material upon which the influence is to be impressed should be naturally arranged and artfully prepared (with respect to its visible form, its elemental qualities, and other properties.)
28.

The primium mobile is like a spherical concave mirror that is so solid it cannot be penetrated by sensible rays from the stars. Such a penetration would serve no purpose for celestial things. (There are several other demonstrations of this.) [In the Medieval version of the Ptolemaic system the primium mobile is the outmost sphere that moves around the earth in 24 hours.]
29.

To apply their useful effects, the stars exercise their strength not only by direct rays, but by refracted and reflected rays as well.
30.

The astrologer should not only know the true size of the terrestrial globe, but also the sizes of the various planets and fixed stars.
31.

The astrologer should also know the true distance from the center of the earth to each of the various planets and fixed stars (and how these distances vary at different times). He should also study the varying altitudes of the clouds (or of the thicker air) above the earth.
32.

It is of prime importance to be able to determine which fixed star or wandering planet is located perpendicularly above a particular place on earth (for any given moment in time.)
The angle which that star or planet makes to other places on earth (from which the star or planet is visible) should also be known.
33.

Every perceivable ray emanating from the body of a star to some external point is part of a large cone of perceivable rays emanating from the star. The Vertex of the cone is the external point. The Axis of the cone is the ray. And, finally, the Base of the cone is the luminous part of the convex surface of the star nearest to the external point.

The boundary of the cone is a circle described by the end of a straight line (drawn from the external point vertex to the star) but which barely touches the star itself [in other words, is tangent to the star].

34.

Of all the rays flowing from the luminous base of any star towards the external point, the ray on the central axis is the strongest. With regard to the other rays, the closer they are to the central axis, the stronger they are. (We will speak about the rays coming from deep within the stellar bodies in another place.)

35.

From Stars that are smaller than earth, all their direct, perceivable rays (which shine on as much of the earth's convexity as possible) emanate from more than half of the convexity of the star.

And these rays will only shine on less than half of the earth's convexity.

Regardless, the strength of the rays is based on how close
 the star is to earth.
36.

Any Star that is larger than earth will shine its direct, perceivable rays onto more than half of the earth's convex surface (at any given time).

Also, the rays they send to earth come from less than half of the star's convex surface.

Even though the rays come from a smaller portion of the star's surface, their strength is still based on the distance between the star and the earth.

[Dee does not actually illustrate these Aphorisms. These drawings encapsulate what he appears to be saying]
37.

For any star smaller than earth, (even though a small portion of the earth is affected by its direct, perceivable rays) it will pour stronger rays of Light when it is close to earth than when it is far away.
38.


All stars larger than earth impress their rays stronger the closer they are to earth.

Also, the closer they are to earth, the larger portion of earth will be illuminated by their direct, perceivable rays.
39.

Regarding the portions discussed in propositions 35, 36, 37, and 38 , you should consider with the greatest diligence the actual amounts of Surface area of the Spherical convexity of both Earth and the star involved.

These areas are bounded by the edges of a truncated cone which is tangent to both the earth and the star.
(Consider the various relative sizes of earth and the star as well as their distances from each other.)

40.

If a cone is made from a spherical star to any point in the universe, the base of that cone will always be less than half of the convex surface of that star. Astronomers should take this into consideration when attempting to measure the diameter of the star.

41.

The Closer a point in the universe is to a star, the smaller the base of that cone will be. The Farther the point is from the star, the larger the base of the cone will be.
42.

You should investigate the various sizes of the bases of these cones (for any position of any star) with respect to any external point in space.
43.

In certain respects the luminous rays from long Cones are stronger than those from short cones, but for other respects they are weaker.

Long cones have larger bases and smaller angles. For these two reasons, the following principle arises: In longer cones, the many rays (not only incident, but reflected) are more concentrated, thus they exert a greater force.

However, because of the natural and simple fact that an agent is more powerful the nearer it is, short cones are more powerful than longer ones.
44.

Accurately determine what proportion of the Moon's convex surface (which is facing us) is illuminated, at any given time.
45.

What we call our true horizon is that circle which is described by the rotation of a line whose end-point is the center of the Earth and whose other end-point is situated in the farthest reaches of the sky, in such a way that a straight line connecting our zenith and the center of this circle will be perpendicular to this circle.

However, our actual Perceivable Horizon (as I have
 shown elsewhere) is that convex portion of the terrestrial sphere which is visible to us (having removed all impediments above the uniform curvature of the earth).

This horizon is bounded by the circumference of a circle drawn by a straight line extending from our eye to the remotest part of earth we can see.
(I have also explained previously that the visible horizon will vary with the height of the viewer).

Many things depend upon this consideration and experts will appreciate that it is very important in Optics, Astrology, and in the science of the Magi.

## porisma [corollary]

In most cases, a True Horizon can be made using 2 points in the universe and the center of the earth [three points define a plane]. But if the two points in the universe and the center of the earth all fall in a straight line, there are an infinite number of True Horizons.
46.

Any star larger than earth sends perceivable rays to us from some portion of themselves before their centers rise to our True Horizon.

For the same reason when a star is setting, and its center has gone below the True Horizon, part of the star can still illuminate us with its direct rays.

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$$



The distance from the center of the earth is the same all the time. However, from any earthly place, the star will be further away when it is on the True Horizon than it will be when it is above the horizon or overhead.

However, the Sun is different. When the sun rises to be overhead in the beginning of Capricorn [around December 21], it is much nearer to us than when it turns in Cancer [around June 21]. This is because of the greatness of its eccentricity, which is also changeable.
[aphelion (the closest earth-to-sun distance) is actually around January 4 and perihelion (the farthest earth-to-sun distance) is actually around July 4]


When the sun is below our True Horizon, it provides rays of subsidiary light to us through the air, as by the brightness of twilight.

In the beginning of the morning Twilight, when the Three Superior planets [Mars, Jupiter and Saturn] and many of the fixed stars are hidden under the horizon (even more than the Sun itself) they will communicate the power of their subsidiary Light to us as if they had their own twilights (though hardly as perceivable as that of the Sun).

I propose that the Inferior Planets [Mercury and Venus] should also be considered in this way. This happens (as I said) not through any principal ray (meaning direct, refracted or reflected) but through what philosophers skilled in optics and catoptrics call Reflections of Reflections.

Investigate why Solar Twilights are not all the same and study the Twilights (as we now call them) of the other planets.
49.

Investigate why the fixed stars and various planets (either below or above the horizon) reflect to us (or to other places on earth) rays of their own light not only from the heaven itself but also from the air, clouds, water, mountains and similar bodies.

Observe and contemplate the wonders of the many fracturings of the heavenly rays in the air, the clouds, and the water and you will be impelled to praise the infinite goodness and Wisdom of God.
50.

God has given every star its own name. Each star has its own unique nature and virtue which can never fully be found in any other star.
51.

At any given point in the universe, and at any given time, there is a particular arrangement of the rays from all the planets and fixed stars.

No identical arrangement can exist at any other location (not even at the same location at a different time).
52.

If you are skilled in Catoptrics [the study of mirrors and reflected light] you will be able to artfully impress the rays of any Star much more strongly upon any given material than Nature does by itself. Indeed, this was by far the greatest part of the Natural Philosophy of the Ancient Wise Men.

And this Secret is no less dignified than the most distinguished ASTRONOMY of the philosophers commonly called INFERIOR. The symbols used in Inferior Astronomy are incorporated in a certain MONAD which is derived from our Theories and which we send along with this little book.
[Dee is sending Gerardus Mercator his Monas symbol, presumably with a preliminary explanation, as Dee tells us his mind was "pregnant" with the Monas Hieroglyphica for 7 years, from 1557 to 1564.]
porisma (corollary)
Obscure, weak and (as it were) Hidden Virtues of things, when strengthened by the Catoptric art, can become more apparent to our senses.

The diligent Investigator of Secret has this great assistance available to him when examining the particular powers, not only of stars, but of other things that the stars affect with their perceivable rays.
53.

Anyone who wants to understand about the effect of the Sun's light on the Moon, or what the Moon can do on its own (not including the Rays of the sun), can learn by studying the full moon and the period of darkness during a total eclipse of the moon (and using the art of catoptrics).
(It is not necessary to point out how this same mode of experimentation can be used in solving other problems).
54.

The closer the radiant axis of a star is to being perpendicular to any elemental surface, the stronger it will impress its forces on that location. If affects that location with direct rays (because of the nearness of the star) but also by reflection (because reflected rays are closely joined with the direct rays).
[Shumaker suggests this last phrase refers to star rays that are reflected off the "shell" of the primum mobile and then rebounded to earth.]

Measuring the eccentricity of various places in the Zodiac can show us which planets are closest to us since they will make an acute angle of incidence with our True Horizon (or some other surface).

But we have spoken about this earlier. Now we will declare this general aphorism regarding equal distances from earth. Contemplating the reason for this exception in various places within eccentric circles is both useful and rewarding
55.

With any star above the horizon, the longer it Pauses, the easier it is for its direct rays to leave a strong impression of its power.
56.

O! The many different ways these 3 factors (Proximity, Angle of Incidence and Pause) can combine makes for a wide range of possible strengths of any given star (above the horizon).
57.

Any given momentary state of the heavens combines an infinite number of effects which direct and impress their forceful strength in the Seeds of events happening at that time. (These seeds will eventually ripen under the influence of other constellations.)

## 58.

Of all the heavenly motions, the swiftest is that which the circumference of the equator makes towards the west in the space of twenty-four equal hours. This is commonly called the Diurnal [Daily] movement of the Whole.

The closer parallel circles are to the equator, the closer their speed is to the speed of the equator.
60.

The ratio of the lengths of the circumferences of any two circles parallel to the equator is equivalent to the ratio of their velocities (as they proceed in the Daily motion of the Whole).

Apply this idea to other planets and fixed stars (with regard to their own daily arcs).

Furthermore, the ratio of these circumferences is also equivalent to the ratio of the Diameters of their Circles.
61.

We should observe and carefully note the periods of the celestial bodies as they move by the power of NATURE in accordance with inviolable laws.

By PERIOD we mean the complete return of a planet (or a fixed star or any celestial point), by circular motion, to the place where it started (or as close as possible). The time it takes to make such a Revolution we call a Period.
62.

From Nature we receive all these most important circles: the Horizon, the Meridian, the Equator (and all the circles parallel to it), the Ecliptic, the Eccentric orbits of the planets, the Epicycles, and others.

I recommend these be precisely learned from the theoretical and Astronomical Canons of the planets.
63.

Any circle might be considered what is commonly called a Circle of Position. Any circle is a circle of position of another particular place. (Actually every place has an infinite number of horizons or circles of position.)

Most places on earth have 3 main types of Circles of Position used in describing Celestial Themes [for drawing horoscopes]: its meridian [longitude line], horizontal circle [latitude] and a circle which cuts the length of the ecliptic at a right angle.

On the poles, there are only two of these three. [The latitude circle at the pole is a point]. And on the equator there are only two [the circle which cuts the ecliptic at a right angle is also the longitude line.]

Thus, there are an infinite number of ways Nature combines its forces.
64.

An equatorial period is the time it takes for some point of the equator, (or, actually, any celestial point), return to the same meridian. This daily motion of the Whole is completed in the space of twenty-four equal hours. As this period is always the same, it is the simplest of celestial periods.
65.

A natural day, or the diurnal period of the Sun, is the time that passes while the center of the Sun is brought back to the same meridian by the diurnal motion of the Whole. Indeed, this period is of very unequal duration.
66.

The time it takes for the Sun to return to the same point in the great ecliptic is called the tropical year of the sun. [in Greek, tropos means "a turn"]. In our age its length is observed to be 365 days, 5 hours, 55 minutes, and about 20 seconds. (However the most accurate observations of the best Mathematicians show that this length varies over time.)
67.

The time it takes for the Sun to return to the same fixed star (or the same distance from a fixed star along the length of the ecliptic) is called the sidereal year of the Sun. [in Latin, sidereus means "belonging to the stars"]

Thabit [Thabit ibn Qurra, Arab astronomer, 836-901 AD], the Son of Chora, found the sidereal year to be 365 natural days, 6 hours, 9 minutes and about 20 seconds. However, Copernicus has shown that in our age a sidereal year is longer by about 20 seconds.
68.

By making an accounting over a long period of time, determine the true length of the lunar period, both in relation to the longitude of the ecliptic and in relation to the Sun. These two kinds of periods are quite unequal.
69.

The diurnal period of the Moon, or a Lunar day, is the time it takes for the center of the Moon to return to the same meridian (by the daily motion of the Whole). This varies from day to day.

The length of time it takes for one of the planets to return to the same meridian is called a Day of Saturn, day of Jupiter, day of Mars, day of Venus or a day of Mercury.

In the space of a single day, there is very little difference between the extremely slow motion of the fixed stars and the daily period of the Equator.
70.

Just as you studied the periods of the Luminaries [the Sun and Moon], with regard to the ecliptic, we recommend you carefully measure the motions which are truly and naturally made by the other five planets (their eccentricity and their epicycles).

Try and distinguish (as best as you can) between their simple movements and their compound movements.
71.

In the same way we study the periodic conjunctions of the moon and the sun [eclipses], study how long it takes for a slower planet (through its true and proper motion) to return to another planet. (This must be done meticulously).
72.

The motion of the equator is the swiftest of all the celestial motions. Thus, of all the movements a planet makes, its daily period takes the least amount of time.
73.

Studious experimenters (lovers of sincere truth) have been able to discern and establish that celestial bodies are Imitated by inferior things in an orderly way, and in accordance with certain rules.

Every particular thing (or part of it) is affected primarily by one specific planet (or fixed star, or group of stars) which is called its Significator (to use the astrologer's term).

Any philosopher would agree that there are many ways that this Imitation manifests itself. It can be observed not only in Motion, Form and Figure, but in other properties and qualities as well.

## Inference 1

The assiduous Magus should explore the great Harmony not only between the Significant and the Imitator, but also in Analogous things in the Microcosm [in Man]. Two things united in similarity will also be harmonious with a Third thing.

## Inference 2

When any two of these have been identified, the third can be found. In the Anatomy of these Three-Celestial, Terrestrial and Microcosmic-a special quality found in one can be found in the other two.

For example, we suggest to you that by the Laws of Anatomical Magic you can see the connection between Sun, Gold, and the Heart of man.
74.

When the specific excellence of a Significator (a particular planet, fixed star, group of stars, or even a place in the sky) has been identified, it should be compared with the characteristics of other Significators (or other planets and fixed stars).

By skillful investigation, it can be understood how the performance of one Significator can either help or hinder the performance of another Significator.
75.

The spaces between the fixed stars have never changed in the whole eternity of time. Thus, there are things in the elementary world that have never changed.

However, all of the fixed stars are subject to an extremely slow Movement to the east, along the Ecliptic. [Precession of the Equinoxes]

As they are all driven by the same spirit, this means that likewise there are mutations and changes in our most important affairs (even though we consider them to be stable and consistent).

This slow revolution of the stars (by means of the Daily Motion of the Whole) makes a complete and unceasing celestial Harmony. This harmony which reverberates from all the fixed stars is kind of a First Form for everything.

All the fixed stars are harmoniously bound, not only to each other, but through their principal rays (and secondary rays), they are connected to each and every particle in the elemental realm. This is the way the Most beneficent and Wise Maker has ordained things to be. If this were not so, No Individual particle would (naturally) be preserved. Not even for a single day.
76.

This slow Motion of the Fixed stars means that over a long period of time, the same star will undergo growth, and even change. Thus, the effect of two stars or a small constellation of stars might (through their special power and their perceivable rays) also change.
77.

Sometimes a weak Agent will produce a stronger effect on a Subject than a stronger Agent. This may be caused by some natural tendency in the Subject or by some artificial rearrangement of the subject (or for some other reason).

This is best understood by those who have Paid their Respects to the Threshold of the Holy Art.

For that which has solemnly been Seven times Separated is ready to be Seven times Joined, to complete that most celebrated Gamaeam [marriage] of the philosophers.

I dare to assert (with God's approval) that this is the Seven Times of David, שׁׁבְעָ which has been expressed for us in the Dual Number.
[What I have translated as "Seven Times," Dee has written in these Hebrew letters: Shin, Bet, Ayin, Tav, Yod, Samech, which is essentially ShBATYS,

Dee's "Sabbatizat" in the
"Thus the World was Created" chart in the Monas.]
[In the margin, Dee has written the number 12 in Hebrew.]
78.

It is not surprising that certain stars which appear to be of the smallest size produce definite, perceivable effects in the air and other things. Even though they are very far away, these small stars are actually 18 times larger than the earth.

There are several reasons for this. It may be because they find an especially appropriate arrangement in the matter upon which they act. It may be because their rays are strengthened by another planet which bends the rays towards earth, invigorating them and making them more robust.

A star's energy might be amplified by something in its periexontos [surroundings] which causes the star to repeat its force every so often over a short period of time [creating an "echo" effect].

Moreover, what should we think about these fixed stars which are 30 times, or 70 times or 80 times larger than the whole terrestrial globe? And what (I ask you) should we think about the effect of those whose magnitudes are 107 times the size of the earth?

What are we to think of the divine power the earth receives at any given time from all the fixed stars of all sizes, distributed through the heavens in their most divine harmony?
[Dee is somewhat following the chart of magnitudes as determined by the Arab astronomer Al-fraganus (around 850 AD ). (magnitude 6 is 18 times earth), (magnitude 5 is 36 times earth), (magnitude 4 is 54 times earth), (magnitude 3 is 72 times earth), (magnitude 2, 90, (magnitude 1 is 107 times earth). Most of his numbers are from the 6 part division of 108.]
79.

If one equatorial period is subtracted from the time of a natural Day, and the remaining time is resolved into portions of the equator, it will be easily apparent how far the equator truly and naturally moves to the west using what are called Right Ascensions.

This is a true and specific demonstration of that most useful and admirable Astrological Praxis commonly called DIURNAL DIRECTION.
[This difference (or Daily Direction) is about 1 degree per day. This accounts for why the sun moves through all the signs of the zodiac over the course of a year (almost 360 degrees). Right Ascencion is the celestial equivalent of terrestrial longitude. Praxis means an "accepted practice or custom."]
80.

While observing this Diurnal Direction (the directional progress of the Equator on any given day when compared to the right ascensions of the Sun's position), also observe any other place in the entire celestial Machine.

Note carefully how much directional movement has been made above the meridian circle (or above the horizontal circle suited to that celestial point in the interval of time used to measure the forward movement of the Sun.)

Now we have established the right ascension and the oblique ascension of the Directional motion. [oblique ascension is the declination from the horizontal or the celestial equivalent of latitude.]
81.

Subtract the Equatorial period from a Lunar Day and it will become apparent how much all celestial places are (as we might say) pushed forward Directionally with respect to their right ascensions and oblique ascensions.
[Dee is saying that the Diurnal Direction of the Moon can be determined the same way the Diurnal Direction of the Sun is measured.]
82.

The Diurnal Horizontal Period of a planet or fixed star is the time it takes for their centers to return to the same horizontal circle (by the Diurnal Motion of the Whole).[This is the time period between one rising (of a planet or star) and the next rising (of that same planet or star.)]
83.

Subtract one period of the equator from the Horizontal period of the Sun or the Moon, and what remains is the portion of the equator which has advanced Directionally to the west (beyond one full revolution).
[This is a reiteration of Aphorism 79, only applying it to the Moon's period.]

## 84.

Even though the strengths of the Sun and the Moon are clear and relatively uncomplicated in this system of Directional movements, the five Remaining planets (as Significators) and the fixed stars should be observed using a similar method (by watching their daily returns to their meridian circles and the horizontal circles).

Remember, we are only considering the true movements of the stars. Beware of prescribinig a certain quantity (of degrees and minutes) to the individual Diurnal Directions of the planets, or their annual ones. (I will treat this elsewhere.)
[Dee recommends using observational calculations rather than using traditionally accepted estimates.]
85.

When their motions are retrograde, the daily period of any of the five planets is less than an equatorial period. Thus, it is essential that both the equator (and other individual movable places in the heavens) be pushed back to the east by these periods.

The Ancients called this surpassing of the equatorial period Reverse Direction. I need not remind you that this surpassing refers to the Horizontal circles as well as the Meridian circles. Nor that the equatorial period must be subtracted from any daily period [of a planet] moving retrograde. These things should be clear enough by themselves.
86.

When the daily period of Jupiter is compared to the equatorial period, a true and physical demonstration of a certain Direction results. The Ancients called this the ANNUAL PROGRESSION, in which they say celestial positions are moved towards the west by about a Dodecatemorium [one twelfth of a circle].

Nature urges you to observe either the parts of the Progression (compared to the true diurnal motion of Jupiter) or the whole annual Progression (compared to the true movement of Jupiter in one solar year).

If you do so, you will easily see that neither of these are always made in a straight line, nor is the number of degrees in the annual Progression the same from year to year (because of Jupiter's true annual movement with respect to the meridian circles and horizontal circles).

The movements of a planet (or a fixed star) cannot be determined by making only 5 readings, or even from 15 readings. Many, many readings must be made.
87.

Carefully examine how the DIRECT movement of a Planet causes it to Delay above the Horizon.

Discern why it makes this movement to include the Harmonic period of the equator in its own daily period.

Finally, learn why is it more likely to produce its particular effect on the Longitude of the Ecliptic.

Thus, it is not unreasonable to judge PLANETS progressing on a DIRECT course to be stronger and more endowed with good fortune.

Certainly those that move more SWIFTLY have greater strength and their significations are projected more fruitfully.

You can deduce from these Theorems what happens when a planet is both moving swiftly and is quite close to earth.
88.

A RETROGRADE Planet seems to somewhat break the constant rule of Nature by completing its daily period in a shorter time than the Equatorial period (which is our normal Time period, as it is the fastest and is always the same).

Second, by the general rule of Nature, the daily motion of all Celestial bodies ought to follow the Primium Mobile. But a Retrograde planet seems to snatch away some part of its function from the Primium Mobile by its own effort (as if taking control of the reins).

Third, it takes away a small part of that universal Harmony from each of its Daily Periods. After several days have passed, it will appear to have pushed back a sizeable portion of the Whole to the east. As it should be rotating perpetually to the west, this does a serious Injustice to the Equator.

Fifth, this obstinate planet seems to abandon its proper and special function, as the proper period for every planet should be completed toward the east.

Six, because of its delay above our horizon, it will be judged to have refused an opportunity to use its strength in a powerful way.

Thus, God did not wish that the Sun or the Moon (the most excellent of all corporeal creatures and the most benevolent to the elemental world) to be involved in these retrograde movements.

Nor does he allow other things to use such a tergiversation except for a very brief time (in comparison to their whole periods).
[Tergiversation means a turning back (from tergum "back" + vetere "to turn). Cicero loved this word and used it frequently. Though it's not used much today, it is still in English dictionaries.]

But truthfully, the performance of retrograde planets does no harm to UNIVERSAL NATURE. They do not corrupt the status of UNIVERSAL NATURE any more than an infinite number of other Antipathies. Indeed, they make Nature more pleasantly ornamented and contribute greatly to the preservation of Nature's wholeness.

During RETROGRADE MOVEMENT a particular effect which a planet performs is not promoted, but rather reversed. They seem to become the Undoer of Deeds. The planet seems to become an Undoer of the Deeds it normally does.

But who doesn't perceive that such things are sometimes necessary and often extremely useful in both Political and economic affairs. Isn't it better (as they say) to move backwards rather than advance poorly.

By interrupting the significant effect and becoming a contrary significant for a while, a retrograde planet is often quite helpful, even though it is by incidental assistance and not direct assistance.
89.

In matters of which they are Significators, planets near their Apogee [farthest distance from earth] exercise their powers more forcefully and more magnificently than they do when they are near Perigee [closest distance to earth].

However, in other matters they act with more vigor and effectiveness when they are nearest to Earth (rather than farthest from Earth).

This Aphorism is demonstrated most brightly and vigorously in Aphorisms 41, 43, 73, 77, and others explained previously.
[These particular aphorisms that discuss the size relationships between two spheres, the cone of rays; Anatomical Magic of Sun, Gold and Man's Heart; and the Gameaem or David's "Seven Times."]

Thus in order to make insightful and precise judgements about things signified by the various planets, their Apogees and Perigees must be known.

However, using the artfulness of Catoptrics you can easily make any of the five planets very distant from EARTH (even over the span of a few days). And finally (in the blink of an eye) you can lead it back to a new Perigee.

I recall reading that once men tried doing this with the Sun and the Moon, but seeing that ephruason ethnê... [the heathen became unruly...]
[Shumaker notes that this Greek phrase comes from Acts 4:25, which derives from Psalm 2:1 in the Greek Septuagint text of the Old Testament. Messing with the rays Sun and the Moon using mirrors might make the masses suspicious and fearful. (Shumaker and Heilbron, p. 234)]
90.

The power of the sun is not always the same [due to its eccentricity with the earth]. The calculation of its effect is not always the same. The effects and forces of the various planets differ. Thus the COMBUSTION of various planets is not always the same.
[In Astrology, a planet is said to be "combust" (or burnt up or destroyed) when it gets to within about 10 degrees from the body of the Sun.]

Even though the Sun has the most eminent and most powerful virtue, it does not always cause harm when it COMBUSTS (as the Astronomers say) another planet.

Indeed, by transferring some of its own strength, the Sun can even amplify the nature of a Combust planet to an even greater magnificence.

But when the Sun does damage the effect of a Combust planet, the degree of harm will vary.

The degree to which Combustion affects the operation of the perceivable rays of a planet can be determined using the rules of Graduation which we treated above in Aphorism 19.
[Dee explains the Art of Graduation more fully in his 1570 Preface to Euclid.]
91.

There is no spot on the terrestrial globe upon which the Sun, Saturn, Jupiter, Mars or any fixed planet does not shine with its direct and perceivable rays (during each of their daily periods).

The fact that the whole earth can be illuminated and warmed by all these direct and perceivable rays (and in such a short period of time) demonstrates that the earth is Truly privileged to be such a Excellent location.
92.

When two stars that are in locations which are ANTISCIIS, their declinations are the same, and distances around their true horizon are the same.
[In Greek, antiskios means "counter-shadows;" the shadows of two people on opposite sides of the earth will be cast in opposite directions.]

Because of the Daily Movement of the Whole, these stars make a mutual turning and will continue to surround and embrace some Terrestrial body. It's as if the care of that body had been entrusted to them.

Two stars working together in this fashion (whether relating in schematic or an aschematic interval) produce a certain effect. This effect can be found in the constitution of a known [Terrestrial] body which is exposed to them.
[Shumaker suggests that "schematic or aschematic" might mean "exact or approximate."]
93.

The part of any Celestial Circle parallel to the equator, which under the Meridian of some location (from all parts of that parallel), makes the greatest angle of incidence with the true horizon of that location.

However, only that part of the Ecliptic which is in the Nineteenth Degree from the horizon will always be elevated in the highest degree above the horizon.
[The Sun is exalted in the nineteenth degree of Aries.]
I realize that it is well known to anyone moderately versed in Astronomy that this nineteenth part is rarely found under the Meridian in an Oblique Sphere, but usually in a Right Sphere.

Thus, (in places whose Vertices are somewhere other than on the equator or on the poles of the World), that part of the Ecliptic found beneath the Meridian (at any given moment) has been called the Heart of the Sky. (The nineteenth part from the place of the ascendant is referred to as the Tenth House.)
94.

All stars are sharers of Light. So, (aside from the specific powers of their imperceivable rays), they are the efficient causes of a certain heat.
95.

The Sun, (the largest of all celestial bodies) is not only the perpetual, immense source of celestial Light for us, but also the main producer of perceivable heat, which is so vital to our existence.
96.

The greatest Heat of the sun will be at the point over which the Sun hangs perpendicularly at the time of its Perigee [closest to earth].

The Heat from the entire Base of the Sun's radiant Cone affects that natural point on the earth's Surface which is at the vertex of that radiant cone.

We generally assume (for the sake of illustrating our Doctrine) that it has a power of Sixty degrees, or One Hundred degrees.
[Dee appears to be saying the Sun is so hot it would be way off the scale of his Art of Graduation which only goes to four "degrees" of heat.]
97.

Besides determining this maximal degree heat at Perigee, we should learn how much heat the SUN directs to various points on the earth's globe (over which it hangs perpendicularly) during the rest of its annual Circuit.
98.

When the sun hangs perpendicular above you, note the amount of heat it makes in some suitable material.

Then you will understand (by experience, not proportional calculation) how much heat it will direct to any other terrestrial point over which it hangs.
99.

Suppose you had two different degrees of heat (in a particular proportion) in two different terrestrial locations that are perpendicularly beneath the two different places of the Sun's Circuit.

Also suppose (at any time when the Sun is shining for us) we devised some kind of artifice that could produce a perceivable heat equal to the heat found in one of those places.

It would be possible, through our Artifice and industry, (at any given moment, provided the Sun is Shining) to produce perceivable heat that would be exactly equal to the other location on earth.

However, this is not the place to explain at how great a distance.
[Dee emphasizes that the Sun must be shining. So he may be referring to some Catoptric heat-multiplying device, perhaps involving concave mirrors.]

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100 .
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Using these same Rules, most accurately examine how much less heat producing power the Planets have compared to the Sun, (as a result of the size of their Conical bases with respect to some terrestrial point, above which the planet hangs perpendicularly, when the planet is at its smallest distance form earth.)

You can calculate the amount of Heat a planet produces by comparing its base and distance with the base and distance of the Sun.

But always keep THIS in mind: Each and every planet (because of its own particular body) mixes another perceivable quality with the general power of its heat. And what sort that is (not only in the planets but also in the fixed stars) you can learn by studying the Moon (refer to the test described in Aphorism 53) and also by other ways.
[In Theorem 53 he recommends using a mirror to somehow calculate the power of the light generated by the Moon itself during a Solar eclipse. Dee's apparently believes that planets generate heat and light. But this is not actually the case. Also as the planets and stars are so vastly far away, his geometry of finding conical distances is a bit unusual. That the "other perceivable quality" Dee refers to here might be moisture (or humidity), the other axis of Dee's Art of Graduation.]
101.

We can apply the rules we used for the Sun to determine the various amount of the Moon's heat (over any particular terrestrial point over which it hangs perpendicularly).

But obviously we must take into consideration the moon's distance from earth at any given time and also how much of the Moon's convex surface facing earth is illuminated (that is, what proportion of the conical base is illuminated).

Let the Careful and diligent Astrologer the consider why Lunar rays don't assist each other very well much the Moon is Horned, compared to when it is nearly full. In all these Aphorisms I leave many things to judgement.
102.

The most special properties of celestial bodies are LIGHT and MOVEMENT. Among the planets, the SUN surpasses all others in LIGHT. The MOON supercedes all the planets in the swiftness of its MOVEMENT. Thus, these two are rightly considered to be the most excellent of all the planets.
103.

The MOON is the most powerful directress of moisture. She is both the producer and cause of humidity.
104.

The SUN, with its excellent LIGHT, is the special director of vital heat. And, by a certain wonderful analogy, the MOON, with its swift MOVEMENT, is the special directress of moisture.
105.

The closer the MOON is to the earth, the swifter it moves, and the more it exercises its own powerful dominion over humid things.
106.

From these things it becomes apparent that the SUN and MOON are (after God) the truly special physical causes of the procreation and preservation of all things born and that live in the elemental world.

Through Heat and Humidity "all things are measured and increased" (if I may use the words of our philosopher). For only these two things are "procreative."
[Dee writes "all things are measured and increased" in Greek (panta sugkrinetai kai auxetai) so he's probably referring to Plato or Aristotle. For "procreative" he uses the Greek word gonima.]
107.

By a certain analogy, the general arrangement of a whole year can be seen in a single day.

For any natural Day has its own Spring, then Summer, then Fall and then Winter.
From the heat of only the Sun (partly through itself and partially by chance) all the primary qualities can be produced, and in the correct order.

If we distinguish a beginning, a middle, and an end in each of these we will perceive the foundation of the Duodenary. [4 (seasons), times 3 (moments) of each, equals Twelveness]

And it is glorious to consider how, under the poles of the World, a Year resembles nothing more than one single natural Day.

To you who investigate the physical mysteries in the unity of The Trinity and to you who gasp painfully, surrounded by your Work in the Blackness of the multicolored Night, apply this Aphorism to higher matters and the greatest Secret will be revealed.
108.

In the eighth book of his great composition [The Almagest], Ptolemy describes 26 different relationships that can exist between the fixed stars and the Sun (which itself has four angular positions).

Transfer these relations to the other planets (and especially to the Moon).
Compared this way, there will be a total of 182 different relationships between the planets and the fixed stars.
[7 planets, times 26 relationships with the fixed stars, makes 182 total relationships]
109.

An imperfection of the Body, not the Soul, is the nearest and most personal cause of physical Death. Thus, nature is the cause of natural death.

Death is dependent upon (and is marked out beforehand) by the general Governors of Nature. In the Human race, certainly, Nobody can live beyond the time Limit predetermined for him by God. However, through their own negligence, very few are even able to reach that Limit. Thus, it appears there are two different Limits for human life.
110.

The human Soul and the specific Form of each and every thing have far more excellent virtues (and provide more services) than either the Body or the Matter from which it is made.
111.

The imperceivable (or unintelligible) rays of the planets are to the perceivable rays as the Soul (of something) is to its Body.
112.

Some stars have been called EVIL, but stars themselves do nothing evil. They have simply poured their strengths either into things of a corrupt Nature or Matter which is badly disposed in the first place. (Refer back to Aphorism Seven.)
[Aphorism 7 reads: Rays pouring from one thing affect various things in different ways.]
113.

There are two reasons for the natural diversity found in all the things that exist in the elemental world. First, there are various kinds of Matter. Second, different stellar rays affect Matter in different ways.
114.

Everything that exists in the elemental world, no matter how miniscule, is an Effect, or a particular Example, or an Image of the whole of celestial Harmony. Its just more clearlt apparent in some things more than others.

## 115.

Thus there is an ANALOGY between celestial bodies (either alone or working together) and bodies in the realm of the Elements.

If you are carefully and constantly looking for these similarities (by using the art which has been described above), you will follow the wide pathway towards complete understanding of Astrology.
116.

The Seven planets are able to exhibit 120 different Conjunctions:
There are 21 possible conjunctiions between any 2 of the 7 planets. There are 35 possible conjunctiions between any 3 of the 7 planets. There are 35 possible conjunctiions between any 4 of the 7 planets. There are 21 possible conjunctiions between any 5 of the 7 planets. There are 7 possible conjunctiions between any 6 of the 7 planets.
There is 1 possible conjunctiions between all 7 of the 7 planets.
The total is 120 possible conjunctions.
The greatest philosopher tells us, most truthfully:

## "In these lies the knowledge of things created in the world: of their origin and of their destruction."

To further investigate these 120 different Conjunctions,we recommend the following Procedure. For conjunctions of 2 of the 7 planets:

There are 21 possible conjunctions when 2 of the seven planets are joined
Next consider that one of these 2 planets involved is stronger than the other. Now there are 42 possible conjunctions.
[ 21 or $1 \times 2=2$; and $2 \times 21=42$ ]
In the same way, when 3 planets are joined there are 210 possible conjunctions.
[3! or $1 \times 2 \times 3=6 ; 6 \times 35=210$ ]
When 4 planets are joined there are 840 possible conjunctions.
[4! or $1 \times 2 \times 3 \times 4=24 ; 24 \times 35=840$
When 5 planets are joined there are 2520 possible conjunctions.
[5! Or $1 \times 2 \times 3 \times 4 \times 5=120 ; 120 \times 21=2520$ ]
With 6 planets there are 5040 possible conjunctions.
[6! or $1 \times 2 \times 3 \times 4 \times 5 \times 6=720 ; 720 \times 7=5040]$
With 7 planets, there are also 5040 possible conjunctions.

$$
\text { [7! or } 1 \times 2 \times 3 \times 4 \times 5 \times 6 \times 7=5040 ; 5040 \times 1=5040]
$$

The sum total of all these different kinds of Conjunctions is $13,692$.
Remember, all these possible Conjunctions are based upon the premise thatthe strengths of the planets are unequal.
(If we took into consideration that there were different degrees of inequality, almost innumerable myriads of different permutations could be found.)

| conjunctions involving planets of unequal strengths (as per Aphorism 116)$\qquad$ |  |  |  | conjunctions involving planets of equal strength (as per Aphorism 117) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1 | 0 | 0 | 0 | 7 | 5040 |
| 2 | 2 | 21 | 42 | 2 | 6 | 15120 |
| 3 | 6 | 35 | 210 | 3 | 5 | 4200 |
| 4 | 24 | 35 | 840 | 4 | 4 | 840 |
| 5 | 120 | 21 | 2520 | 5 | 3 | 120 |
| 6 | 720 | 7 | 5040 | 6 | 2 | 14 |
| 7 | 5040 | 1 | 5040 | 7 | 0 | 1 |
|  |  |  | 13692 |  |  | 25335 |
| $\begin{gathered} \text { number } \\ \text { onver } \\ \text { inver } \\ \text { con } \end{gathered}$ | $\begin{gathered} \text { how } \\ \text { hany } \\ \text { marnur } \\ \text { tations } \\ \text { pors } \\ \text { posible } \end{gathered}$ |  | $\begin{aligned} & \text { column } 2 \\ & \text { times } \\ & \text { colunm } 3 \end{aligned}$ |  | $\begin{aligned} & \text { inequality } \\ & \text { produced } \\ & \text { from } \\ & \text { equality } \\ & \text { (generally } \\ & 8 \text { minus } \\ & \text { column } 5 \text { ) } \end{aligned}$ | column 6 factorizized then times column 3 (except firstentry) |

117. 

Using the same procedures, let's look even more deeply into the virtues of Nature. We assert with most certainty that the rays of the seven planets (the principal perceivable rays, subsidiary incidental rays, and rays of a more secret influence) converge and mingle with each and every thing in the world, at all times.

And this perpetual conjunction of all these planets remains in each and every thing in the World (not only because of the natural effects of the planets, but also because of their actual positions in the heavens).

Thus, if the powers of the planets were unequal, Nature is able to control their workings in 5040 different ways. [ $1 \times 2 \times 3 \times 4 \times 5 \times 6 \times 7=5040$ ]

Next, consider that sometimes 2 of the planets have equal degrees of power (or sometimes 3 , sometimes 4 , sometimes 5 , sometimes 6 , or sometimes, but very rarely all 7)

We would find there are 20,295 possible relationships. (These equalities might be found in the highest degree, the lowest degree, or even in some intermediate degree). If we add to that the 5040 kinds of absolute inequality, the result would be 25,335 possible relationships (indeed, very general ones).

It is most worthwhile for the philosopher to apply the rules of Graduation to these results for it will lead to great pleasure and immeasurable usefulness.

So you can more easily understand the truth and arithmetical Logic of these two Aphorisms [116 and 117], we have included a chart of our calculations (which is also very useful for other purposes).

The industrious artificer will be able to extend this Procedure almost infinitely, not simply stopping with the number Seven.

The computations in the second part of that chart are difficult to see.
So to help students, we offer this example (and explanation):
If only 2 planets (out of the 7) have equal strength, six general distinctions will be found among all the strengths. (This can be seen in the fifth and sixth columns).

But according to the third column,
a binary conjunction among the 7 planets can happen in 21 different ways. And in the second column,
the unequal strengths of 6 planets are able to be considered in 720 different ways.
Multiply 720 times 21 and you get 15120 ,
(the number you will find in the second place down in the last column).
Apply this same method of computation
when $3,4,5$, or 6 are furnished with equal strength.
Finally, to more fully explain this matter, here is a very brief chart of the work.

118.

Within the Revolution of a Solar year, look for the beginning or some other noteworthy moment in the period of a planet.

Or, at any time, look for some strong and unusual configuration of planets (or of the planets and special fixed stars). Or any other unusual Astronomical event.

Then Look Around the whole world astronomically and determine what terrestrial place is (or might be) affected by the first Appearance of such a powerful and special configuration in the heavens.

There are two ways this remarkable and secret procedure works.
You can understand how the nature of the stars and other Sublime celestial things will influence the events at a particular Place on earth. Or by studying the outstanding events of a particular Place on earth, you can better understand the special nature of the planets, fixed stars, and other Sublime celestial bodies.

Thus a Wise Man (if he is a Cosmopolite) [a Citizen of the World] can draw upon this most noble Science (for himself or for others) to procure favorable things or, contrarily, to remove noxious things. Thus, the Opportunity [favorability] of various terrestrial places is of great importance.

This is all similar to the tale from long ago of the Wise Men who,
having looked around the heavens, declared:
"WE HAVE SEEN HIS STAR IN THE EAST."
119.

As Thrice-Great Hermes has taught us:
Xoris tês kosmikês sumpateias, tois anthropois ouden epiginetai.
Nothing happens to men without cosmic sympathy.
120.

Ikana ta THEIA, kai ê touton Periphora, tên en to kosmo ton phusikos ginomenon, Sunexeian phulassein.
Certain befitting divine things and their circular motions are enough to preserve the continuance of everything that is physically born in the cosmos.

HONOR AND GLORY TO GOD ALONE

Monas Hieroglyphica



pramitatio ad kegem
ne vits Duplex, inque diucrfasfententius, Curfus (quorum alterum ingrediuntur Plerique omnes) iftac confiderandus ratione. Quam primum, Infantia confecto curriculo, Pueritieque: $\operatorname{Adolef}$ centum iam, 2 uod vita deinceps ingredientur genus; Animum torquere incipiat Optio: Tunc, in ancipitisfudicy aliquantulum bafitantes, Biuio:Statuunt tandem: Vel, (Veritatis Hï̆ quidem \&o virtutis Capti Amore) ad Philofophandum, toto reliquo pita/patio, neruos contendendos omnes : Vel, (Illi certe, Mundans irretiti Illecebris: aut Dinitiarum flagrantes Cupiditate) delicatä Queftuofámue nitam ducere, modis follicite Laborandum omnibus. \&t Iforum, Mille, profectoo, I. velfacillimè inuenias: Vbi fllorum ( fincerius (cilicet qui Pbilo oppbic operam nauant) vix V num monstrare queas: 2ui ipfa Pbyjice, [altem prima Veráque, deguftarit funda: menta. At, 2 иi Calefium virium \& Actionu:: Rerum 2. sliarrü Ortus, Status, Obitusq́ue, fuerit penitius pleniusq́, perfcrutatus Cauffas:ne corum quidem, qui §e totos ad Sao $^{\text {a }}$ pientic fudia convertére, Mille fimum, in medium adferre, Reff. Literaria poteft. Quid erge, Qui, istis difficul 3 tatious uperatis omnibus, ad Supercalefitum Virtutum, Metaphyficarumque Influentiarü̆ Speculationé ©v Coms prebenfonem Aspirarit, V BI H VNC, in toto Terrarums Orbe (nostris iftis deploratiffimis Temporibus) MMagna:nimum, vel VNVM, effe, ßerabimus H ERO A? Cum ius xta prioris noftra(baudtemerè recepta) M IL LESIME Praportionis Progreffum: Ex CEN TVM SINCERE

PHILO-

## INCIYTL REGIS

MAXIMILIANI
excellentissime maiestati,

## Ioannis Des, Londinensis,

 Imperiums optat Falicifimum,触
 v e due caufa, mea Conditionis Hominem, REGEM tantum, tam exiguo donare $M u-$ nere, animare poßunt, be ambe, nunc, me ad hoc fuciendum impulére: Beneuolentia nimirum erga vestram Maiestate é mea maxima: Et Mus neris ipfius, licet parui, tum Raritas magna, tum Bonitas baud appernanda.Beneuolentiam vobis excitauére et conciliauére fempiternam, Vestre admirande Virtutes: शue tante funt, $v_{t}$, qui illas oculatt non perfexerint fide, alijs quide, vel mediocriter credant, Rariffima, de eijdem, licet veriffima, narrantibus. Sed qui eafdem diligenter atcuratius $q_{;}$funt Contemplati Prafentes: Orationis. $\int e$, Diifionisque maxima laboraturos Inopia acpaupertate fatebuntur;quam primùm Oratoriè in earüdem omnem fe dif: fundere cupiant Amplitudinem. Husiufe rei cautios, Ego, proximè iam praterito Septébri, in Hungarici veftri Regmi 'Pofonio, aliquam trabensmoram, luculentiffimas, eas'que varïs sexploratas modis, aculatus cognosit Testis.

De NHuncris autem (mole quidem ipfa exigni) quod diceremR Raritate; Derbis, quam fieri pofsts; pduciffims; shibi, Mentisi adaganti conamine toto, Occurrit Huma

$$
\text { A } 2 \text { nerite }
$$

MAXIMILIANVM.
PHILOSOPHANTIVM MYRIADIBVS: ATEX PROMISCVE HOMINYM SORTIS, CENTVM* myriadvm millibvs, Hvnc Vnicvm FOELICISSIMVM FOETVM EXSPECTARE DEBEMVS. Cuius fic demonftrate R ARITATIS, HIEROGLYP HICVM Typum, ad Pythagoricam (diEtam) appingemus literam. Vbi, peftre Excellentice attentius intuenti, maiora $e \int e($ (onfideranda) offerre videbun. tur, Myjteria: ex noftris boc modo defcripta Cosm OPOLITICIS Theorüs.


Fn quonunc Triplicis iftius (Pbiloopbica) explicate Raritatis Gradu(Clementiffime R Ex) Optarem quidem boc meum E $\int f$ e, Cenferiq́que Munus:Vel Ippe, qui eArtium Maximaru, Rerum ${ }_{q}$ Secretifimarri cognitione Excellis \&o $A_{3} \quad$ Abuedas

> PRAEFATIO AD REGEM
> Aburdus, fucili poffis afsequi coniectura. At infufimos I. promoque Pbilofophandi genere, fatuere : non id àme arroganter efe factum exifizo. Et fiab bumo, altius interdum videatur Caput leuare velle: Ex eodem ergo on BoN I t A I Is Gradu, fructus vberes, de isto meo Sperandos Munere, Vestra Celfitudini polliceri, audeo. Et, hac 2. quoque Raritate praditum est, boc nostrü Munus, Quod eogenere Scribendi, $\downarrow$ §que ad extremum Orationis filum, contextum est, quo, nunquam, ad bodiernum $v \int q u e ~ d i e m$, aliquod fuiße abJolutum Opus, vel auditione accipere potui, vel ex Msiorum intelIgere ©Monumentis.

> Hieroglyphicum etiam licet appellem, fubeßetamen or 3. . Lumen © Robur quafi Matbematicum, Quipenitius ex. aminarit, fatebitur: Quod in tam Raris factitare rebus, fatiseße Rarum liquet. eAn non boc Rarum, quafo, 4: eAfronomicos Vulgares Planetarunn Characteres, (ex eivortuis, aut Mutis,aut faltem quafi Barbaris ad banc borà Notis; )Lam, Vitaimbui Immortali: © in omni Lingut © Nuttione, proprias fuas Eloquentifimè explicare p®ßevires? (ui etzĭ accedit © © istud valac Rarum: Ex- 5 : ternsecrundè Ccrpora, ad myfficas iam fucs (optimis Argumètis Hieroglypbicis) eße reuocata,reffitutáue Symmetrias. Quı 2 i, vel eedem fuißent olim, apud Seclum prius: vel tales fore nosfri Optaßent Maiores. Fin Ecliptica 6 . Dodecatermoriorumn Notis, quàm ñoud fofliciq ${ }_{j}$ idem prea. fare tentauerimus fuccef $\int u, *$ id videre, vt eft Rärum, itaNosuiop prorfus. Et bec ennia inVnicojeóque MeR-7.

> CVRII

## prameatio ad regem

Su. 1 ș7. mum: Apologeticè, olim differuimus. Sed tanta de büs mitas respraic. conftant Myjferia, qua jolidiflima babent (tum ifius Artis
 $\mathfrak{c c c}$
 plicare magno queam; nec Locus ife, iam, requirere vide. tur. Néq, ${ }_{\text {j }}$ mireris, 0 Romanorum Rex Inclyte; $\mathcal{M e}$, Alpbabetariam Literaturam, magna cötinerc Myfteria, nunt obiter referre: (um IP S E, qui omnium Myferiorum Atw thor eff S OLVS, ad Primam ©f Vltimam, S EIP S VM Comparauit Literam. (2uodnon in Graca Jolum effe in. telligendum Lingua: fed tum in Hebrea, tum in Latina, varijs, ex Arte ifta, demonftraripoteft vüs.) O, Quanta, túm, debeant effe, Intermediarum ©Myftria? Et non ef mirum, boc, in literis fic conffare:Cum \& Vifibilia \& I N v IS IB I L IA omnia:Manifefta, or Occultifima(NaturavelArte) abipfo Deo emanantia, ad eius B ON I TAtem, Sapientiam or Potentiam, predi candam, celebrandamq́ú; ;à nobis, diligentiffima Indagint funt perluffranda. Inde, excufatione omni carere, $\mathrm{H} v-$ Md Rem, MANVM GENV $s$, docebat Paulus: Etiam $f i$, nusllum ex Creatione, ipfo Digito $\mathrm{DeI}_{\mathrm{E}}$, in omnibuseftexaratum Creaturis. eAt, boc nunc non ago, Curiofius, $v t$ ifa ab omnibusrequirere velim Grammaticis:Sed Ipfos, 2 ui ${ }^{\text {R Rerum abdita eruëre } \mathcal{M} \text { Myfteria Laborant:cum, Testesfa }}$ erre, nos, RAR VM quoddam in hoc Gevere, (ex nostra Monar

MAXIMIEIANVM.
CVRII, Cbaractere Hieroglypbico (eAcumine quodun premunito) includi, esf omnino Rariffinum. Verè ergo, Ille, nobis totius Afronomie Refitutor or Infaurator no. minari poteft: Et nofri I E O V $\begin{aligned} & \text { in } \\ & \text { in } \\ & \text { bocgenere Nuncius, }\end{aligned}$ $\nu t$ Sacram banc Scriptionis eArtem, vel Novam Conderemus Primi : vel extinctam prorfus, Cơ ex omni hominum BMemoria deletam, eius Reuocaremus Monitis. Fdque, à nobis, hoc eff factum modo, vt placidißimè, er quafi fuafponte, Hieroglyphica illa fnterpretationes Omnes, fefe in medio ponant: Violentum nil, vel Improprium quafi per totum videri Opufculum potest.
8. Et bac, Ita, Londinensi nostro Hermetis Sigillo (ad fempiternam Hominum memoriam) (onfognari; $\mathrm{V}_{t}$, in eodem,ne Superfluum Punctum $\mathrm{Vnum}_{;}$ (4) ad bec que diximus fignificanda, (longéque maiora) ne vnum deficiat Punctum ${ }_{5}$ Omnes cogentur, maximè fateri Rarum. At pre ceteris, Illi, qui in Pbilofopbie Sapientisq́queprofundioribus Difquifitionibus, Noo men poffunt profiteri fuum. Sic enim Tefificabuntur i. Grammatici: dum rationeseffe reddendas, de Literarum formis, Situ, Locis in Ordine Alpbabetario, Nexibus varї̈s, Valore Numerali, alïs sque plurimis (que circa Triums Linguarüs Alphabeta Primaria cöfiderari debent) bic admoneri fe videbunt. Vt \& aliàs, tam Rarum effe Grammaticum, Q vi Grammatică, V n a m effe Scientiam,ab V o o difcendam Homine, exacte defendere pofft: 2uamm FIlum; quem Supra in Terris demonftrauimus Ruriffmum:

MAXIMILIANVM.
5
MONADE;) demonfraffe Exemplum: tum, Amicè admonere; Primas, Mysticasq́que,Hebraorü, Gracorum, ©ண Latinorum literas: à Deo folo profectas, © EMortalibus Traditas: ( 2uicquid bumana iactare folet eArrogantia) Earumque omnium Figuras, ex Punctis, Rectis Lineis © Circulorum peripherüs, ( mirabili, Sapientif/moque dispofitis Artificio) prodiffe. Et, licet,omnem Mifoaice Legis fenfum, B/que ad fodim ©C- Apicum fmpletionem omnium, confiderandum effe, nos docuit aternat Calestis samb.cs. noftri Patris Sapientia: quafion IOD or Cbireck ( $\mathrm{ex}{ }^{\text {s. }}$ quibus omnes Hebreorü Litera, Vocales $\not$ que confurgunt) pltima Cofiderationis Legalis, facta Analy fi: Nobis tamen nonest id Contrarium, VNitate apicis CHIreck,immotamanente: Trinitatem MONADVM CONSVBSTANTIALIVM, IN Vnitate ipsivs IOD, conspic̣vam, Amplecifentibus: Ex Recta descendente einea Vna, et diversis peripherie partibve Dvabvs, Conformatam. Unde fatis enucleatè, eodem labore detegimus: Primos Homines, tam Stupendam Hebraicarum Literarum \&大 Nekudoth Fabricam, ex tam Mysticis condere Principïs, fine Prafentißimo Diuini Numinis Afflatu, noेPotuiffe. Que, etiamfi, Minima eorum funt, que vulgarium Grammatio corum ponderentur-Iudicüs: Dum tamen,quo fefè ad omnem Literarum or Nekudotb Generationem, or quatm mir_bili accommodent eArtificio, aptè à Sapientibsse confio B derantur,
fiderantur, Maxima, perpluraq́ue ( abolutißima e Ana. gogia ) illosedocent $\mathscr{M}$ Myzteriat. Sed dimißis, boc modo, Literarum iffis, \& Lingue Pbiljoppbis; Mathematicos meos, Raxritatisifius noffrie ©Runeris, ad 2. ducam fincrifiSimos Teffes. Arithmeticys, (non dico, Logis TA) an non mirabitur, Numeros/wos,quos ${ }_{4}$ à rebus Corporatis Abfrrailos, ©CO fenflibilibus omnibus Liberos, in Dianais recondebat receßßibus; ;bique, Mentis varijustractabat Actionibus: Eofdem, bic, in noftro Opere, tanquam (oncretos \& Corporeos ostendi, feríque: (4) eos rundem Animas, Formaleśque vitas, ab eis, in nostros $f$ ecerni $\downarrow$ fus? An non maximè mirabitur, Tantum ridere ${ }_{2}$ Monadis Fatum:cuinec vlla Monas Alia, vel $\mathcal{T}$ (umerus, additione accedit : Jec extrinjecé ad ipfam MuL tiplicandam adbiberi poteft? An non admirationeaffi-; cietur maximan in Rei E'Cerfurs Subtilifima Generalíque Regula: Vnivs rei, tanquam Chaos, propofite, (ad omne diffoluendum Aritbmeticü Dubium, babilis) C E NSVM ip/um, © Valorem, fiue Estimationem (Potentia in ìf/a Re Latertis) H H $\hat{u}$, Primofemper Examine, DENARIO explicari Numero? Accuratis Diuifonis ©f E- $_{-}$ quationsं operibus (vel vt illa Ar spraforibit) mediàtibus 3. Prius? Geometra (mi Rex) fibide Artisf fuevix fuť̇s plenè côfare Principùs (quod valde mirü eff)incipiet befitare: cumm,biu, in Secreto, murmuirari, fnnuiq̆que intel. Lget: Qfadrato, Circvlare,omino equahi, huius MONADIS Hieroglyphica Mysterio dari. Archime-

## praEfatio ad regem

8. Haud fecus, وui Rationes P L E NI © V AC VI (argin, mentum rofque ab ipfis Pbilofophis Incunabulis controuerfum) diligentißime ventilarunt: Videruntq́que, ea Le. ge, 心 Natura(quaff Fndifolubili) vinculo, (à Deo Opt. Max.) coördinatas, cönexas, © Copulatas Elementorium proximorum effe Superfcies: Vt in Igne, Aëre © eAqua, furfum deorfum, Horfum illorfum, (ex eorum animif ententit) ducendes impellendifuc; bominibus SMiranda confidentifimè ofendere poffint (Varÿs ©foilli quiden fn. uentis Reip.funt votiles: Vt Hydraulicorum totum efrtiffium monstrat, © \& reliqua Heronis Thaumopceticis „vt nunc placet illa nominare.) eAt, quod Terre Elemen,s tum, Surfum, in Fgnem, per e Aquam, oulla Machina ex, antlare poßit: J ©ullus exilla Profefione, fibi vendicabit. „Noftret tamen MO N A DIS Theorice, feriid $p o f f e$, demorn ftrant. O SapientiSisine Rex, IFta in Mentis veftre, Memorisque reponatis Thefauris Secretißimis. Ad CA9. BALIS T AM iam venio Hebraum: $2 v i$, , pbifuă ( $(f i c d i m$ Clam) Gemetriam, Notariacon, \&T Tzruph (Artis fue tres quafiprecipuas Claues) extra Sancte, J(uncupate, Lingue exerceri fines videbit: Immò ondiquaque (ex obmïs quibusque, viffbilibus \&o Inuijbilibus) buius, ( Deo) ReceptaTraditionis SMyficce Notas, Characterefq́ue corrogari, Vel, hanc quoque Artem, tum, vocabit SANCTAM: ( veritate coacturs fifntelligat) Vel, non $\mathcal{F}^{\prime}$ udrorum, tantum, ${ }_{3}$ Sedomnium Gentium, Nationum © ©
 neuolentifs.

MAXIMILTANVM.
Arcbimediśque dictos S V DO R E S, bic, excellentifímocös penfari poffe Fructu: licet tentatum baud fuerit ipfe affecutus Problema. In SMagnis Voluife Sat est. Mvsi C v's, quo ftupore flle poßit iure affici meritißimo:cùm 4 fine ©Notu \&o Sono, frexplicabiles, Celefesq́quebic Intel liget Harmonias? Et Astronomvsaznons. perpeßfifub Dio Algorsis, vigiliarum \&\% laborum panitebit fe maximè Cwn, bic, ine Aëris olll perferédd Iniuria: Sub tecto, Cluufis vndiq́; feneffris Ofiijsque, ad quodcunque datum Tempus, Celeffium Carporum Periphoras, ocuLis exactifBimè queat obffruare? Et boc quidem, fine ENTechanicis allis , ex Ligno velOrichalco confectis Infrumentis? Et Perspectivvs, fui Ingenij Stupidita- 6. tem condemnabit: Qui, ,vt iurta Parabolice Cani Settionis Lineam (aptè ing yrum circumactiam) Speculum efficeret, modis lajorarit omnibus:quò propofitam quamcunque(igni obnoxiam) Materiam, incredibiliex Radijs SoLaribus vexaret Calore: Cün, bic, exTetrabedri Sectione Trigonica, Linea exhibeatur, ex cuius Forma Circulata, feri poteff Speculum; ${ }^{\text {Quod }}$, (vel Nubibus Soli fubduEfī) quof (unque Lapides, Vel Metallü quodcüque in fom palpabiles quafi, vi Catoris (verijfime maxima) redigere potest Pulueres. Et,qui Pond ERVM fubtili Spe- 7 . culationi toto vita Tempore infudarit : Quàm bene, fwos ille collocatose effe Laborere, fumptusqué iudicabit: Cư, bict, Elementiun Terrájupra Aquam natarepoffe, certißisime Experientia, M ONADIS noftra docebit OMagiferinm? B 2 Haud

MAXIMILIANVM.
7
neuolentißimum fatebitur : Nullumq́qu Mortalem $\int_{e}$ Excufare pofle, de Sancta huius nostre Lingus Imperitis. Quam, in noftris ad Parifienfes Apborifmis, R E A L E M nominaui CA B A L A M, fue T今̃ örтos: Vt illam vulgarem alteram; Cabalisticam nomino GRAMM A TI C A M fiue İ̃ $\lambda$ eqoúsr; qua, notißimis Literis, ab Homine Scriptibili, bus,infffit. Hac autë, que (reationis nobis est Nata Lege,( $D t$ Paulus innuit) R E A LIs CABALA, GRAMMATIC A quoque quadam Diuinior eft: cum Artium ista fit Inuentrix Nouarum, er eAbftruffimarum fidelifima Explicatrix : Vt boc noftro alij tentare Exemplo, de ceterò, poßint. Non exborrefces, bene fio, (O RE x) Licetiam, in vestra Regia Prafentia, MAGICAM banc 10. proponere audeam Parabolam. Terrestrequoddam Corpus, M ON As bacnostra Hieroglyphica, in Centro Centri, Latens, poßidet: Quod, Qua fit ACTV A N DV M diuina Potëtia, gine Verbis, Ip fa docet: Cui iam A C Tv vTO, Lunaris (t) Solaris eft (slatrimonio perpetwo) Cop vin nd a, Influentia Gonetica: Licet, ante,in Cew lo vel alibi, fuéreab E ODEM Corpore SEPARATISSIM E. Hac (Dei Nutu) facta Gamaaa, (2uam, Pari
 monï Terram: fue Influentialis (oniugij,Terreftre Signü) Superfuam Nativam Terram, Eadem, plterius Nutriri non poteft, vel Irrigari, quàm ad Q v A R T A м magyim veréque sMetapbyficam Reuolutionem Completam. 2uo finito Progreßu: Qui aluit, in MeT A MORAHOS 1 M , B 3 Primu

PRAEFATIO AD REGEM
Primus fppe abibit: Rarißiméque, pòst, Mortalium con-乃icictur oculis. Hec, 0 Rex Optime, Vera est, toties decartata ( $\mathcal{\circ}$ fine Scelere) MA G O R VM IN VIS I BIlITAS: Que( $D 5$ Posteriomnes fatebuntur Magi) nofreeft MONADIS conceffaTheorijs. Expertifimus
II. Medic vs, etiam ex eifdem, facillimè Hippocratis My, ficam affequetur voluntatem. Sciet enim, Q VI D, C VI, vifore ADDENDVMET AVFERENDVM $\int i t: \nu t$, ipfam Artem fub maximo M O N A D IS noftra Compendio, $\sigma^{\circ}$ Medicinam ipfam contineri, Lubens deinde futeri 12. Teelit. Beryllis tic vs,bîc,in Lamina Chryftala lina, omnia qua fub (alo L vn e, inTerra vel Aquis ver fantur, exactiffime videre poteft: © in Carbunculo fiue Eาs Lapide, Aëream omnem \&o Igncam Regionem ex13. plorabit. Et, fi Voarchadvmico, nostre Hieroglyphice MO N A D I S, Theoria vige imaprima, fatiofat ciat; Iffiq́ue, Voarh beth $\triangle$ dVmoth, Speculandum miniftret: Ad Indos vel Americos, non illieffe Pbilofopbandi gratia, peregrinandum, fatelitur.

Deinque de ADEPTivo genere (quicquid vel 14. ARI I T O N eArs fubminiftrare, vel polliceri pofit; vel viginti Annorum maximi Hermetis labores funt affecuti) asmisb. licet ad Parifienfes, fua M ONA D Epeculiari (AnagogicaApodixi illiffratum) aliàs feripferimus: Vestratamen Maiefati Regia confanter afferimus, ID OM N E, Analos gico noffre M ON A DI 5 Hieroglypbica Opere, ita ad viuiu cxprimi, pt Simitius alisd Exemplum ${ }_{2}$ bumano generinons pofet

MAXIMTIIANVM.
,, poffet proponi. Quod, in feipfum, dupliciter, traducere de, bet:Ip ris Imitari Dignificationenn.
$\mathcal{X}$ (unc, Satis à me; (Imò vereor, fo bee hominum audi= ret Vulgus, ne plusfatis, ) de Raritate noftri buiuf(c Muneris Theoretici, effe dictum, (Triplicis Inclyte Diadem.1tis Honore) Concedas Rex $O$ Shaximiliane: Eifdem'que limitibus, eiufdcm definiri Bonitatem. Satis ergo fit, (Regum omnium Decus fingulare) boc noftrum Munus, Dum, tam effe Rarum demonftrauerimus diligentius, $\mathcal{N}$ (eminem tamen (licet Inuida Lingua Petulantia SMaledicentiff2mum quidem) © Aucm effe I fopicam muffitare poße.Tan tum profécto abeße, vt iustè, illius Indignitatem ferat $C a *$ lumnia, $\mathcal{O M o d e s t i f i m i ~ o m n e s ~ S a p i e n t i f / i m i q u e ~ f a t e b u n t u r ~}$ Pbilofophi:quòd non dedignabuntur Illi quidé, rnà meccư, Laudes or Honorem illi Pbanici accinere, ex cuius Solius Mifericordie Alis, Rarif/tmas iftas omnes cum Timore or eAmore extraxerimus Theoreticas Plumas:cötra noftram per Adamum introductam Nuditatem: Vt eijdem, 'fgnorantie asperrimis quibufdam frigoribus, multò refifteremus alacriores: © Errorum Turpitudinem, à Pbilofophantium tegeremus oculis; Honestal V ERI TA Tisftue diofffimi. Et quamuis Auctoritate aliqua bumana, nullo modo, Jic fumus freti, Sicubi tamen, Antiquif)imi alicuius Pbilofopbi, opportunè poterat noftro illustrari Lumine, aliquod notabile dictum vel Scriptumi ibi, illud anvo cè nostris exbibere Posteris, non recufauimus: Veluti in Hermetis,

## PRAEFATIO AD REGEM

Hermetis, Ostanis, Pythagora, (Democriti, \&o Anaxaga requibuSdam Myferïs : In que, ex nostris Hieroglyphicis defcendimus Demonftrationibus, non tanquam ab il lis, fidem emendicantes in istis. Etifam tantam Raritatem, ita, Dbiq́que coniuncta Comitatur Bonitas: vt Nibil, vel apertè vel tecfè, in hoc libello à nobis effe pofitum, Protestemvr, quodnöIdem Honeftum, fincerum, Dignitati Humana aptum $\varsigma_{\mathrm{I}}$ : ' Pietatis perfectißime, Rea Ligionisque veraftudio Vtilißimum. Et vt O P $\odot O$ I OMEIN certè, in tam arduis SMyferüsnon poteff, nifinlle, Qui, corum perspectis ßmam babet omnë Amplitudinem: Sic Nemo citius Infantiam fuam, ©Malitiam, vel Arrogantiam proderet, quàm Ille, $2 u i$, quicquam eorum que bic Viestre Sapientic Commendauimus, vel tanquam Impium Condemnare, veltanquam friuolum Reïcere auderet. Cuius rei, cum nullum, velIudicio eAcutiorem; velVfu Expertiorem: vel Auctoritate Potentiorem: vel Sinceritate Fideliorem; adducere quis poof it T Testem, quàm $^{\text {s }}$ Summus Ille Regü Rex Omnipotens, Regem fecerit MA. ximilianvm: Erit ergo mibi Vestra Augufa $\mathcal{L M a i c}^{-}$ Stas infar aliorum Omnium: (uit, hac nostra, Probataeffe, baberique Rata; non folum, Triobolarium multorum obtburabit ora Grămaticastrorum: Sed etiam multorum Pbilofopbantium eriget animos : vel bumi, iam, propter tantorum Myjferiorum proclamatam Incertitudinem, Iacegtes: Vel,propter Rerim Raritatem, fmperitorum Superba timentesIudicia: 2uiBona cum Malis (temerì, promidicul-

MAxIMIEIANVM.
promi(cueque, ex nominis fola Similitudine,) condemnare folent Studia. Cum maximè deplorando( interdum) Optimorum librorum interitu. Quorum Dtrumq́qe, Reipub. Cbristiana, plurimum, varüs temporibus, attuliffe detrimenti, clariffimè conftare poteft. Apto nimirum ad tam magna tractanda Capeffendáque fngenio, vel priori ratione perterrefacto: vel iam, quidem, cùm Progreffus baud mediocresfecerit, Rustice eiufdem or Superbè, ab Imperitis 'fudicibus, oniuerfo tam nobili tamq́ue diuino © Myfteriorum condemnato fudio. At alterius eft loci, ingulis Scientüs Honeffis, fuas comparare amulas: fal!as illas quidem, Vmbratiles, Odiofas, Molestas, Hominumq́ue Societati Inutiles. 2uas, Solas, \&\% earatione qua vulgares captant homines er exercent: nen Tulgarif olum, fed Sapientiffimi cuiusq́ue Iudicio explodēdns, condĕnandasq́que, © fatemur, © ita diligentifjimè fieri, nos quoque, jüdemus. Sed, Qui, C ORP OR A illa, vel Effenefiant, vel Ubi, vel Qualiafint; Quorvm ifte tenuiffime funt Vmbra: Quo modo, Illi, Hominum non Uulgarium, non Uulgaria condemnare Studia, velaudent, velfaltem'fure poffunt? FIA T I vSTITIA. Unicuíque, Quod Suum. efts $\mathrm{I}_{\mathrm{ic}, \text {, tribuatur, in iftis. Vulgaribus Sciolis, Artium Ma- }}$ gnarum Vmbras non feitantibus folum, ed exfdem etiam freleratifjimè ementientibusodulterantibusq́ue : Nugas, Errorem, omnemq́ue adfcribamus Impietatem: At in Bonis Solidisque ftudijs Prouectioribus : © boncftis mori. bus tum coinfirmatis, tum fua integritate Clarifimis: Vel,


#### Abstract

PRAEFATIO AD REGEM Vim (obleuem Vulgi Calumniam) Inferre: Veleorum in Odium Vocare Nomen, fudiaq́;: vel in dij(rimë,, Vitam:nă folum inhumanum id mibi( ( Rex) Sed Iniuffum © $q$ quafi Impium, Videtur.Nam, vt Corporum quorumcunq́que,oms nes pbicunque Vmbre, Сомm vn es cum ipfis Corporibus Termin os babët: (2vod Mathematicis eff no. tißiimum) Eodem modo, ©̛ bî, Pbrafes Loquendi, Scribendiq́ue: V'mbris, Verisque ipfis Corporibus,_(ommunes effe, Permitturt Sop н i. Vbi, Imperiti, Temerarÿ, eo Prefumptuofi Simie, V'm ar as Captant foles, nudas, छ Inanes: Dum fpfi Sapientiores Pbilofophi, CorPOR VM Solida fruantur Doctrina er fruitu gratiSimo.  kaberese putabant, (vmbratile,) tanquam non Solidum? \& Sinctrum, ex maxibus cripiatur, iustij] imè: : ${ }^{\circ}$ Cor poo' rat tractantibus, Vmbrarum omnús Iit conceffa honefalegintimáque Comprebenfio et) Cognitio. OP O O T O MEIN igitur oportet, ( 0 Rex, ) inter Vmbram \% CorPvs : © rotrius'que distingure fines, vires, or vfurs, I vs titie Itleeft Gladius, Regius, Imperatoriusq́ur: cuius, vt alia multa, ita, \&o hoc, est praflare Diuinum Munus. Et Arte profecto quadam, interdum, IpfiSophi, Vmbratiles figuras, intra ipforum Corporum Sinuofocsunfrafius libenter admittunt: : ne Afinis in Hesperidum Hertos, ruditer irruentibus electij jime prabeantur Laétuce, cùm illis Juffciant Cardui. Ignefres mihio $O$ Rex, Mundumple'fniuffitia (ex Clriffi Auctoritate) arguenti.


Neque

## TYPOGRAPHO,

GVLIELMO SILVIO:
Amicofunfingulari;
IOANNES DEE LONDINENSIS,

$$
S . \quad \mathcal{D} . \quad P
$$



Ides Amice mi, Optime Gulielme, Quàm vnice charas, Preclarilsimas hiabeam, Illuftrifsimi Regis Maximiliani Virtutes: Cui ex Cordis mei Scrinijs,Rara, excellentifsimaq́ue communico Ar, cana:Eáque ratione, illicommunicanda Curaui, vt etiam Plures per Terrarum Orbem (tum in cius Honorem,propter eximias fuas, Regíásque virtù, tes: tum vt Alijex illo Sibi exemplum capiant: qui \& Regiis Sapientifsimè vacare Regnorum Gubernaculis: \& Philofophorum tamen, Sophorúmque Stupenda cumulate addifcere Myfteria poteft)Plu res, inquam, eildem frui; Veftra Diligentia, \& Fide queant. Duoigitur funt, quæ mihies orandusmaxime: Vnum, Vt vbíque accuratammeam, in Lite rarum Varietate, Punctis, Lineis, Diagrammatibus, Schematibus, Numeris, aliisque, Imiteris, (quantum pofisis) Diligentiam: $\mathrm{Ne}, \mathrm{Idem}$ Ipfum, quod Ego(Deinvty) peperi ex omni parte bene Formatum Corpus; Typographix Negligentia, vel Mutilum, vel Deforme prodeat in Lucem : indignum

MAXIMILIANVM.
10
Neque bec, Dllo modo, boc loc, bijs Temporibus,Tue pres. fertim cömemorata Sapientia, Parergacenferivolo: immò ne Superflua quidem. Atque hac bactenus. Huncergo meum Monadis Hieroglyphice Fatum (Conceptione quideै Londinenfem, Natiuitate vero Antweerpienjem) Uefra Serenifime Maiefati, bumilimè of fero:Obnixè à vobis̀ contendens:vt eiufdem non Dedigne. mini, nurı quidem, fieri Compater: pòft verò, cùm erit \& atate grandior, © fide fua Commendabilior, in Deffrafems. per vobis ve feruire pofit prafentia. Pro veffro, deinceps Egocundem baberi volo, o Clementißime REx: Qui, vt mibi vijusestotopartus Tempore, Blandißimo ASpectu, ante oculos verfari meos:ita, ea ratione, facilem mibi expes ditumq́ue buius in Lucem editionisis, Laboremf fecisti.Nam
 eurdem, incredibili veffra ad tantum Interuallum, Virtu- tfyit mee

 Faufü̆qúqe effe, tum veffre eAugufec Celfitudini, tum ar- 1 ssisice
 la Sacrofancta Trinitas, Que(in Mona dis Ineffabilis, Omnipotentia, ante omnia Secula, fundata, ) viuit regnatq̆ư Sempiterna: Cui Soli, omnis Lutus,Honor, Uirtus (4) Gloria, ab omni femper exbibeatur, decanteturq́ue Creatura. Amen.
$\frac{\text { Antwerpic. }}{\text { Anno 1564. 7anuery, 29. }}$ C.2.

## AD TYPOGRAPHVM.

II dignum,fiquidé, Regetanto; Indignum verè Philotophantium Studijs, \& laboritus, quos in copenitífime, fępifsiméque examinando, collocare volunt, Maximis. Cauere tamen latis, de ifo, mihi Videor, Infortunio, dum te elegi, Ittius nouiter Nati Operis Parentem Typographicum: quiomnibus modis, nitidum, fuifque bene Compofitum Membris, tua Curatura, emittere potes.

SECVNDVM, quod à te preftari Optarem, haud eft leue, id quidem: Nimirum, Promifcuo vt hominum generi, hofe, nullo modo, in marrus des Libellos. Non quòd illis ego hxequidem, vel meliora, inuideam: Sed hoc inde oriturum mali Sufpicans: Non folum, quod, ex ifto Labyrintho, Se , Miferi,nunquam extricare poffunt:(Ingenium in terca, Incredibilibus Angentes modis, pefsiméque fuis profpicientes Rei familiaris negotijs) fed ectia, quòd, Alijs quoq;,(illis inuium) vel, Ingredi fuadebunt Iter: vel de ciufdem, veluti illis explorata, Certitudine,Sceleratifsimè ementientur; Impoftores, Hominúmque Laruæ:Vel Denique, talia DeI Magnalia, Effe, Negare; Aut meam, rabidifimè accufare Sinceritatem audebunt : tunc tandem Defperabundi; Vt,primò, hæc Myfteria, cum maxima Prefumptione aggrefsi funt Temerarij. At in hoc tanti Momenti negotio, Si te bene à multis iam annis noui (vel propter amicitiam noftram:

AD TYPOGRAPHVM.
vel Reip. Chriftiajax Vedilatem; vel faltem propter Ipfius Sapientifimi Maximiliani, Heroicas Virtutes, que nihil Commune cum Hominum Vulgari habentSorte) Cauebis, Spero, ne Fidem tuam fruftra requifiuiffe Videar. Cauebis tu quidem: \&, per te, Horieftisimi omnes

Librorum Mercatores. Valeas.

Ex SHufao noftro Antworpienfi:
A Avo Is64. Fanuarй 30

MONAS

MONAS HIERO-
THEOREMA TIIT.
LVnx Hemicyclium, licet hic, Solari fit Circulo quafi Sa-
 Regemq́que fuur obferudt : eiufdem Forma ac vicinitate adeo gaudere videtur, vt $\&$-illum in Semidiametri æmuletur Magnitudine, (Vulgaribus apparente hominibus,) \& ad eundem, femper fuum conuertat Lumen: $S_{O L A R I}$ z $v S^{\prime} Q \vee E$ itatandem imbui Radijs appetat, vt in eundem quafi Transformata, toto díparear Crelo : donec aliquot poft Diebus, omnino hac qua depinximus, appareat corniculata figura.

THEOR. V.
ET Lunari certè Semicirculo ad Solare complementum perductö: Fätum eft Vefpere \& Mane Dies vnus. Sit ergo Primus, guo $\mathrm{L} v$ x eft facta Philoophorum.

THEOR. VI.
SOlem, Linamove, Rectilinex Cruci, inniti,hicuidemus. Que, tumTernariym,tum QvaternaTI I $m$, appofitec fatis, ratione fignificare Hicroglyphica, po-
 Etis, \& Communi vrique, quafi Copulaticio Puncto. Qviternarivm veroees 4 . Rectis, includentibas 4.Angulos rectos. Singulis, bis, (ad hoc) reperitis; (Sicq́ue, ibidem, fecretiffimè, etiam O cto NARA*s, fefeoffert; quem, dubito an noftri Pradeceffores, Magi, vnquam confpexerint:No: tabisçue maxime.) Primorū Patrum, \&SOphorüm $T_{E}$ ह̉Nativs, Magicus, Corpore; spisity, \& antuA, conftabat. Vnde, Manifeftum hic Primariŭ habemuṣ Seprexarive.Ex duabus nimizumpeatis, $T$ Communi Pumcto:Deinde ex 4 Rectis ${ }_{2} \triangle B$ Vno Puneto, fefe, Separantibus.


MONAS HIEROIVNCTIO. Tunc enim latére non potcit, quantum noframonadis, Soli, Lynae Qve, Crucis $\mathrm{D}_{\mathrm{f}}$ vazia inferuiat Proportio.

THEOR. $X$.
DOdecatemorij Arietis,omnibus eft notiffima, quæ eft in Aftronomorum vfu (quafí Aciordes, Acuminataćue) figura gnex, ifta:Vt \& ab hoc cxli loco, Triplicitatis I. notari Exordium conftat. Adignis ergo mi nifterum (in huius Praxi MONAD I s) requirifignificandum, Arietis adiecimus Aftronomicam notam. Sicquebreuiter, noftre Mo Na dis, vnam abfoluimus Confiderationem Hieroglyphicam: quā fic volumus, vnico Contextu Hieroglyphico proferri


Monadis istivs,
IvName Sol, sva separarivolvite IEMENTA, IN QVIBVS DENARIA VIGEBIT PROPORTIO; IDQYEIGNIS FIERIMINISTERIO.

THEOR. XI.
A Rietis Nota Myftica, ex duobusSemicirculis, in communi Puncto connexis, conflituta: Aequinoctialis Ny cthemeræloco aptiffimè affignatur. Viginti enim \& quatuor Horarum Tempus, Aequinoctij modo diftributum, Secretiffimas noftras denotat Proportiones . Noftrí dico refpectu Terrx.

THEOR. XII.
A Ntiquiffimi Sapientes Magi, quinque Planetarum, nobis tradidêre Notas Hieroglyphicas: Compofitas quidemomnes, ex Lvaevel Soins Characteribus:cum Elementorum aut Arietis Hieroglyphico Signo. Veluti iftas,

explicare difficilc.Atprimùm, de ijs quæ Lunæ habët Charaterem, nosnunc Paraphrafticè agemus: de Solaribus deinde. $\mathrm{Lv}_{\mathrm{Naf}}$ is nofra Natur, dum per Elementorum fcientiam, circanoftram fit femel reuoluta Terrä, $S_{~ A ~ I ~}^{\text {V R }}$ n v s myfticè dicebatur. Et eadem de caufa, Io v is quoque habebat nomen:iftamque retinebat figuram fecrenorem. Er Lunam, rertia elementatam vice, obfcurius fic notabant. Quem, Mercyriva vocare folent. Qui, quàm fit $L V{ }^{2} A R$ I s, videtis.Iftum, CVARTA Reuolutione produci, licet Quidam velint Sophi : noftro Secreto propofito tamen,non erit id Contrariam : Modò Spiritus Puriffimus Magicus, loco Lurax, тìs $\lambda$ enzársos adminitrabir Opus:\&fua virtute Spirituali, nobifcum Soiv s,per Mediam quafi Naturalem diem fineverbis, Hieroglyphicè loquarur:in Puriffimam Simplicitsimamq́ue, à nobis preparatam Terram, Geogamicas, iftas 4 introdu-


THEOR. XITI.
MARirs ergo Character Myfticus,an nonex Sol is \& ARTETIS, Hieroglyphicis,eft conflatusì elemen:
 fo, an nonex $S$ o lis \& Elementorumi Pleniore Explicatione? Intiergo Planctr, S o la a ex refpiciunt meierocain, Opusíue A'salacervpriosess: In cuius progreffu fit tandem

GITPHICA.
ille Hermes, nos olim admonuit: Eius Patrem, $\mathrm{S}_{\mathrm{L}}$ п em, effe, afferens: L v x a m autem, Matrem : Nutriri verò Scimusin Terraiemnia. Radijs nimirum Lynarievis \& Solaribys, Singularem circa Eandem, exercentibus INFLVENTIAM.

THEOR. XV.
SOirs proinde Lvnaévecirca Terram Labores, Philofophis proponimus Confiderandos. Huius qui- I. dem, quo modo, dum in Aricte verfatur Sof a e e Iubar: Ipfa tunc in Proximo(fcilicet Tauri) Signo, Lucis nouárecipiat Dignitatem: Exaltexvéove Supra Innatas fibi vires. Quam (præalijs notabilem magis) Lvmin aII v m, Vicinitatem, Charactere quodam mylfico explicabant veteres: $T_{\text {A }}$ v $_{\text {R }}$, infignito Nomine. Quam, quidem, Lveaeffe Exaltationem, vfque zbipha prima Hominum ætate(inter Aftronomorum Placita,) memorix effe proditum, notiffimum eft. At Intelligunt Myfterium Illi foli, qui abfoluti euafere Myfteriorum Antiftites. Vt \& fimili ratione, Veneris effc Domvn, dixere TavR V m : Cafti nimirum Prolificiǵue Coniv GAIISAMO-
 Ostanesin Secretifsimis fuis Recondidit Myfterijs.

So 1 is verò, qua ratione, Ipfe, poft Aliquas fui Luminis, 2 admiffas Eclipfes; Mar xiva Roburaccipit : \& in ciufdem quoque D ом о (Noftrof filicet Ariete) veluti in fua Triumphare dicitur Exaltatione. Qux Secretiffima Myfteria, noftra etiam M on a s clariffimè,perfectiffimeć; demonftrat: TAvkiquidemifta que hic eft depista Hieroglyphi- taurus ca figura: \&illa Mar trs:quā 12. \& 13 .Theoremateadduximus: quæ Solem Recta in Arie- Ar т $₹ \times$ tendentem, indicat. Exprefenti autem Theoria, D 3 Alia

MONAS HIERO-
Alia noftrx Monad 15 fefe offert Anatomia Cabalifica: cuius ifta eft vera Artificiofaq́ue explicatio. L v Nae, so. LIS'QVE EXALTATIONES, MEDIANTE ELEMEN TORVM SCIENTIA.

ANNOTATIO.
Dro bic maximopere notanda effe Cenfoo: vnü, quod Tauri Hierogl. phica isfa figura, nobis Grecorum Dipthongum z, exaltereprefontet, Prime Declinationis, Gignitiuem femper fingularem Terminutsonem. Ses caondó, ex apra Metathefi Locall, dupliciter nobis A 1 P н 1 commonftrat:


## THEOR. XVI.

IAm nobis de Cr v c e, paucis, ad noftrum propofitum, eft Philofophandum. CRvx noftra, licet ex duabus Rectis(vt diximus)\& xqualibus illis quidem, confecta fit: non fe mutuo tamen in $x$ quales diffecant longitudines. Sed rum xquales, tum in rquales partes, in Myftica noftre Crucis diftributione, haberi voluimus. Innuëntes, in Binarum ita fectarum poteftate(eò quòd æqualis funt Magnitudinis) $\mathrm{C}_{\mathrm{g}}$ v c is quoque Aequilaterx, virtutem la. tére. Generalifsimè enim, $\mathrm{C}_{\mathrm{R} V} \mathrm{~V}_{\mathrm{E}}$, ex xqualibus Rectis, fieri iuffa; xquali profecto linearum Decuffatione, eam fieri debere, Narvan quadam requirit Ivsimia. Secundum cuius luftitix Normam, de Aequilatera C r vc.s(qualis ef latini Alphabeti litera vigefima prima) hec que fequuntur,perpendendaproponemus. Cry © is, „ReCtilinex, Rectangulx,\& Aequilaterx, Siper commune $\leadsto$ fectionis punctum, \& Contrapofitos angulos, Rectavbi„cunque tranfire concipiatur: Exveraque partc, fic tranfeun$\geqslant$ tis Rectx, Crucis facix partes, funt ommo fimiles \& $x$ $\Rightarrow$ ) zuales: Quarum figure, exdem funt, cum illa Latinorum
 Qvinariva denouandum, apud Antiquifsimos Latigorum Philofophos vfitatifsima erat:Idq́ue haud abfurde
abillis: 2 billis effe factum Cenfeo; cùmfit Denarij noftri, Conformis Medietas. Ex illius crgo figurx, Sic duplicarre (ex hac Hypothetica Crucis diuifione) proueniétis, ea ratione, qua $Q$ I INARI y m vtraque repre fentantlicet erectaaltera, Altera autem hic fit euer fajMonemur, Radicum Quadratarum hicimitari Multiplicationem Quadratam: (qux hic mirabiliter in $\mathrm{Nvam}_{\mathrm{E}}$ RVM CIRCVIAREMincidit, filicet QVINARIVM) Vnde produci certòconftat, VIGINTI\&RVINQVE: (vt \& ipfalitera, eft vigefima: \& Vocalium Quinta.) Nunc vero alium fitū ipfius $C_{\text {r v c is }}$ xquilaterx confiderabimus:iftum nimirú: qui noftreMONADICAE Crva is Sirui eff fimilis : Similem autem hic fieri Crucis Diuifionem bipartitā'(vt fupra) fupponimus.Vnde alterius literre, latini Alphabeti, fe monftrat etia geminata figura:ereeta vnajeuerfa, \& aucr13, altera: Que (ex Latinorum veruftifsima confuetudine)ad Quinevagintareprefentandum, invfueft. Iftud, inde mihi primò ftaturum videtur: Eò quòd fit \& Illa quidem Qvinarit, Nota; ex noftro Crucis Denario, effentialiter defumpta: at co fitu Locatx, quo, omnium Myfteriorum Maximi, ipfa Crux, eft Confummatifsima, Hieroglyphica Nota: VndeDenari i Poteftatem, in fua Qivinaria Virtute Compiectens, evinCVAGENARIo NVMERO tanquam fuo Partui,gratulatur. O, MI devs, QVANTA HAEC MTSTER IA ? \& Nomen illi, $\mathrm{E}_{\text {I. Immò \& hac ratione quoque, }}$ ipfam Denariam Crucis virtutem refpicere videtur; quòd Medio Loco, inter primam Alphabeti Literam, \& ipfum Crucis Denarium fit conftituta : \& ab alterutra, ipla fit, ordine, Decima. Et cum in C RVCE, duas ciufmodi integrales effe partesoftendimus(Numeralem nunc folùm earundemvim Confiderantes) Centenarivainde excrefcere

## GIYPHICA.

${ }^{5} 7$
ficiunt. Quem Numerum, duabus adhuc aliis rationibus: ex promirsis vt nos elicere poffumus: ita Cabalifticis Tytonibus, eundem commendamus eruèndum: breuitatific Studentes: Eiufdé tamen Magiftralis Numeri, variam productionem artificiofam, Philotophorum dignam Iudicantes Confideratione. Nec vos,aliam, hic, Myftagogiam Celabo, Memorabilem. Cz ve ex noftramin duas alias literas, fe Diftribui Paffam, Videntes: Si , vt Numeralem earundem virtutem quodam modo perpendimus prius, ita vicifimnunciliagym verbalemping civa ipSACEVCE, CONFEREMVS, quòdinde Oriatur Lvx:Veravm, Finale \& Magiftrale (exilla Terna${ }^{2}$ I 1 , in Vnitate Verbi, Confpiratione \& Confenfu) cum fumma Admiratione, Intelligemus.

THEOR. XVIII.
EX duodecimo \& decimotertio Theorematibus noftris colligi poteft, Caleftem Aftronomiam, In FERIO-
 R is effe quafí Parétem \& Magiftram. Subleuatis ergo in Cxlum oculis Caba lifticis(ex Predictorū Mylteriorü Theorica llluminatis)talé ad amufim noftrx Monadis, confpiciemus Anato miam:InNatyRAE IVMINE,VI: ta ovelefe ficnobis femper oftenderem. Etfuopte Nv IV,Secretilsima hu-

E iufe

MONAS HIERO
 gentem. OVI autem figuram, iffiC OOR DINATIONi adhibere:Caleftis $\mathrm{NV}_{\mathrm{V}} \mathrm{CI}$ I dum Theoricos, Cate fteĺque Geftus, fumus aliquando Contemplati, fuimusedocti. Ovai ese enim, Ipfum, in Aethere, fuo Curfu Figurare Circuitionem, Aftronomis eft notifsimum. Et, cìm Dietum, Sapienti,Sat effe debeat: En noftras huius Caleftis Confilij Interpretationes (fic Hieroglyphicè propofftas:) pradietis omnino Confentaneas. H I a c Monitu, difcant Miferrimi Alchimifta, fuos agnofcere Errores varios: Qux fit Albuminis O vorvm a QVa: QVodex yitelifs oleva. Que OVorvm caix:Hinc, Imperiuifsimi illi Impoftores, cum illorú Defperatione, $\mathrm{In}_{\text {n- }}$ telligant: Aliaq́ue his fimilia, perplura. Hî $\bar{c} P_{\text {r }}$ o porn tionatymanatyra, fere totymban bemvs. Hocilludeft Ovva abiininvm, Quod Scarabevs, olim difrupit:Propterin ive iam,quz Timidis Brutif́; Hominibus, Illius avis Violentia \& Crudelitasintulit: Licet ad Scarabci Antrum (Auxilij Implorandi Gratia) aliquibus confugientibus, non inde tamen liberatis: Sed ipfe folus Scarabeus, hanc fibi vindicandam In IVRTAM, modis omnibus, exiftimans: Vt erat alacri animo, Conftantiq́ue Voluntate paratus, ita, ad id praftandum, nec Viribus carebat,nec Ingenio:Vnde, varijs Conatibus $A$ ev ilam dum perfequeretur Scarabeus: Subtilifsima Fim I Arte vfus, Illius tandem (vel in louis Gremiodepofitü)Ovvm, in TErrampramctpitari adeoquc D ISRyMP I effecit. Et eadem, aliáueratione Aquilinam tandem totam Speciem, è Terris deleuilset Scarabeus, nili, (malum tantum Pracauens,) Iupiter, effeciffet: Quo Anni tempore,Aquilx fuafollicitè curăt $O$ v $A$, Nulli ve circumuolitent Scaraser. Illis tamen Confulcrem, qui itius A y is vexantur Crudelitate, ab ipfis

## MONAS HIERO-

عã libello videre licet. Nihil hic effe extra noftræ Mo NA, D I s virtutem Hieroglyphicam, qui animum iftis Myfteris fincerius applicat, clarifsimè perpiciet.

## THEOR. XIX

Qòd $\mathrm{SO}_{1}$ \& $\mathrm{L}_{\mathrm{y}}^{\mathrm{N} A, \text { omnibus cateris Planetis, longè }}$ fortius, in inferiora cuncta Elementata Corpora, fuas Corporales infundant Vires: Omnium rerum Corporata rū́nalysis pyronomica, Effectu demonfrat: Lynae dum refundunt Aqueum Humorem: Soliso Q ${ }^{v}$ E Igneum Liquorem:quibus, Rerum Mortalium Sufte. tatur Corpylentiaterrestais.

## THEOR. XX.

I Icet fatis boma ratione Hicroglyphica, fupra, demonftrsuimus, Elementa,per LineasRectas fignificari:Hic tamen de Cavcis noftre PvNcro quafi Centrai I, Exactiffimam dabimus Speculationem. In Teer n.sR 1 inofri Confideratione, nullo modo, Illud Abeffe poteft: in eo noftribinarii Situ. Si enim abeffe poffes Quis (Diuinx Imperitus Mathefeos) contenderet: Abeffe Supponat. Non erit ergo Reliquus, BinARIV nofter: Sed emerget Qviternarives: Punctiillius Ablatio ne, Difcontinuata Linearum vnitate. At Binarium effe Reliquum, vnà nobifcum Suppofuit Aduerfarius nofter : Erit ergo\&Binabivg,idem, \&Quaternarivejea-
 Manifefum. Adeffe ergo ex omni Necefsitate, debet illud Pvecrvm, quodcumbinarto noftrum Cofltituat TernarivmenecAliud quid eiusloco $\mathrm{S}_{\mathrm{va}} \mathrm{stir}$ wa poteft. Non tamen eft de Hypoftatica Proprietate, ipfius Binarymectaliquo modo Pars. Quèd foonf fir Pars, hinc demonftratur. Omnes Línex́ Partes, fúnt Linêx. At allud effe Pvex y P , hypothefis confirmat. Norr erge

GLYPHICA.
18
Heliocantharis (qui ita certis Temporum Curriculis latitando viuút) Vuilisimam artę difcere: Quibus,immlicet nō faciant ipfi, effet tamen longè gratifsimú, fuis IN $\boldsymbol{D}$ I ci is $\&$ Signis, de fuo Inimico, Vindi $\neq a 3 m$ fumi poffe. Et hic ( O Rex) non Aefopum conari me vt agam,Sed Ocdipum,Faterentur; fi adeffent, illi, quorum Mentes, ita de Nature Summis Fabulari Myfterijs, primò fubiuit. Effe profe-
 haberent Dissoivtym AQvilinvm ovvm, $C_{A L C E M}$ eiufdem, cum Albumine puro, totoq́uc $T_{E M} M$, perarent primó. Deindcillud TemparamenivM, Viteili liquoretoto,artificiofo ordine, oblinirent:voluendo,reuoluendoçúue: Vt Scarabei fuas conglomerant Pilas. Ita, magnaficret $O$ vi Meramor-
 cetdifparëte,\&quafi inuoluto $\mathrm{Al} \mathrm{B} \mathrm{VMI}^{2}$ N E ipfo(illismultis, velutiHelicis Reuolutionibus factis ) in ipfoVitelifinoso hrevore. Cuius Artificij,taleHieroglyphicum fignū, Natvramhaud difplicebit Oeconomis. Sæculis prioribus, multùm effe à grauifsimis, \& Antiquilsimis celebratü Philofophis, tale Artificium,Fegimus:cenifsimum \& vtilif. fimum. Anaxagoras certe, ex hoc Magifterio, excellentitisi-


Binamitillius Pars aliqua: Vnde multo minus de Hy poftatica Proprietate Binarij. Proinde No i a si v va eft naximè, quod \& Propriam Habeat н ypos tast $\mu$ : Et nihilò minus tamen, in ipfis noftri $\mathrm{B}_{\text {INA }}$ R i i Longitudinibus Liseakibys,cötinearur. Etquia,Sic, VtrisQ VE videtureffe COMMVNE; QVANDAM, \&IPSVM, zINARIT, SECRETAM RECTPERE IMAGInem cenferi. Vnde, Qyaternarivm, Hic, Demonstramvs,internario eviescentem. Tu, mi Deus, mihi ignofcas obfecro, Si erga zuam nunc Peccaucrim Maieftatem, tätum, in Publicis Scriptis, Reuelans,Myfterium.Sed Spero,quòd,Soli,qui fant Digni illud verè Intelligent. Pergamus nunc ad noftra $\mathrm{C}_{\mathrm{R} \text { v } \mathrm{C} I \mathrm{I} \text {, }}$ illum, quem alsignauimus Quternarivm. Vbian Abeffeillud $P_{\mathrm{v}} \mathrm{c}$ т у м poteft, quod $\mathrm{I}_{\mathrm{B}} \mathrm{I}$ Reprcfentatur.perpendamus. Mathematica profectò nos docet remoueri poffe. Nam non Solum, Eosfaparito, Relin evvis Eftnofter Qvaternarivs: Sedcum Distinctiorlongè, tum Ciariorinomnium oculis crit Factive. Nvila svae sugstantiaLIS PROPORTIONIS RECEDENTE PARTE: SED SVPERFLYO, ET CONFVSIONISPYNCTO, Sic damnato, reiectóqve. O Omnipotens Diuina Maieftas, Qyantam tivisapicizvs, er IOTIS, INTVA DESCRIPTIS, DISPOSITIS'QVE LEGEINESSE SAPIENTIAM, ET INEFFAbilivmmysteriorvminfinitatem, Con fiteri cooimvr mortaies: Simaxima terrena secretamearcana, vinivitsTIV'SPVNCTI, AME (ATINTVOLVMINE) hocate et examinati, indicio vaRIO, Explicarietfidelissiam demonstanateveant? Punctividelicet, inTeana-

MONAS HIERO-
rio diwino, nullomodo Svperfivitat pyncti in Qvatvor elementorvm receoc confide rati, Fabcilentiquidem, Corrvipitilits, TENEBRICOSI. O Terq́ue, Quaterq́ue Beatos Hllos, quilludTbranti, (quaficopviativvm)adiq pisci poffunt Pvectivm: \& illud Qvaternan
 ", nebrarumq́q; Relinquere Principi.Sic,ad C la r it a tis力niyeab, \&aibarvmvestivm Ornamentaper. „ueniemus, O MAXIMILIANE: Quem,Deus,(ifta Myftagogia, aut Auftriacx Familix aliquem)Maximum, aliquando faciat (vel me quidem in Chrifo Dormiente) ad fui Tremendi Nominis Honorem: in iftis, Iftis, (Punctiin TERRIS SVPERFLVI, abominandis Tenebris;\&ulterius, intollerabilibus. Sed ne Ipfeiam Superflua (non apto fcilicet loco) profundam verba, intra Propofiti med Cancellos, actûtum, nunc me recipiam. Et, quia, illis Sermonem iam abfoluerim, quoram Oculi in eorum Sedent Corde:Nuncmihi ad illos cóuertenda Oratio eft, quorum Corda in corüadhue promineant oculis. Qux hocloco di, ximus, En CRvers adifripta figura, aliquo modo reprefen tare poreft. Primùm, de Pvn сто, in Binis Aequalibus Lise is (rqualiter \& inrqualiter decuffatis) NECESSARIO; Velutihic,ad A. Dcinde, adB (quafrquandam Punctifiperflui ablati, Vacuitarem)diftinCas videris, $Q$ yar vor rectas Lineas:iे v п ст o, priusillis cómuni, Separamas:Illis, inde, nullo equenicnte fai detrimento.
 \%Hact via, per quam Noftra Monas, per Binarium, TE:R$2 \mathrm{NABIV} \mathrm{M}^{\prime}$ Q I progrediens, in evaternario Pu\#nificatos is i. 1 Vni reftituatur, per Aequalitatis Proportio2n nem. (Qaodq́ué enim Totum, fuis omnibus.partibusełt

Aequale.)

## MONAS HIERO-

(hoc nouo modo Locatam)in Anatomica Membra B.D.C. Vbi,in illo nouo Ternario; ipfius D, \& C, vel Rufticis quidem, funt nota $\mathrm{F}_{\mathrm{I}}$ gvrae.AtilleTertivs,quiper $B$ defignatur, non tam facilè à Cuntris cognofci poteft. Nec illud quidem leuiter eft confiderandum:illas 1. tam notas Formas, $D$, \& C; fepa-
 ratas diuerfasque ab illo B , oftendere Essentias: Se 2. cundò, quòd iftius C , cornua, deorfum, quafi $\mathrm{T}_{\mathrm{ER}} \mathrm{RA}_{A K}$ verfus conuerti cöfpiciantur: $\mathrm{Et}, \mathrm{D}$ illius, ea pars quæipfam
3. C, illuminat: verfus terram, deorfum Scilicet,refpicit:incu-
 4. st re e.Et Quòd vtraqueDenique D \& C,ad Inferioramagis loca, hic fuum Hieroglyphicum faciút Indicium, quàm B. Terra autem, Hieroglyphicè, Stabilitatem, \& Fixionem.notare nobis potef. Qualia ergofintD, \& C, inde, concludendum relinquo. Vnde etiam Magnum nunc notare S ECRETVM, Quifq; poteft:de Priore so$I E \& L V N A, q u x$ diximus, quo modo hinc Interpretationem pleniorem, \& maximè neceffariam, recipere poffunt Illis quidem, vique in hunc locum, furfum politis: Lunaribusq́ue Cornibus furfum elcuatis. Sed de hoc Satis. T ERII I nunc illius,Iuxta noftre Hieroglyphicx Artis Fundamenta examinemusnatraiu. Primò, in Capite geftare
 inuerfum Myticè., Deinde Elemétorum habet annexum Hieroglyphicum Signum. Quantum ad Lvnam Du plicatam artinet: Sie(iuxta Mateviarnfabiectam) explicari poteft: DVPiEX IVNAE GRADY s.De gradibusloquimur illis, quales Phyfices Periti, Q v A $\boldsymbol{T}$ vo r tantum inter omnes poffintinuenire CreatasNA x y 1 a s: Nimi-

GIYPHICA.
Aequale.) Hocq́ue dum fiat, nihil interea Externarum ad- cc mirttir, Noltra Mo nas, Vnitatum:Numerorúmue:Cum cc ipfa fibi exactiffimè Sufficiat: Suis abiolutiffima Numeris cc omnibus. In quorum Amplitudincm, tum Magicis dif- ce funditur modis: tum non vulgari, pò̀t, Artificis Induftria, "c \& maximo Ipfius Monadis Emolumento, (in Dignitate \& ic Potearia) ad fuam Primam Propriamq́ue Reftituirur MA- " tEAIAM: interim, qux ad genuinam hereditariamq́ue cs fuam non Spectant Proportionem, omni modo \& diligen- ce tia, refétis,rciectisque in xternum Fxcibus.

THEOR. XXI.
SI, Quod in noftre m on A id is Receffibus, Interius Latebat Inuolutum, effer id quidem in Lucem crutum; cōmu tatisq́ue vicibus,eiufdem Partes Primx, quafiq́ue Exteriores, Loco Includerentur Medio, Qualis inde fieret M oNA d is Philofophica Transformatio, Superius Vidifis: Nunc verò, Myftice Monadis, aliam vobis proponemus Localem Commutationé: Partibusillis,vndeS v p eriozym planetarym, Characteres noftri Hieroglyphici, fefe nobis obrulere prius,Surfum hic erectis : eaq́; ratione, reliquis quidē deinceps Planetis, eum fingulis Sortientibus Sitū, qué illis Plato adicribere ferè vifus eft: Si ritè ex Pofirione ifta defumantur. In ipfo enim Acumine Arietino, Conueniunt Saturnus, Iupiter,Mars: deinde defcēdendo, Crux V'eneri Mercuriós; inferuitSequuntur tandem ipfe Sol, \& Infima $L_{\text {v }}$ a . Sed hac alio
 funt ventilanda loco: Noftrx tamen monad is hofce nolui celare ThefaurosPhilofophicos: Sicq́ue vriam rationem dare, cur ita Mon $\wedge$ dis mutari Situm, confultum duximus. Sed, alia, qux in rem vefrram effe fcio, Videte, Auditecque, de hoc Situ, maiora: paucisfure explicinda. Diftribuamusigitur M ONADEX,
(hoc

## GIYPHICA.

21
rúmesse, vivere, sentire, \&intifliceix E . Primos ergo Duos iforum Gradus, huic ineffe annotantes:Sic dicemus:L, vNaEXISTENS, VIVA. Vitáverò Quidam per Morum definiunt. Mo y v s autem Sex funt notiffimx Species. C r v x certè quæ adiū́ta eft: Elementorum hic requiri Notat Artificium. Preterea, in
 fe Hieroglyphicum fæpiffimè tradidimus: Ita \& Integrum Circulum, $S_{0}$ i в м fignificare: hic autem, duo funt Semicirculi; Sed SEPARATI (ad commune P yN cyva Copulati tamen)qui, fi aptè coniungantur (vt arte poffunt quidem) Solarem nobis Circularemq́ue referre poffunt Plenitudinem. Ex iftis fimul confideratis, fic Summatim, Hieroglyphicè, nos hanc proferre poffe Sententiam patet. Lvinaexistens viva, pferelemenTORVMTRACTANDA MAGISTERIVM: HABENS potentiam, vt soentem representet PLENITVDINEM, SVIS SIMVLARTECONNR$x$ is semicircuits. Compleatur ergo: Fiatq́; ille, (quem diximus) Circvivs: vt, per Eliteram, hicannotauimus. Memores ergo fimus, primò hunc $S_{O}$ I $A \mathbb{R E M}$ GRAD v:M, non Natura nobis fuiffe obuium, fed ARTIFICIALEM, FACTITIVMQVEIam effe:Eteumquidem, nobis fe obrulifle primo afpectu, \& Natura fua, (videlicet in B) fuis Partibus Laxis, Fluxis, diffoluris; non SoIID E in folarem Speciem Compactis. Deinde horum Semicirculorum Semidiametrum, non effe xqualem Semidiametro D \& C (nobisita natorum, \& omnibus Notiffimorum) Ced Minorem multo. Vnde Clarum cft : non effe tantre Amplirudinis, iftum B, quantx funt ipfa D, C. Ethoc benenobis confirmat Eipfum: opere ifo Circulari, $\mathrm{a}_{\mathrm{B}}$, in Speciem E,pronroto.Nam indenobis emergit $V_{\text {ENER I }}$ folumCharater.Apertum ergoiam fecimus, Hieroglyphi-

MONAS HIERO－
cis itis Syllogifmis：Ex B，pon fperandum nobis verum D． Necfuiffe primò veram $C$ ，in naturara $B<V$ nde nō fuit $V_{z-}$ ra，LvNs，viua．De Virs ergo \＆Motu quoq；ia dubitare poters：an verè \＆Naturaliter，ficfe habeant：Erunt tamíe，rt iamPrudentibus Elucidauimus，ad minus a Na I 0 o 1 CA
 rius，que de C，$\& \mathrm{D}$ ，perffrinximus breuiter，ANALOCLCE Ipfi B，cum fuis Elem Entis，Propriè conueniunt．Qutede Arietis etiī Natura adduximus，hnic debēt exactè côuení－ re：cimn eandé illius in fuo capite（licetinuersä）geftet Figu－ ri：vr \＆Elementorū eadé Nota Myftica，ipfi B adiungirur．
Cùm ex hac tamé Anatomiavidemus，quòd exvnico no－ fitx m o N A D is corporétali diffeto arte）ife nouus pro－ dierit Teanal iys ：Indedubiare nō poffumus，Eitf－
 thiav：vnionemeye monadicam absolvtissiman，
 G simica virtus eftvegeta．
Hoc denique annotare libuit，（animi recreandi gratix） Quod ipfum B nobis， Rvsric cas，tot literas expediuiffi－ mè exhibet，quot Punctafurfum，conficienda in Capite，\＆quafi Fronte gerit：iffas ceilicet tres：$n<3$ vt\＆̊ alizs quafi fex：（Súmatim auté ter tria）zy DEs valde \＆impolitras funxiles volubile $f_{g}: ~: v t$ ，ex Semicirculis， ynovel pluribus，eafdé effée fuztas videtis．Sed Expertorum literatorumq́que manibus ineff frmior Stabiliorque is $s \not \subset s$ rozuandi lit Enas Ratio．Myfterioruinfinitaté，hic ante oculos habui：fedvoluicum hoc Ludicro，itam abrumpere Theoriam．Haud parū tamen me quorundi promoturf Conatus intelligo：Si（priorifuo Myffico Situi，reflituta no－
 bris）Saltem moneam eofdem，borter que：accuratius， ，vvs


8より析

## MONAS HIERO－

vt Videris：Ex Rectaenim，Circulo \＆Semicirculo，Vcrailh lius，Myfticäq́uciā nos primi docemus，Symmetriam（licer fupra etiä monuimus ex Circulo \＆Semicirculo eandé fien， ri poffe：omnia tamen in idé recidunt propofitū Myficumm） $\mathrm{At}_{\mathrm{t}}, \lambda_{2} \& \delta:$ ：Primú quidem，aliorū funt Vaforum quafi Ima－ gines：（ $\lambda_{3}$ quidem Vit re i i：$\delta$ auté，Terrei．）Sed，fecúdo in toco，$\lambda, \& \delta$, nos memores reddere．poffunt，cuiufdam Pi filli \＆Mortarij，ex Materia（verè）tali preparandorum，挔 cum eildemMargaritas Artificiales non perforatas，Lami－ nas chryftallinas，Beryllinaf＇， depreteriofos：Carbunculos \＆a alios Rarifsimos Lapides Ar－ tificiales in Pulueresfubtilifsimos Conteramus．Denique quod cum $\omega$ notatum videtis，Vafculum eft，Myfteriorum Phenifsimum：\＆ab ipfa Vltima Alphabeti Greci litera，（ad fuam primam inftitutam Myftagogiam nunc reftituta）vel fola partium manifefta Metathefi locali difcrepās：ex duo－ bus $\&$ illaquoque conftante Semicirculis．De Vulgatibus praterea Neceflarijs Vaforum，tum figuris，tum（vnde fieti debent）Materijs，non eft neceffe hoc loco，vt verba facia， mus．Hoctamen erit confiderandüm，$\alpha$, fui Muneris ob－ eundi captare Occafionem，ex Secretifsimo breuifsimoque

 expeditiffimum eliciet Primordiale Specimen ：Interim dā Svatiliora Praparandi，artificiofior illis innotefat Via．At in $\lambda$ ，virreo（In precipui fui officij functione；）Aër omnis externus，Ventufúe damnum adferret magnum．
$\omega$, autem， O м M I vm eft HORARVM Homo． по́ргган．
 mos\＆faluberrimós Fructuse：vel ex iffarum（dico）dua－ sum tantum literarum enafcentes Mytterio ？Quorum ali quosquafiin feculo videndos，propius aliquabtalume noftris

GIYPHICA．
22
pitcitatis primaze．Qisille Aequinotialisno－ fter．Quis in caufafuit，quòd SOL EXALTARIpo－ terac Svpra vvigarem syvi gradvaice－ teraǵue priora，perplura，SECVNDIS SAPIENTIO－ RIBVSPERCVRREREMEDITATIONIBVS．SCd nos ad alia nunc properantes，digito tantùm alijs iterindi－ eare，（cui infiltcre debeant）non amicè folùm，fed ctiam fi－ deliffimè voluimus：Myfteriorum（vt diximus）aliorum ta－ centes tamen infinitatem Confpicuam．

## THEOR．XXII．

NOndumnoftrx Mon A is effe cxhaufta Myfterizfa－ cilè liquebit．Si fecretiora quedam $A_{\text {rtis }} S_{A N-}$ craz Vafa（omnino Cabaliftica illa quidem）Solis Initia－ tuis Reuelandajex eiufdem Monadis officina cautè de－ fumpta，Veftrx SerenitatiRegix，nuncexhibuerim fpeetan－ da．OMNI ergo $N E X$ y noftrx MONAD I SSapien－ ter $\mathrm{D}_{1}$ \＆ $\mathrm{s} 0 . \mathrm{L} \mathrm{V}$ т o，fingulis partibus（diftinctionis gratia） literales addamus Notas ：prout hic factum videtis． Monemus ergo，$\alpha_{2}$ ， effe Vas quoddà Artificiale，ex A \＆ B：cum（vrifque communi，\＆iam Manifertādo $S_{\text {E－}}$ MIDIAMETRO） ipf quidem $M$ ，fa ctum： $\mathrm{Et}, \mathrm{ab}$ Al－ phabeti Gręci，Pri ma，hac litera，fola partií locali Me－ zathe $\mathrm{fl}_{2}$ diuerfum：


> GLTPHICA.

23
noftris HEspexidvuhoreis）adducemus：Nihil， extra noffram MO NA D E 4 ，in mediü ferentes．Ipfa enim qux in Alpha apparet Recta Linea，omologa illi eft，ex po－ ftremx Anatomix，Crucis parte ea，qux Litera M，nota－ tur：reliqua eciam，inde patêre poteft vnde huc veniant．


His paucis，tales me fcio non apopuì，folū，fed Aprdixes dare illis，quibus Igneus intus vigetglifitque Vigor，\＆cx－ Ieftis Origo ：vt facilè iam magno b）emocrito aurempra－




MONAS HAERO-




THEOR. XXIII.
SYmmetrias, iam, in noftre M on A dis Conftructione Hieroglyphica,à nobis obferuatas: \& ab illis, quiin Ap nulis, , igillisúe eandem geftare, vel aliter habere,gratu erir, obferuandas:accuratè annotatas hic exhibemus. In Nomine Iesv Christi, pro nobis Crvciaffixi (chius Spiritus celeriter haxc per me Scribentis, Calamum tantùm, effe Me, \& Opto, \& Spero.) ExEle е е е п тоR v a noftra $C$ ह v $C$ e,omnes iftas nunc petemus Menfuras. Vel hac quidem (iuxta PROPOSITI-ARGVMENti materiampratione: Quòdfub Cælo Lvnae, quidquid fux Generationis capit Exordiü, vel ex Q y a y vor Elementis eft coagmentatum:vel Elementaris ipfa quidem eft EsSENT1A: Idq́ue modis varijs,non Vulgariter cognitis. Et quia in nulla re Creata, Elementa ipfa, in Aequ*lifunt Proportione, vel virture:Arte tamen adAequalitaté, in quiburdam(vt Sophi norunt)rebus, redaci poffunt: in C r v ce noftra, Aequales \& non Aequales conftituimus partes. Quod,alia rationc,Idem \& Diuerfium:fiue Vnum \& Plura, nominare poffumus: $C_{R}$ VCisæquilatere, (vtfit pra monuimus) in Secreto, admittentes Proprietarem. At, Si spmmetriar vm híc pofitarum, rationes (quas tenemus) fingulas, in medium adduceremus: velaliter, quìm (Sapientibus) abundè fatis,per totum fecimus opulculum, demonftraremus caulas: Propofiri noftri, Limites, nobis, baud temerè proffriptos, tranfilifemus.
ACcepto, in plano, Puncto aliquo: Veluri A: per idem, vtring; ducatur Reffa fatis longa:que fit $\mathrm{C}, \mathrm{A}, \mathrm{K} . \&$ fupgr lineam K, $\mathrm{C}_{2}$ à Puncto $A_{2}$ erigatur Perpendicularis ; Verin-

GEYPHICK:
24
que, ad inficientem producta Logitudinem (in Infinitum, tolent dicere Geometre; bene, incommoda pracauentes) Qine admittatur effe D A E. Iam in A K: accipiarur Punctum, wi libet:\& fit B. Habita primùm nunc $\hat{A}, B$, (noftri fcilicet operis cómuni Menfura) huius, Tripla capiatur, ab A verfus $\mathrm{C}: ~ \& ~ p o n a t u r$ effe A.C.Ipfius AB,Du pla tat AE. Et Duph ipfrus A B, fit A D. Ita quòd tota $D E$,fitipfius A B, Quadrupla. Sicergo noftran Czvcem Elimentalem cö fecimus. Ex $A \cdot B, A C$ AD, \& A E.Linearum Scilicet evatemenR10. Nanc, ex BK;refecetur recta,equalis ipfi A D: \& fit BI. Centro I, \& Interuallo I B, defcribatur Circulus; quifir BR: fecans rectã AKin pücto R.A'puncto $R$, verfus $K$, refcinda tur recta xqualis ipfi A B; \& fit R K.Ad punctú
 K , educaturvtrinque, (adangulos rectos, cum ipfa A K) Sufficientis longirudinis linearecta:qua fit P,K,E, Ab iplo K , puncto, verfus F , refecetur reita, ipfi A $D$ xqualis : Et fit K, F. Centro deinde K, \& Interuallo K F: defcribanur Sen micirculus F, I, P, ita quod F, K, P, fit eiufdem Diameter. Tandem adpunctum C, ipfirectra A, C, ducatur Perpendicularişvtionque, ad longitudinemfufficientem extenf;

## MONAS: HIERO-

$\&$ fit $O, C, Q$. Pofteàeex linea $C, O, \&$ ad puncturn $C$, act cipiatur Retta, xqualis A, B, linex: Et fit C, M. Centro M, \& intertitio M, C , defcribatur Semicirculus $\mathrm{C}, \mathrm{H}, \mathrm{O}$, cuius Diameter fit. $\mathrm{C}, \mathrm{M}, \mathrm{O}$. Et fimili denique ratione, ex $\mathrm{C}, \mathrm{Q}$, recta, \& ad Punctum C, refecetur linea xqualis ipfi A, B; \& fit $\mathrm{C}, \mathrm{N}$. Centro igitur N, \& longitudine N, C, fiat Semicirculus, C, G, Q:Cuius, CNQ fit Diameter. Iam Afferimus requifitas omnes, in noftra MO NADE, SYNMETRIAS, explicatas, defcriptasq́ue effe.

Monere tamen Mechanicum libet: $\mathrm{C}, \mathrm{K}$, totam lineam, nouem effe talium partium, qualiú, noftra FV NDAMENra i is, A B, vna eft. Vndealia via, ille ad hoc idem opus abloluendū accedere poteft. Deindé Diametros, Semidiametrosqúue omnes, obfcuris hic (vt loquuntur Mechanici) lineis delignari debere. Nec vllumvifibile relinquendum Centavm: excepto Centro Solari: quod, hic, litera I, notarum videt. Literasq́ue adiungédas nullas. Tum ad Ornatum,(non Neceffitaterm aliquam Myfficam à nopis eara tione, iam confiderandá ) Peripherix Solari, Latitudinen Superficialem (intrinfecus parallelo vno defcripto) Mecha nicus adijcere poteft. (Parallelorum vero diftätia, per quart, tam quintámue partem, A, B, velcirciter, fieri poteft.) Lunari autem, illam tribucre Speciem, qua folet Prima, poft fuā cum Sole Coniunctionem, in Cæł Apparere: videlicet Corniculataadmodum. Quodfier, fià $K$ puncto, verfus $R$, accipiarurilla, (quam diximus) Quarta; quintáue pars linex $A, B: \&$ fuper eius linex fine, tanquam Centro, Semidiametro vera Lunari, trahatur ifta fecunda Peripherix pars;': ad vtrunque prioris Semicirculi contactum nitidum Simite quid ad $M ; \& N$;puncta, fieri poteft: erectis Ji Perpendicularibusin quibus pars; ipfins $A B_{5}$, fexta, vel minor accipiatur: vbi, facto Centro, prioribusautem $M$, $\mathrm{C}_{2} \& \mathrm{~N}_{2} \mathrm{C}_{2}$ Semidiamerris ducâtur extrinecus, illifecundi,
quafi Semicirculi. Per iplas denique, noftra Crucis Rectas, vtrinq; poffunt Parallelx protrahijà medijs per octauam, vel decimam partě ipfius A, B, diftantes: Itave noftra Crvx, ex evatvor Superficiebus, quafi Lincarib", ea ratione cōficiatur:quarum latitudo, fit quarta vel quinta pars ipfius AB,rectw. Hxc Ornamenta, appofita figura, voluialiquo modo adumbrare. Qux omnia, vnufquifque, pro fuiani mi fententia,facere po-
 teft: modò interea, noftris Myfticis SymmeTRIIS, nulla (vel minima)inferatur Iniuria: Ne, ea quidem negligentia,temporis tandem progreffu, verarum iftarum (\& maximè neceffariarum) Commenfurationū Hicroglyphicarum perturbetur, perearúe Difciplina noua : longè amplior Maiorq́ue quàm hoclibello, eandem vel poiuimus, vel voluimns quidem explicare. Vt Temporis Filia, Deinvty, docebitVeritas.
$A^{T}$, qux cuinis effe obuia polfunt, in iftis noftrx Mo: AI I s Symmerrijs fefe exercenti, Methodicè iam quxdä, ob ocnlos ponemus. Primùm quidem ordientes, à noffre CrvcisLincarum Quaternario:eo habitore-


G re,quis

MONAS HIERO-
re,guis poteft. Deinde de Earundem linearum Quay enNAsio:proüt peculiayem, Mŷfticamq́ue, alio modo, habēt partirionem, \& rationem. Tertio, Numeris, quos vel ifto loco, vel ex alijs, per totū libellum, Theorijs, artificiosè elicuimus, vtilia quadam à Deo in Natvra, effe deftinata Officia, nonnullis monftrabimus exemplis :aliaq́ue opportunis inferemus locis: qux fructum haud exiguum ferent, probè intellecta:hxccque breuiffimè abfoluemus.


Nofter Metathefoos Canion.
"NAturali ordine, à Prima Monade, defcriptis quotcung; Numeris:Sia Primo ad Vltimum, fiat Continuata mul"tiplicario:vt, Primi in Secundum:produti in Tertium: il-
 $\approx$ Productum viltimum,omnem Poffibile Metathefim in illis ntot locis, determinat. Pariqueratione, in quibufcunque, tot >diuerfis rebus: Hancego Operationem, tibi (O REX) plarimùm Commendo:tum in omni Naturx examinatione, tum in alijs Reipub.Negotijs vtiliffimá. hac ego in Hebræorum Tziruph(fue Thmura) cum maxima volupiate, vii foieo.

QYA-



EXiftis Schematibus,plura elici poffunt: (fi penutiusconGiderentur)quàm apertis par eft proferre verbis.Hoc tamen pra ceteris monemus lingulare vnum, (à nobis etiam Primis vnà cum tota hac noua euulgatum arte) Rationem hícin medio effe pofitam, ob quam, Q VATERNARIVS, velDenarivs, Numerationibusfinem imponit quendam: eamq́ue caufam quam attulere Maiores noftri, non fuiffè abfolutam, exactamq́ue afferimus : fed iftam, quam nuic narrabimus.

Poftquamifta $\mathrm{Monas}, \ell$ ef fibiintegrè pleneque Phyficéque Reftitura, (tum - quidem eft MoNA $s, v$ nitissima, Magorum queiudicataVmitas) neq; in Natvrae, neque viliusaryis eft potefatẹ, EANDEM SAEPIVS QVAM QVATER, per Supercaleftes Reuolutiones, ad Progreffum vilum, Mo o$\tau \mathrm{V} \triangle \mathrm{V}=$ faciendum impellere: (Acinde progignitur Ille,

MONAS HIERO-
" quem nos,ob eminétiam fuam, fic notari volumus,) Y "Idqúue ea de caufa, quòd nec in Elementali mundo, mnec Calefti, nec Svpexcaelesti, fitaliqua $\dot{\text { p }}$ „Potctas, Creatainflventialis: Qua, $\approx$ tunc, non fueritabfolutiffimè Ditata \& Dotata.

Cuius, hunc verum Effectum, Q y a t vo r fimul(olim) Philofcphantes Clariffimi Viri, Opere funt confecuti:Vnde, diu, Maximo Rei MiraculoAttoniti, Tandem ad Dei Opt.Max. Canendas,predicandasque Laudes, fe totos, deincepsconuertebant: Qui, ea ratione, illis, tantam Sapientiam, \& fuper Creat vas acteras, Potentiam, Imperiumq́que fuiffet Largitus ampliffimum.

## THEOR, XXIIII.

VT, noffrum huius Libelli Exordiī, à Puncto,Recta, Circulocque Cœpinus: Sicq́ue ex noftro Mona it ico pyNcto, linearem noftrofúElementorvag Effuxionem Extremam, in Circulum Circumduximus, 1. Analogum ferè, ipfi Aequinoctiali;qui Horis 24 , fuă Conficit Circuitionem: It a, nunctandem, $Q$ vaternaris OMNIMODAMMETATHESIM; (Numero definitam,
2.24.) $M E T A M O R P H O S I M^{\prime} Q V E$, hac noftra Vigefima Qvarta Confummabimus, Terminabimusque Theotia: Ad Honorem, Glortam'Que eius: Qyr, (Tefte, Myfteriorum Diuinorum Archiprefule, Ioanne: in Quaris Apocalypfeos Capitis, parte Qivarta, vitimávo ejim Throno Seder.In Cuius Medio cir-
 $S_{E} \times$ habenria) Sine requie, $\mathrm{D}_{\text {IE }} \mathbb{C} \mathrm{N}_{\mathrm{C}} \mathcal{C T}_{\mathrm{T}}$, dicunt: Sanctus, Sanctus, Sanctus Dominus Deus Omnipotens:
 4. ctiam, ex 24 Sedilibus, in CIRCVIT ${ }^{2}$ pofitis, $S_{\text {ENI }}$ IO-5-xis 24 , procidentes (Averiss vis ABIECTIS corenis).

GITPHICA.
coronis) adorant; dicentes: Dignuses Domine accipere Gloriam\& Honorem, \& Viatv-
tem: Quia, ty, Criastiomita:
Et propter Volveratemtvak
synt: etcheatasynt.
AMEN, DICIT
LitinA CMARA,
$\Delta$ :
Cui, Dev s, Voluntatem Ha_
bilitatemque dedit, Diuinums
boc Myfterium,eternis Sic con fignare Literarkm Monimentis: Laboresóg hoface Suos, plaw cidijJime abfolure, Lanuan' 25 : dieciufdem. 13 , 7 nchoatos: eAn.1564. Annwerpic.


Vulgaris, Hic, Oculus Cancoasit, Difideteys

## plurimùm.

## Antivepiaz:

 GRAPKYS: PRIDII CALEND. APRIIIS. AN. Ig64


## Monas Hieroglyphica



Translation by Jim Egan
with guidance from translations done by
Scott Barker in 2008,
C.H. Josten in 1964,
W.L. Hamilton-Jones in 1946, and Anonymous in 1691

## NOTES ABOUT THIS TRANSLATION

1. The words written in a [small typesize and enclosed in brackets] indicate my clarifying comments and sometimes Dee's original Latin word.
2. All the parentheses (and the words they contain) are Dee's parentheses.
3. The words which Dee wrote in Greek have been highlighted with italics or in some cases with regular type.
4. The placement of marginalia follows Dee's original text (including the numerals and quotation marks that Dee used for emphasis) .
5. Previous translations have ignored Dee's many capitalizations. As they are expressions of emphasis, I have forrowed Dee's styling.
6. I have used Arabic numerals instead of Roman numerals make it easier to keep track of the 24 Theorems. However, the use of the word "Theorems" for Theorems 1-4, and "Theor." for Theorems 5-24, follows Dee's original styling (because its a clue).
7. I have included the 3 large decorative letters ( $\mathrm{Q}, \mathrm{V}$, and P ), which begin each of the three sections of the book because they are so graphic (and because they are clues). However, the "first letters" of each of the translated Theorems (also clues) are not necessarily the "first letters" of each of Dee's original Latin Theorems, so I did not capitalize them.
8. Dee used rather long sentences and paragraphs. For easier reading I have made shorter sentences, more frequent paragraphs, and have left space between the paragraphs.
9. Even though this English version is easier for most people to read, many "letter" and "word" clues in the text and illustrations are "lost in translation." Be sure to study the primary source, Dee's original Latin text, for these subtle clues.
10. To simplify, I have deleted the headers, the printer's pagination letters (at bottom of recto pages), and the "carry-over" words (at the very end of each page). I have kept Dee's page numbers and also added the corresponding "verso" page numbers ("opposite side"), so the pages can be referred to more easily.

This translation was done by Jim Egan, with assistance from Scott Barker. © 2009 Jim Egan
It is based on original 1564 Latin text, but in addition, these three previous translations were consulted:
Anonymous, (1691), Ferguson collection MS 21, Glasgow University Library, Glasgow
J. W. Hamilton- Jones (1947), Red Wheel/Weiser, York Beach, ME (1975 and 2000),
C.H. Josten, (1964), AMBIX Vol. XII, No. 2 \& 3, London

# TO THE MOST EXCELLENT MAJESTY <br> OF THE REKNOWNED KING <br> MAXIMILIAN 

JOHN DEE OF LONDON<br>Wishes a Very Fruitful Reign



The two causes which were able to encourage a Man of my Circumstances to present so small a gift to so great a KING have now impelled me to do so.

This gift is so extremely rare and of great goodness that the warm feelings I have for your Majesty should not be held in contempt, even though it is so small in size.

Your wondrous virtues have raised and procured an eternal Benevolence towards you. Your virtues are so great that even those who have not witnessed them in person believe, without a doubt, the extraordinary, yet quite true, reports of others.

Yet even those who have witnessed them in person and have carefully and keenly contemplated them, are still at a loss for words to fully describe the extent of these virtues.

As an eyewitness myself, I understand this very clearly, as I was in Posonium in your Kingdom of Hungaria last September [Dee attended his coronation as King of Hungary].

Allow me to speak about the Rarity of this Gift (small indeed in size) in as few words as possible. Using the full effort of my mind, I have concluded that the course of a Human life must be considered as two distinct parts (and most people live long enough to experience the second part).

2 verso

After Infancy and Puberty, the Adolescent is faced with a mind challenging choice: What type of life path to follow. After hesitating for a while, they must finally Decide between Two possible paths.

Some, (who have fallen in love with truth and virtue), for the rest of their lives, will devote all their energy to Philosophy. Others (ensnared by worldly allurements or burning with a desire for riches) work anxiously in many ways, in order to lead a luxurious life of profit and pleasure.

You can readily find a thousand examples of this type. Yet of the other type (that is, those who sincerely apply themselves to Philosophy), you can hardly find one who has even begun to examine the true foundations of Nature.

Even of those scholars who have entirely devoted 2. themselves to the study of wisdom, the Republic of Letters can hardly bring forth one of a Thousand who have searched deeply into the Causes of Celestial powers and Actions as well as the Beginnings, the middle States, and the Endings of Things.

What should we then say of someone who, having 3. surmounted all these challenges, further aspires to the investigation and understanding of Supercelestial virtues and Metaphysical influences?

Where on the whole Orb of the Earth (and in these our sorry times) can such a Magnanimous and probably UNIQUE HERO be found?

Following our one-in-a-thousand Proportion (which was not rashly conceived), WE OUGHT TO EXPECT THAT THIS UNIQUE AND MOST FORTUITOUS SPECIMEN IS ONE-IN-A-MILLION AMONG PHILOSOPHERS, OR ONE-IN-A THOUSAND MILLION MEN OF THE COMMON SORT.

To demonstrate this RARITY, we present this HIEROGLYPHIC figure of a letter (called) Pythagorean. If your Excellency studies it with great attention, still greater Mysteries will present themselves (for your consideration), shown, in this way, from our COSMOPOLITICAL Theories.


Now, in what degree of this Three-level (Philosophical) Rarity I wish this my gift of mine to be, and to be esteemed, you (most Merciful KING), who excels and abounds in knowledge of the greatest Arts and most Secret Things, may easily conjecture.

## 3 verso

But even if I place it in the lowest and first degree of 1. Philosophizing, I think I shall not be acting in an arrogant manner. Raising our Heads higher above the ground, I can confidently Promise Your Highness even richer fruits than this Degree of EXCELLENCE.

My gift is endowed with a rareness because it is woven 2. together with a manner of writing, right up to the last thread, which up to this day, as far as I have heard or gathered from the written Monuments of our forefathers, no work has ever been composed.

Even though I call it Hieroglyphic, he who has exam- 3. ined it closely will confess that a sort of mathematical light and strength is exists in it, which is even rarer in such rare things.

Or is it not a Rare thing, I ask, that the Common As tronomical Symbols of the planets (instead of being Dead, or Dumb, or, up until now, Barbaric marks) are now imbued with Immortal Life, able to express their special meaning Eloquently to those of every Language or Nationality.

Another great rareness has also been added, that is, 5. the external bodies [of the Astronomical Symbols] have now been brought back and restored to their Mystical Symmetries (by the best hieroglyphical arguments). It's as if, in an age long past, they were depicted like this or as if our forefathers had wished than in the future they would be made this way.

The new and successful way we have depicted the signs 6. of the twelve divisions of the ecliptic is as rare as it is completely novel.

And indeed, the Rarest thing is that all this is embod- 7. ied in One Unique Hieroglyphic Symbol, that is, MERCURY (fortified by a Sharp Point).

Truly, Mercury is properly called the rebuilder and restorer of our whole Astronomy. He is the Messenger of our IEOVAE [Jehovah], sent so that we might be founders of a NEW discipline of this Sacred Art of Writing, or with this aid, renew one that was extinct and had been wholly wiped out of mankind's memory.

We have done this in a way that all these Hieroglyphical Interpretations show themselves most gently and of their own accord. Nothing is forced and nothing inappropriate, as it were, can be seen throughout this whole Little Book.
8.

We seal those things we have just discussed (and things far greater yet to come) with our HERMETIC SEAL of LONDON declaring that there is not one superfluous point included and (even more significantly) that there is not one point missing. Everyone, especially those who profess to be serious investigators of philosophy and wisdom will be forced to authenticate the great Rarity of this work (for the everlasting memory of mankind).

Grammarians will have to Admit to this rarity when 1. they see that there are specific reasons for the shapes of Letters, their Positions or Places in the Order of the Alphabet, how they are Bound together, their Numerical Value, and many other things (that must be considered with regards to the Primary Alphabets of the Three Languages).

Furthermore, it is a Rare Grammarian who can Defend the idea that Grammar is ONE Science WHICH can be learned from ONE Man.

## 4 verso

In my 1557
narrative on the Englishman Roger Bacon entitled A Mirror of Unity.

Such a Man we have previously shown to be the Most Rare on Earth [that is, the one-in-a-thousand million Adept], when we wrote a Narrative about him. It appears to be that there are so many great Mysteries (of the Art of Grammar and things drawn forth about such Mysteries with the aid of the Art of Grammar) which have solid Foundations in the Sacred Scriptures of GOD ALMIGHTY, that even in a large Book I could not furnish all the explanations; nor indeed does that seem to be required Here.

Nor should you, O Glorious King of the Romans, be surprised that I mention in passing that Alphabetic Lettering contains such great Mysteries. For HE, who is the SOLE Author of all Mysteries, has compared HIMSELF to the first letter and the last Letter (which is to be understood not only in the Greek language, but also in Hebrew and Latin, as can be demonstrated in various ways in this Art). Oh how great, then, must be Mysteries of the Intermediate Letters? It is not surprising that such Mysteries are found in Letters, for all things visible and INVISIBLE, manifest or hidden (by either Nature or Art), emanating from God himself, are to be most diligently explored in our investigations, so we may proclaim and celebrate his GOODNESS, WISDOM, and POWER.

Thus Saint Paul taught that MANKIND would have no good excuse [for not proclaiming the Wisdom of God] even if it had no written testament other than his Creatures, which were made from GOD'S own finger during the CREATION. I would not be so demanding as to require these things of all Grammarians.
But to those who labor to find out the hidden Mysteries of things, witness that (by our MONAD) we have demonstrated a RARE Example [Exemplum] of this Kind.

We admonish them, as friends, that, the first Mystical letters of Hebrew, Greek, and Latin were issued by God alone and handed down to Mortals.

Furthermore, (despite what may be the custom of human arrogance to boast) the shapes of all those letters derive from points, straight lines, and circumferences of circles (by wonderful and most wise artfulness). The eternal wisdom of our Heavenly Father has taught us that the whole sense of the Mosaic Law [Laws of Moses] is to be considered, even to the fulfillment of every Jot and Tittle. The ultimate consideration and Analysis of these Laws is the IOD and Chireck (from which all the Hebrew letters and vowels arise).

> ALTHOUGH THE ONENESS OF THE POINT OF A CHIRECK REMAINS MOTIONLESS AT THE APEX, it is still not contrary of us to embrace a trinity of consubstantial monads, which appear to the ONENESS OF THE IOD ITSELF; THAT TRINITY BEING FORMED FROM ONE STRAIGHT LINE AND TWO DIFFERENT PARTS OF THE CIRCUMFERENCE.
> The analysis reveals quite clearly that The First Humans could never have devised a work as Amazing as the Hebrew Letters and Nekudoth [vowel accent marks] without the Presence and Inspiration of Divine Power.
> Even if these are the least of subjects, which are considered by Vulgar Grammarians, when the Wise properly consider how, and by what wonderful artfulness, they lend themselves to the generation of all the Letters and the Nekudoth, they will learn very many wondrous things (by perfect Spiritual Enlightenment).

## 5 verso

Let us dismiss those Philosophers of Letters and Language and bring in my fellow MATHEMATICIANS honest Witnesses of the Rareness of this our Gift.
2. Will not the ARITHMETICIANS (and I don't say LOGICIAN) - who treats Numbers as Abstract Bodies, far from being perceived by the senses; who subjects them to various Mental Processes and hides them in the depths of Intellectual Reasoning - will he not be astonished to see, in this our Work, that his numbers are shown to be Concrete and Corporeal, and that their Souls and Lives as Forms are separated from them, so that they may be of service to us?

Will he not be surprised to see such wonderful Off- 2. spring of the MONAD, to which no Other Unit or Numbers need to be added, and which do not need to be Multiplied by any numbers they do not already contain?

Or by first contemplating Carefully Prepared operations of Division and Equation (as this Art prescribes)?

Will he not be filled with the greatest admiration by this most subtle, yet General Evaluating Rule: that the strength 3. and intrinsic VALUE of the ONE THING, purported by others to be Chaos, is primarily explained (beyond any Arithmetical Doubt) by the Number TEN?
3. The GEOMETER (my King) will begin to feel embarrassed, and feel that the very Principles of his Art are insufficiently established (which is quite strange) when he understands what here is Secretly whispered and Intimated: By the SQUARE Mystery of this Hieroglyphic MONAD something CIRCULAR, and wholly Equal, is being conveyed.

Also that the TOILS of Archimedes may be compensated by a most excellent Reward, even though he never solved this Problem. In matters this Great, it is Enough to have had the Intention.

And won't the MUSICIAN be rightfully astonished when here he will be able to perceive inexplicable, celestial HARMONIES without any motion or sound?

And won't the ASTRONOMER regret all his sleepless vigils and cold labors he has suffered under the Open Sky, when here, without any Discomfort from the Air, Under his own roof, with windows and Doors Shut on all sides, at any given Time, he is able to observe the movements of the heavenly bodies? And, indeed, without any Mechanical Instruments made from Wood or Brass?

And won't the OPTICIAN condemn the Senselessness of his Ingenious work, laboring in all sorts of ways to make a Mirror according to a Line (appropriately curved in a circle) of a Parabolic Section of a Cone, which will attack any Matter (able to be burned by fire) with the incredible Heat from the Rays of the Sun. Yet here a Line is presented, resulting from a Three-Cornered Section of the Tetrahedron, from which, when Made Full-Circle, a Mirror may be found that (even when the Sun is being blocked by Clouds) can reduce any kind of Stones or Metal into Impalpable Powders by the force of (truly the very strongest) Heat.

And will not be, who has devoted all the Time of his life to making exacting measurements with WEIGHTS, judge just how well his Labors and costs have been invested, when here, the Magistery of our MONAD will teach him, most assuredly by actual Experience, that the Element of Earth can float above that of Water?
8. their findings regarding PLENUM, occupied by matter, and VOID, empty of matter, (a subject that has been controversial since Philosophy was in its Infancy). They have seen that the Surfaces of Elements, which are in close proximity are coordinated, connected, and Joined Together by a Law (decreed by God Almighty) and Bond (practically Unable to be Loosened) of Nature. They can most assuredly demonstrate to people that Fire, Air, and Water can be pulled or pushed, upwards or downwards, This Way or That Way (or in any direction they desire) in miraculous ways by various Inventions (which are useful to the Republic, as demonstrated by the Whole Art of Hydraulics and Heron's Feats of Magic [Thaumopoetica], as we nowadays like to call them.)

But no one of that Profession can claim to have made a Machine, which could raise the Element of Earth Upwards, through Water, and into Fire. However, the Theorems in our MONAD demonstrate that this is possible.

O most wise King, may you Store these things in the most Secret Treasures of your Mind and Memory.
see that Gematria [certain letters represent certain numbers] Notariacon [first letters of a phrase combine to spell a new word, similar to an acronym] and Tzyruph [certain letters, jumbled, form different words] (the names of the 3 principal Keys to this Art) are used here, outside the confines of the Language, which is called Holy. Also, he will now see that the Symbols and Characters of that Mystical Tradition (which was received from God) entirely corroborated here (from the obvious, which is sometimes visible and sometimes invisible) then he will call this Art SACRED as well. Furthermore, (compelled by Truth, if he should understand) he will acknowledge, the same Most Benevolent GOD is not only the God of the Jews, but of all Peoples, Nations, and Languages,
regardless of boundaries, and that no Mortal may Excuse himselffor his Ignorance of this our Holy Language.

In my Aphorisms delivered to the Parisians, I called this language the KABBALAH OF THE REAL, on the Kabbalah of Being. I call the other Kabbalah, the vulgar one, which utilizes well-known Letters, which are Written by Man The GRAMMATICAL Kabbalah or the Kabbalah of Saying.

The KABBALAH OF THE REAL, born to us by the Law of Creation, (as Saint Paul intimates) is more Divine, as it allows for the Discovery of New Arts and faithfully Explains even The most Difficult to understand Arts. Following our Example, others may see how it applies to other Arts.

I know well (O KING) that you will not be horrified if I offer this MAGIC Parable in your Royal Presence. Our Hieroglyphic MONAS possesses, at its Innermost Center, a Terrestrial Body. The MONAS explains, without Words, how that Terrestrial Body is ACTUATED. When ACTUATED, the Terrestrial Body is UNITED (in a perpetual Marriage) to a Generative Influence, which is Lunar and Solar. Previous to this, in Heaven or elsewhere, the Lunar and Solar influences were QUITE SEPARATED from the Terrestrial Body.

When (by God's will) this Marriage has been made (which I interpreted for the Parisians as Tes games aîan, that is, the Earthly Marriage, the terrestrial image joining with influences from above), the Monad can no longer be nourished or watered on its Native Earth until the FOURTH great, and truly Metaphysical Revolution has been Completed. When this Advance has been made, he who nourished the MONAD will First Go Away into a METAMORPHOSIS, and afterwards, will very rarely be seen by the eyes of Mortals.

This, $O$ Great King, is the true INVISIBILITY of the MAGI, which has been sung about over and over again (and without Sin), and which (as all Future Magi will discover) has been granted to the Therems of our MONAD.

The most expert PHYSICIANS will most easily
11. learn from these same Theorems about Hippocrates' Mystical intent. For he will know WHAT IS TO BE ADDED

Liber de Flatibus
[meaning
"Book of Breathing"] OR TAKEN AWAY. He will Gladly acknowledge that this Same Art of Medicine is contained in the short Compendium of our MONAS.

The SCRYER ["Beryllisticvs" or crystal-ball gazer] may
12. see most accurately in a Crystal Lamin [thin plate used in scrying] all SUBLUNARY things that are of Earth or Water. And in a Carbuncle or Ruby he can explore the Region of Air and Fire.

And if the $21^{\text {st }}$ Theorem of our Hieroglyphic
13. MONAD can satisfy a REFINER OF GOLD ["Voarchadvmico"] and give him ENLIGHTENMENT ["Voarh beth адумотн" as a subjet of speculation, he will admit that he need not travel to India or America for the sake of Philosophizing.

And finally, (using whatever ALCHEMY ["Ari-
14. отол"। can provide or promise, gleaned from 20 Years of hard work in The Hermetic Art), we have written on the subject of the ADEPT in a treatise to the Parisians, with its own particular MONAD (illustrated with Conclusive Mystical Evidence). Nevertheless, we assure your Royal Majesty that with ALL THIS VERY evidence, so carefully presented, in this our Spiritual Hieroglyphic MONAD, that no other Similar Example could express it to mankind any better way.

It must doubly turn into itself. Namely: to Assimilate the Dignified Work and to Imitate its Worthiness. You may now Agree, O King Maximilian, (famous for the Honor of his Three-fold Crown) that I have said enough (Indeed, I fear, more than enough if Vulgar men were listening) of the Rarity of this our Theoretical Gift, whose Quality is defined by its own limits.

It is enough ( $O$ to the singular Glory of all Kings) that While we have carefully demonstrated that this Gift is so rare, let No Aesopian bird (not even the most Envious Mischievous Tongue) mutter [disapprovingly] about it.

The most Modest and Wisest Philosophers will agree that this work is far from deserving the Indignity of False Accusations. For They will not disdain to provide, with me, Praise and Honor, to that Phoenix. From the Wings of its Lone Mercy, we have plucked, with both Fear and Love, all those extremely Rare Theoretical Feathers against our Nakedness brought on by Adam. May we much more Cheerfully resist all the sharp coldness of Ignorance, and hide the Shame of our Errors from the Philosopher's eyes, while striving for the honest TRUTH.

And although we have not, in Any Way, relied here on any human Authority, if something said or written by an Ancient Philosopher can be opportunely illustrated by our Light, then we have not refused to deliver this advantage to our Descendants.

In our Hieroglyphic Demonstrations we descend into certain Mysteries of Hermes, Ostanes, Pythagoras, Democitus and Anaxagoras, but not simply for the purpose of seeking confirmation of our own tenets in them.

## 8 verso

This great Rarity is so well joined with such Excellent Quality that Nothing, WE PROTEST, has been placed by us in this little book, either openly or covertly, that is not Honest, Sincere, in accord with Human Dignity, and extremely Useful in the pursuit of perfect Piety and true Religion.

Such steep, difficult to reach Mysteries can only RIGHTLY[оRтнотомеIn] be judged by someone who sees their whole Amplitude.

For no one would betray his Childishness, Maliciousness, and Arrogance faster than he who would dare to Condemn as Impious, or Reject as frivolous, any of the things which we have Commended to Your Wisdom.

And in this regard, nobody could produce a witness that was Sharper in judgment, More Experienced in Practices, more powerful in authority, or more Faithful in Sincerity than the Greatest, Omnipotent King of Kings has made King MAXIMILIAN. Therefore, Your August Majesty will stand as a witness for me above all others.

The fact that our work has been Approved and Ratified [by your Majesty] will not only stop the mouths of many Wicked Grammaticasters but it will excite the minds of many Philosophers who are dejected, or Lying around Idly, by the Alleged Uncertainty of such great Mysteries. On account of the Rarity of such Things, they might be fearful of the Arrogant Judgments of the Ignorant - those who are wont to condemn Good Studies and Bad Studies alike (blindly and indiscriminately, as their usual names have a Resemblance), resulting in the most deplorable destruction (sometimes) of the Best of books.

It can clearly be seen that both [types of philosophers, the uncertain and the fearfull have, at various times, done great harm to the Christian Republic.

Their minds undoubtedly had the capacity to undertake such great matters, but they were completely terrified, for reasons previously mentioned; Or perhaps because Ignorant Judges had Rudely and Arrogantly condemned their whole study of such noble and divine Mysteries, they made only mediocre Progress.

But this is not the place to compare all the Honest Sciences with their false rivals, which are indeed Shadowy, Hateful, Troublesome, Harmful to Human Society.

Solely because of the way the vulgar grasp andfollow [these false sciences], must, we say, be exploded and condemned, not only by the Judgment of the Vulgar, but by that of every wise man. And we urge that this be done diligently.

And those who do not even know these BODIES exist, or WHERE or what they may be, and of which [their false studies] are but weak shadows; How do they have the audacity; How can they justifiably condemn the non-Vulgar studies of the non-Vulgar man. LET JUSTICE BE DONE. Let each get his own due.

The Vulgar, who Pretend to have Knowledge ["sciolis," sciolists], who not only eagerly pursue the Shadows of the Great Arts, but also defile them and lie about them in a most wicked way. We might attribute this to Foolishness, Delusion, and Lack of Respect.

To bring Violence against Virtuous and Firmly Grounded Studies of those who have strong moral character and Distinguished integrity (simply because of the petty, False Accusations of the Vulgar) not only brings their Names and their studies into disrepute, but also puts their Lives in danger. This (O King) seems to me not only inhuman, but Unjust and almost Sinful.

## 9 verso

All bodies have EDGES in COMMON with their Shadows (something which Mathematicians know quite well). Similarly the WISE realize that true Bodies [of work] have Diction [word choices], in Speaking and Writing, which are in common with their shadows. While the Wiser Philosophers enjoy the Solid Teachings and pleasant benefits of the BODIES, the Ignorant, Foolhardy and Presumptuous Apes Grasp at mere SHADOWS, which are empty and Worthless.

And so indeed we see This happen. All honest and legitimate Understanding and Comprehension of Shadows must be conceded to those dealing with true Bodies, but [to the vulgar, who hold things which are] not Solid and Sincere (merely vague shadows), such things will be snatched from their hands.

RIGHTFULLY [оRтнотомEIN], it is necessary (O King) to make a clear distinction between SHADOW and BODY in order to distinguish the Limits, Strengths, and Uses of each

Luke, Chapter 8
[Luke, Chapter
8, Verse 18 reads, "Take heed then how you hear; for to him who has, will more be given, and from him who has not, even what he thinks that he has, will be taken away."]
of them.
This Divine Duty, among many others, is performed with the Royal and Imperial sword of JUSTICE.

However, with a certain Artfulness, the Wise will gladly allow the figures of SHADOWS to exist in the sinuous curves of true Bodies, lest the choicest lettuces be offered to asses rudely rushing into the Hesperian Gardens, though thistles would be good enough for them. [What Dee seems to be saying is: Shadows can be quite valuable (like lettuce) and should not simply handed over to the vulgar (asses) when the vulgar would be content with much less (thistles).]

Forgive me (O King) if (by Christ's authority) I convict the World of Injustice. "And when He has come, He will convict the world of sin, and righteousness and of judgment."

Josten points out that this is a reference to John 16:8. "And when He has come, He will convict the world of sin, and righteousness and of judgment." (New King James Version of the Bible, 1982)

Jerome's Latin Vulgate (405 AD) reads "et cum venerit ille arguet mundum de peccato et de iustitia et de iudicio." (Notice that the verb arguet (convict) is the same verb Dee uses.) (In the original Greek, the verb is elegcho, to reprove, accuse, or convict.)

Nor do I wish that this work, which I have particularly commemorated to Your Wisdom, here and in these our times, to Appear to be mere opinion or as Superfluous. But enough of these things.

Thus, I most humbly Offer to Your Serene Majesty this my offspring, the HIEROGLYPHIC MONAD, (Conceived in London, yet Born in Antwerp). I earnestly desire, with all my strength, that you do not disdain to become its Second Father. Not only now, but later in life, when it will be older and even more Valuable because of your Trust, may it always be at hand and of service to you. I wish that henceforth you will consider it your own, O Most Merciful KING. During the entire period of its birth, your pleasing face seemed to be present before my eyes. In this respect, you have made my Labors fruitful and helped me bring this work to Light.

My Mind has been pregnant with it continuously for the past 7 years, yet because of the magnetic virtue you exert, even from such a great distance, it took me only 12 days to bring it forth, most peacefully, into the world.

May the Most Holy TRINITY grant that this be a happy and auspicious event in the life of your August High-

As it appears in Aphorism 52 of our Propaedeumatic Aphorisms, printed in London, in the year 1558. ness as well as to my most passionate searchings for honest truth. This Most Holy Trinity, (founded before all time, in the Omnipotence of the Ineffable MONAD), ""Ineffable MONAD" refers to the ONE whose name is not spoken, as in the Jewish tradition of not speaking the name of GOD. $]$ which lives and reigns forever, and to whom alone all Praise, Honor, Power, and Glory always be given and sung by every Creature. AMEN.

Antwerp.
In the year 1564, January 29.

# To the Printer GULIELMO SILVIO: <br> My exceptionally good Friend. 

JOHN DEE OF LONDON<br>S. $D . \quad P$.<br>[Offers his Wishes for much Health]



You See, my Good Friend Willem, how especially I esteem the most noble Virtues of the Illustrious King MAXIMILIAN, to whom I impart, from the Shrine of my Heart, my Rarest and most distinguished Secrets. I communicate these secrets so that Others in the Circle of the World can also enjoy them, thanks to your care and diligence. (This is done in honor of the King for his extraordinary and Regal Virtues. Thus, others may learn by his example, as he not only wisely attends to the Royal Governance of Kingdoms, but is still fully learned about the Wondrous Mysteries of Philosophers and Wise Men.)

There are, therefore, two things, which I earnestly ask of you. The first is that you carefully copy (as best you can) the Various Letters, Points, Lines, Diagrams, Shapes, Numbers, and other things.

This, the Same Body to which I have given birth, perfect in every part, (BY GOD'S WILL) will not be Mutilated or Deformed due to Printer's Negligence, as it is brought forth into the Light.

[^1]In this way it will not be unworthy of a King, nor indeed unworthy of the studies and labors of the Philosophers who will frequently be examining it deep into its innermost parts.

I believe I have taken sufficient caution against that misfortune by selecting you as the Typographical Parent of this new Born child. I am certain you will take great Care to send it forth, in all ways, shining clearly, and with all of its Members Well-Composed.

The SECOND thing that I ask of you is indeed not a light matter. Make certain not to hand these Books indiscriminately to just any man. It is not that I begrudge them this, or anything better, but I suspect that bad things will result. These poor men may not be able to find their way through the Labyrinth (as they torture their minds in incredible ways while neglecting to take care of their everyday affairs).

Also, these men might persuade others to follow the same path (which will likewise be impassable). Even worse, impostors, who are but ghosts of men, may maliciously lie about its certainty, pretending that they had explored it fully. Finally, these men may boldly deny the existence of such MIGHTY WORKS OF GOD.

Based on their Presumptions, they will first rashly attack these Mysteries, then, in their Despair, they will furiously make false accusations about my Integrity.

Yet, having known you for many years, I know you will be cautious in such important business (either because of our friendship or for the Good of the Christian Commonwealth or, at least, for the Heroic Virtues of the Wise MAXIMILIAN Himself, virtues that are not found in the Common Sort of Men). I know I have not sought your Trust in Vain.

I know you will be cautious, and, because of you, all honest booksellers will be cautious as well.

Farewell.

From our Study in Antwerp In the year 1564, January 30.

## MONAS

# SACRED SYMBOL OF ONENESS <br> JOHN DEE OF LONDON <br> Mathematically, Magically, Cabalistically, and Anagogically <br> Explained To <br> MAXIMILLIAN 

Most Wise
KING
of The Romans, Bohemia, and Hungary

THEOREM 1


The very First and most Simple Representation, of not only existing things, but also things hidden in the Folds of Nature, and also in the exhibition of the Bringing Forth of Light, is made by means of a straight Line and a Circle.

## THEOREM 2

However, a Circle cannot be skillfully crafted without the Line. Likewise, the Line cannot be crafted without the Point.

Thus, Things come into being by way of the Point and a Monad. And things related to the circumference (regardless of how big they may be) cannot exist without the
 Service of the Central Point.

THEOREM 3
Thus, the Central Conspicuous Point of the HiEROGLYPHIC MONAD refers to the EARTH, around which both the Sun, as well as the MOON, and the rest of the Planets complete their Courses.

And in this gift, since the Sun possesses the greatest dignity (because of its excellence) we represent It by a Complete Circle with a Visible Center.


## 12 verso

## THEOREM 4

The Semicircle of the Moon is shown here to be Above the Circle of the Sun. Nonetheless, the Moon obeys the SUN as her Master and King.

The Moon seems to rejoice in the Sun's Shape and proximity so much that she emulates him in the Size of her Radius (at least, as it appears to the common man). Finally she longs to be imbued by the SOLAR RAYS so much that she becomes Transformed into him. Then she disappears from the Sky altogether. After a few Days she reappears as a horned-shaped figure, exactly as we have depicted her.

## THEOR. 5

And most certainly, one Day was Made out of Evening and Morning by the joining of the Lunar Half-Circle to its Solar complement.

Thus, it was on this first Day that the LIGHT of the Philosophers was made.

THEOR. 6
Here we see the SUN and the MOON resting on a Rectilinear Cross. By virtue of Hieroglyphic interpretation, this Cross is able to signify both the TERNARY and the QUATERNARY.

The TERNARY, as two straight lines and the one Copulative Point they have in Common.

The Quaternary, from 4 straight Lines forming 4 right Angles.


Each line might (for this purpose) be twice repeated. (Thus in this most secret way the Cross also shows itself to be OCTONARY. I doubt whether our Predecessors, the Magi, ever perceived it this way, but it should be especially noted.)

The magical TERNARY of the First of our Forefathers, and Wise Men consisted of BODY, SPIRIT, \& SOUL. Thus we have here manifested the Most Excellent SEPTENARY: [made from] two Straight Lines with their Common Point [ a Ternary of things], AND 4 Straight Lines separated by One Point [a Quaternary of things].

THEOR. 7
An experimenter will learn that when homogenous Parts of the Elements have been removed from their natural Habitations, they will Return to them along Straight lines.

Thus, it is not Absurd to show the Mystery of the FOUR ELEMENTS by 4 straight lines emanating from a single Point in Different Directions (where they are each resolved into single Elements).

You will particularly note, Geometers teach that a LINE IS PRODUCED BY THE FLOWING OF A POINT. In the same way, our Lines signifying the Elements are like DROPS (like physical points) that continuously Fall (as if FLOWING) in our Mechanical Magic.

## THEOR. 8

Furthermore, the Cabalistic Expansion of the QUATERNARY, using the customary Style of Enumeration (as we say, One, two, three, four) sums to the DENARY [TEN].

As Pythagoras himself used to say, $1,2,3$, \& 4 add up to ten. It is not without reason that the Oldest Latin Philosophers decided to signify the number TEN by using the Rectilinear CROSS made from 4 Straight lines (as it is the Twenty-First letter of the Roman Alphabet).

Its place might further be defined as being established when the TERNARY carries its power through the SEPTENARY.

THEOR. 9
All this agrees well with the SUN and MOON of our MONAD. By the Magic of the same 4 Elements, a Most Exact SEPARATION [SEPARATIO] has been made. Furthermore, the circumference lines of the circles, in the SOLAR compliment, form a CONJUNCTION [CONJUNCTIO] (for all lines of a given length will describe the same-sized circle, as per the laws of Geometry).

## 13 verso

Thus, it is not possible to hide how much the DENARIAN symmetry of the Cross in our MONAD usefully serves the SUN and MOON.

THEOR. 10
The (Sharp, Pointed) symbol of the Zodiacal Division of Aries, used by Astronomers $\frown$ is quite well known to everyone.

It is also well known that this is the place in the heavens where the Fiery Triplicity Begins. Thus, we shall add the Astronomical sign of the Aries (in the Practice of this MONAD) to signify that the aid of fire is required.

We cam summarize this hieroglyphical consideration of our MONAD in our hierglyphical statement:

the Elements of the Sun and Moon of this Monad, IN WHICH THE DENARIAN SYMMETRY IS STRONG, WANT TO BE SEPARATED, AND THIS IS DONE WITH THE AID OF FIRE.

THEOR. 11
The Mystical Sign of Aries, consisting of two Half-Circles joined together at a common Point, is most fittingly signified by the Equinoctial Nycthemera [the place of the sun on the Spring Equinox, the first day of Aries].

The Time of Twenty-four Hours, divided in Equinoctial mode, denotes our most Secret Proportions. I say this in respect to the Earth.
[Equinoctial mode means using with hours of equal length,
not hours of unequal length, a system used before 1200 AD.]

THEOR. 12
The most Ancient Wise Magi have handed down to us the Hieroglyphic Symbols of the five Planets. Indeed, they are composed of the characters of the MOON and the SUN, and from the hieroglyphic symbols of the Elements and of Aries. As shown here, it is not difficult to explain their shapes Hieroglyphically from the foundations we have previously laid down.

First, we shall speak, in Paraphrase, of those planets, which have Lunar Characteristics, then of the ones with Solar characteristics.


When our LUNAR
Nature first revolved around the Earth by the science of the Elements, it was mystically called SATURN. Later [during its second revolution], for the same reason, it was called JUPITER and retained that more secret shape. [rotated clockwise, see chart above].

And, in a more obscure way, they [the oldest wise men] represented the Moon, in the third revolution, with the elements applied. They used to call it MERCURY. You can see how LUNARY it looks [the Lunar Mercury Symbol]. Some of the Wise Men preferred to envision Mercury as being made in the FOURTH Revolution. This will not Contradict our Secret analogy.

Only the Purest Magical Spirit can manage the Work of the albification [tês leuxanseos] in the place of the Moon. By his Spiritual virtue, he may, when ALONE with us in the Middle of a Natural day, speak to us hieroglyphically, without words. He will introduce those 4 Geogamic [Earthly] figures and IMPRESS them into the very Pure and Simple Earth prepared by us. Or, instead, that other symbol [the Lunar Mercury Planets Symbol, on the far right].


THEOR. 13
Don't the Hieroglyphs of the SUN and of ARIES combine to make the Mystical Symbol of MARS? Doesn't the Magistry of the elements (partially) intervene? And, I ask, don't the SUN and the Fully expressed Elements make the sign of VENUS?

Therefore, these two Planets have consideration for the SOLAR circumference [periroran] and to the work of revivification [Anazoopyreseos] by fire.

progression Appears another Mercury, who Uterine Brother of the first. This is clearly plete Lunar and Solar Magic of the Elements, as the Hieroglyphic Messenger tells us most expressly, if only we fix our eyes upon him and lend him an attentive ear. He is (GOD WILLING) that most Famous Mercury of the Philosophers, the MI-

Yet some Great Experts put the SUN itself in his place and degree. In our present age, we are not able to demonstrate this unless we let this Golden Work [Khrysoxarallino] be governed by the SOUL that has been Separated from the BODY by the Art of Fire. This work is difficult and dangerous because of the Fires and Sulphorous

But, surely that marvelous SOUL will show forth, binding VENUS [LUCIFERUM] and even MARS [PYROENTA] to the disc of the MOON (or at least that of MERCURY) with unbreakable bonds.

In the third place (as some will have it) is the SUN of the PHILOSOPHERS (to
Complete our SEPTENARY Number). You can see the exactitude and the clarity with which the ANATOMY of our HIEROGLYPHIC MONAD corresponds with the ARCANA of these two Theorems.

THEOR. 14
Now it is clearly confirmed that this whole Magistry depends upon the SUN and the MOON. Of this, even the ThriceGreat Hermes admonished us, asserting its Father is the SUN and its Mother the MOON.

And we know it is to be nourished in LEMNIAN EARTH. Without a doubt, LUNAR and SOLAR rays exert a singular INFLEUNCE upon it.

THEOR. 15
We suggest that the Philosophers should consider the Labors of the SUN and the MOON around the Earth. While the SUN's Radiance is exalted in Aries, the MOON Receives a new Dignity of Light in the Next Sign (namely Taurus) and is EXALTED above its own innate powers. The ancients explained the Proximity of these LUMINARIES (more notably than others) by the mystical Symbol of TAURUS.

That Taurus is the EXALTATION of the MOON is common knowledge, which has been handed down from the first age of the Man (among the Maxims of the Astronomers). This Mystery can only be Understood by those who have become complete Masters of the Mysteries. For a similar reason, they have said that TAURUS is in the House of VENUS [Veneris esse Domym], of Chaste and Prolific Conjugal love.

As that Great OSTANES concealed in his most Secret Mysteries, "For Nature delights in Nature [ê physis,te physei têrpetai]."

But the SUN, having suffered some Eclipses of its light, re-
2. ceives MARTIAN Strength and is said to be Triumphant in its EXALTATION in the same HOUSE [DOMO] (namely, in Our Aries). These Secret Mysteries are clearly and perfectly shown in our MONAS.

Depicted here is the
 Hieroglyphical Sign of Taurus and also that of MARS, which we explained in Theorems 12 and 13 has a straight line going from the SUN to ARIES.

## 15 verso

From the present Theorem, another Cabalistic anatomy of our MONAD presents itself, of which this is a true and skillful description: KNOWLEDGE OF THE ELEMENTS,WHICH ARE IN THE MIDDLE BETWEEN THE EXALTATION OF THE MOON AND THE SUN. NOTE
In my Opinion, there are two things that should be particularly noted here. First, that the Hieroglyphic Symbol of Taurus also represents to us the Dipthong of the Greeks, which is always the singular Genitive Ending of the first Declension. Secondly, by way of Simple Transposition, the letter ALPHA is demonstrated in two ways: either with the Circle and Half Circle Tangent or (as shown here) intersecting.

## THEOR. 16

We must now briefly Philosophize on our assertions about this noble CROSS. Though our CROSS has been made, as we have said, from two straight lines of equal length, they do not divide each other into equal lengths.

In the Mystical distribution of our Cross, we wanted equal parts and unequal parts. However, hidden in the power of these Two lines divided this way is also the virtue of an Equilateral CROSS (because the two lines are of equal Length).

Generally speaking, a certain JUSTICE of NATURE demands that when a CROSS is made from two lines of equal Length, they should be divided Crosswise equally. In accordance with this Justice, we shall propose the following ideas about the Equilateral Cross (which is just like the twenty-first letter of the Latin Alphabet.)

On this Rectiliniar, Rectangular and Equilateral CROSS, when any Straight dividing line goes through the point of intersection separating Oppositely placed angles, the parts on each side of the dividing line are similar and equal. The resulting parts are the same shape as the letter that the Latins accepted as their FIFTH vowel, and was commonly used among the most
" Ancient Latin Philosophers to denote QUINARIUM [the number 5].

And I think that it was not done by them Irrationally, as it Conforms to the Middle of our DENARIUM [the number 10]. Each of these two parts (from this Hypothetical division of the Cross) represents the number FIVE [Roman Numeral v], one of which is upright, and the Other is upside-down.

This reminds us of a Multiplication, which is the Squaring of Square Roots (which here falls wonderfully on a CIRCULAR NUM-
BER, the number FIVE). Most certainly this produces TWENTY-FIVE (and ing of Square Roots (which here falls wonderfully on a CIRCULAR NUM-
BER, the number FIVE). Most certainly this produces TWENTY-FIVE (and it [the letter V ] is both the twentieth letter and the fifth vowel).

We shall now consider another orientation of the equilateral CROSS which is similar to our MONADIC CROSS. If a similar Division of the Cross into two halves is made, (as above), the twin symbols of another Letter of the Latin Alpha-
 bet is revealed. One of them is upright, and the other is upsidedown and backwards. This letter (from the ancient custom of the Latins) has been used to represent FIFTY.

It seems to me that this sign was established first, because the sign for FIVE was essentially derived from the sign for TEN of Our Cross, and from a Place where that Cross, the Greatest of all Mysteries, is the most Consummate Hieroglyphical Sign. Thus, EMBRACING the Strength of TEN and the virtue of FIVE, it rejoices, and brings forth the NUMBER FIFTY.

## O, MY GOD, HOW GREAT ARE THESE MYSTERIES?

Furthermore, the Name of that Letter, EL [letter L], seems to respect the Denarian virtue of the Cross as it has been placed in the Middle Position between the first Letter of the Alphabet and the letter which makes the Denarian Cross, being Tenth in sequence from either letter [L is halfway between A and X$]$.

And since we have shown that there are two such integral parts of the CROSS (considering now their numerical meaning) it's apparent that the CENTARIUM is produced [the number 100].

## 16 verso

But if, by the Law of Squares they [the two letter L's or the two 50 's] are multiplied by each other, our result is Two-Thousand-Five-Hundred.

If this SQUARE NUMBER [2500] is divided by the previously mentioned Square of the first Circular Number [5 times 5, or 25] it will bring us back to the CENTENARIUM $[2500 \div 25=100]$. Thus, the CROSS, explaining itself by its DENARIAN Strength, will be perceived as referring to CENTURIO [the number 100].

Therefore we are now taught (besides other things worthy of being noted) by these Theories of the CROSS to enumerate and proceed in this manner: One, Ten, Hundred. We are carried upwards by the DENARIAN Symmetry of the CROSS. Nevertheless, as the Character of the CROSS is unique, it also represents One.

THEOR. 17
As it is apparent from Theorem 6, there are FOUR right angles in our CROSS. The preceding Theorem teaches how to attribute to each of them a QUINARIAN significance, the right angles being still arranged the same way, but having a different Position [ X as opposed to + ].

The same theorem shows how the Hieroglyphic Symbols of the Number FIFTY are made [Roman numberal L].

Also it is quite evident that, vulgarly, the CROSS signifies the number TEN. This is also the twenty-first letter in the sequence of the Latin Alphabet (whence it came to pass that the Wise Men called Mecubalists [ones versed in Jewish tradition] used to signify twenty-one by the same letter).

Finally, the Cross may be considered in a most simple way, as it is seen to be One Symbol, whatever other virtue and whatever degree of strength it has.

From all this it may be concluded, by the best Cabalistic Description that our CROSS is able to signify, to the Mystics, in a Wonderfully Abbreviated way, TWO HUNDRED AND FIFTY TWO [number 252]. As FOUR times FIVE; FOUR times FIFTY; TEN, TWENTY-ONE, AND ONE makes TWO HUNDRED AND FIFTY TWO.

There are two other logical ways that we can draw forth this Number from our premises. For the sake of brevity, we recommend these reasons be rooted out by Beginning Kabbalists. The various artificial productions of this Magistral Number are also worthy of the Consideration of Philosophers.

I shall not conceal from you here another Memorable Secret Mystery. We have Seen that our Cross has allowed itself to be Divided into two other letters. As previously we dealt with their Numerical virtue in a certain way, now we shall compare their VERBAL FORCE with the CROSS, because then a LIGHT [LUX] will appear. We shall understand with the highest admiration the Final and Magisterial WORD (through the Harmony and Agreement of the TERNARY in the Unity of the Word).

THEOR. 18
From our twelfth and thirteenth Theorems it may be gathered that Celestial Astronomy is like a parent and master to INFERIOR [Astronomy].


Therefore, our Cabalistic eyes being lifted towards Heaven (illustrated by the Theories of these Aforementioned Mysteries) we shall behold an ANATOMY exactly corresponding to that of our MONAD, showing itself to us in the LIGHT AND LIFE OF NATURE.

For it reveals, by its own WILL, the Secret Mysteries of this Physical ANALYSIS.

## 17 verso

As we were contemplating both the Theoretical and the Heavenly motions of that Celestial MESSENGER [Mercury], we were taught that the figure of an EGG might be applied to these COORDINATIONS.

For it is well-known to Astronomers that he makes an OVAL-shaped Circuit on his course through the Aether.

And since a word to the wise is sufficient, behold our Interpretations of this Celestial Advisor (shown hieroglyphically), which completely agree with what we have previously said. HENCE, let the Pitiful Alchemists be admonished to acknowlege their various Errors.

> What is the WATER of the White of EGGS?
> What is the OIL from the YOLKS?
> And what is the SHELL of the EGG?

May these Ignorant Impostors, in their Desperation, come to understand these things and many more things like them: HERE WE HAVE PRACTICALLY ALL OF NATURE'S SYMMETRY.

Once upon a time, a SCARAB [dung-beetle] shattered an EAGLE'S EGG because of the INJUSTICE, the violence and cruelty, which that BIRD had inflicted on Men and Timid Beasts. Some took refuge in the Scarab's Cave (seeking help), but still they did not have their freedom.

The Scarab determined that he alone, in any way possible, must avenge that INJUSTICE. He had a spirited mind, was prepared with a firm determination, and lacked neither Strength nor Ingenuity. The Scarab made several efforts to persecute the EAGLE Using the most Subtle Art of DUNG.

At last, he caused the EGG (which had been deposited in the Lap of Jupiter) to FALL DOWN TO EARTH and be BROKEN INTO PIECES.

Using this and other methods, the Scarab would have obliterated all of Eaglekind from Earth, had not Jupiter (on the Alert for such an evil) ordered that no SCARABS shall fly about at the time of year when EAGLES care for their EGGS.

I would counsel those who are bothered by the Cruelty of the BIRD to learn a most Useful art from those Sunbeetles (who live by lying hidden for certain courses of time).

Even if they themselves do not act, it is still most acceptable if, from the EVIDENCE and Signs, Revenge can be taken on the Enemy.

If those men, to whose minds it first came to telling fables concerning the highest Mysteries of Nature, were present, they would confess (O KING ) that I am not trying to play Aesop, But Oedipus.

I know for sure that there are some who, if they had the EAGLE'S EGG DISSOLVED, by the SCARAB'S ARTFILLNESS, would first COMBine [TEmperamentum] its SHELL with the entire, pure white of the EGG. Then they would smear that compound with all the liquid of the YOLK, in a skillful way, rolling, and rolling some more, just as the Scarabs conglomerate their Balls.

Thus, a great METAMORPHOSIS OF THE EGG would occur. Indeed, the WHITE, (by those multiple, as it were, Spiral Revolutions), would certainly disappear as it involutes with the LIQUID OF THE YOLK.

By this Artifice, such a Hieroglyphical sign will not displease the Stewards of NATURE. We read that such an Artifice was much celebrated in prior centuries, by the most venerable and most Ancient Philosophers, as most certain and most useful.


Later, Anaxogoras made his most excellent Medicine from this Teaching, as seen in his little book, The nature of whirling around fast. [peri ton ekstrophon physikon]

## 18 verso

He who sincerely applies his mind to these Mysteries will clearly see that nothing here is outside of the virtue of the Hieroglyphical MONAD.

THEOR. 19
The Pyronomic Analysis [Analysis by Fire] of all Corporeal things demonstrates effectively that the SUN and MOON infuse their Corporeal strengths, into all Inferior Elemental Bodies in a much stronger manner than do all the other Planets.

The MOON pours out Watery Moisture [Aqueous Humor]. The SUN pours out Fiery Liquid [Igneum Liquorem]. Thus the TERRESTRIAL CORPULENCE [of the fat of the Earth] of all mortal things is sustained.

THEOR. 20
Previously we demonstrated, by good Hieroglyphical reasoning, that the ELEMENTS are signified by Straight Lines. Here, we shall provide an Accurate Observation about the POINT which is at the CENTER of our CROSS. As in our Examination of the TERNARY, that [point] can in no way be Regarded as Absent from [that central] location in our BINARY. Some (Unskilled in Divine Mathematics) might Contend that it was Absent. If it was absent, then our BINARY world not Remain, but a QUATERNARY would emerge. Taking away that point, would create a Discontinuity of the uniformity of the Lines.

Yet our Adversary had Supposed with us that a Binary would Remain. By this argument, the BINARY and the QUATERNARY would be one the same, a thing which is Manifestly impossible [ton adunation]. That POINT must Necessarily be there, as, along with the BINARY, it Constitutes our TERNARY. Nothing else can be SUBSTITUTED in its place.

Nonetheless, it is not of the Essence [Hypostatic Property] of the BINARY, nor in any other way a Part of it. That it is not a Part can be clearly explained this way: All Parts of a Line are Lines. Yet the hypothesis affirms that this is a POINT.

Therefore, it is not any part of the BINARY, never mind its being of the Essence of the Binary. Thus it should be particularly NOTED that it even though it is contained in the LINEAR Lengths of the BINARY, it has a ESSENCE of its own.

And since, in this way it is seen to be COMMON TO BOTH, it can be thought of as RETAINING A SECRET IMAGE OF THE BINARY.

Thus, we clearly DEMONSTRATE: THE QUATERNARY RESTS IN THE TERNARY.

I beseech you, my God, to forgive me, if I have Sinned against your Majesty by Revealing so great a Secret in Public Writings. But, I Hope Only Those who are Worthy will Understand.

Let us now proceed to that QUATERNARY, which we have assigned to our CROSS. Let us discuss whether that POINT contained THEREIN can be absent.

Mathematics surely teaches us that it can be removed.
IF THERE IS A SEPARATION, not only does our QUATERNARY RESULT, but it becomes much more DISTINCT and made CLEARER for everyone to see.

NO PART OF THE SYMMETRY OF ITS SUBSTANCE HAS GONE AWAY. THIS SUPERFLUOUS AND CONFUSING POINT IS THUS UNCOVERED, BUT CONDEMNED.

O Almighty and Divine Majesty, WE MORTALS ARE FORCED TO ADMIT WHAT GREAT WISDOM AND INFINITY OF UNSPEAKABLE MYSTERIES ARE CONTAINED IN THY TITTLES AND JOTS, AS REPRESENTED IN THE ORDERLY ARRANGEMENT OF THY LAW.

CAN THE GREATEST SECRETS AND ARCANA OF THE EARTH BE EXPLAINED AND FAITHFULLY DEMONSTRATED, BY VARIOUS EVIDENCE, SOLELY BY THAT ONE POINT WHICH I (BY THY LIGHT) HAVE LOCATED AND EXAMINED?

## 19 verso

This POINT, seen clearly in the divine TERNARY, is by no means SUPERFLUOUS there. But, when the POINT is in the REALM OF THE FOUR ELEMENTS, it is considered FECULENT [containing feces or dregs], indeed CORRUPTIBLE and FULL OF DARKNESS. O Three, Four Times Blessed are Those Who are able to ATTAIN that (as it were, COPULATIVE) POINT of the TERNARY, and who can leave its GLOOM and SUPERFLUOUSNESS to the Prince of Darkness.

Thus we shall reach a CLARITY [as white as] SNOW and the distin-

O MAXIMILIAN (with you or some future member of your Austrian Family as The Teacher of these Mysteries), Whom God, to the Honor of His Tremendous Name, will make the Greatest in times to come (while I am Sleeping in Christ) in that abominable, even intolerable Darkness (of the Point, which is SUPERFLUOUS ON EARTH). But, lest I Myself should offer Superfluous words (that are not in their due place), I will presently bring myself within the Limits of my purpose.

Now, since I have finished my Discourse to those whose eyes are Seated in their Hearts, I must turn my Speech to those whose Hearts still extend from their eyes. The figure of the CROSS, illustrated here, is able to represent the things we have previously spoken about.

First, in figure A, the POINT is NECESSARY in the Two LINES of Equal Length (intersected equally or unequally).

Then, in figure B, (where there is a certain Emptiness where the superfluous Point has been removed) you can distinctly see FOUR
 straight Lines which, without suffering any change, have been SEPARATED from the POINT they previously had in common. This is the way in which Our MONAD, progressing by way of the Binary and TERNARY, is restored to its OWN Oneness in a Purified QUATERNARY by the Proportion of Equality (for every Whole is Equal to all its parts).

During this process, our MONAD does not admit any External Units or Numbers. It is perfectly self-sufficient, being complete in all its numbers.

It is diffused in Magical ways into the grand Abundance [of Numbers]. Eventually, by the uncommon, Skillful Work of a Master and by the greatest Profit of the Monad itself, in Dignity and Strength), it is Restored to its First and Own MATTER. Meanwhile, the Impurities which have no Respect for its genuine and hereditary Proportion, have, by all means and diligence, been cut off and cast away forever.

## THEOR. 21

Earlier you have seen the Philosophical Translation of the MONAD made when that which Lies Inwardly Enclosed in the Recesses of our MONAD was brought to Light. Its First Parts or, as it were, Outer Parts changed Places and Became Enclosed in the Midddle place.
[Dee seems to be referring to how the planetary symbols formed the central
Monas symbol in the "Anatomy of the Monad" diagram of Theorem 13]
Now we will show you another transposition of the Mystical MONAD. When our Hieroglyphical Characters of the SUPERIOR PLANETS earlier showed themselves to us, they were Upright.

When they are changed in another way, these Planets will be in the Order which Plato ascribes to them. Saturn, Jupiter, and Mars come together where the Point of Aries is. Then descending, the Cross serves [to help form the symbols of] Venus and Mercury. Finally, there follows the Sun itself and, at the bottom, the MOON. But these matters should be dealt with in another place.


However, I did not wish to conceal these Philosophical Treasures of our MONAD, so I have decided to give one reason we considered it meaningful to change the Position of the MONAD in this manner. Concerning this Position, you shall See and Hear greater things, to be explained in a few words.

## 20 verso

Let us therefore Divide the Monad (positioned in this new way) into its anatomical parts $\mathrm{B}, \mathrm{D}$, and C . In that new TERNARY are parts D and C, signs that we have previously become acquainted with [Moon and Sun], but here they appear somewhat uncouth. The THIRD one, marked B, might not be as easily recognizable to everyone, but it should not be considered lightly.


Those well-known FORMS, D and C, denote ESSENCES which are separate and different from B.

Secondly, the horns of C are seen turned downward, as it were, towards the EARTH.

And that D , in whose center alone is that POINT to be seen which is truly TERRESTRIAL, illuminates C, and looks towards the earth, namely downwards.

And finally, that both D and C here direct their Hieroglyphic message towards lower places than does B.

The earth, however, may Hieroglyphically denote to us STABILITY and FIXATION. What, therefore, D and C are, I leave to inference. Everyone can hereby learn a Great SECRET. What we previously said about the SUN and the MOON when the lunar Horns were elevated upwards, may now be interpreted in a fuller and most necessary way. But enough of these matters.

Now we will examine the NATURE of that THIRD symbol [labled B] in Accordance with the Principles of our Hieroglyphic Art. First, it seems to carry on its Head a DOUBLE MOON, our Aries sign (only Mystically inverted). Then, appended to it, is the Hieroglyphical Sign of the Elements.

How great this Duplicate MOON is, (according to the subject Matter) can be explained by the GRADES OF THE DOUBLE MOON. We speak of those degrees, which Experts in Natural Science can find but FOUR among all created NATURE, namely, TO BE, TO LIVE, TO FEEL AND TO UNDERSTAND. Noting that the First Two of these Grades are in this [inverted Aries sign or "double-moon"] we shall thus say:

The moon exists and is alive.

Some define Life by MOTION, and there are Six well-known kinds of movement [up, down, left, right, front, back, as per Plato in the Timaeus].

The adjoining CROSS denotes that the Distinguished Artifice of the Elements is required here. Moreover, we have frequently said in our Theorems, the HALF-CIRCLE is the hieroglyph of the MOON, and the Whole-Circle signifies the SUN.

But now, there are two Half-circles, which are SEPARATE (though Connected by a common POINT). If they are appropriately joined (as indeed they may be by art) they are able to represent the Circular fullness of the SUN. Taking all these considerations together, we might Hieroglyphically Summarize with this maxim:

THE MOON, EXISTING AND ALIVE, WITH THE TREATMENT OF THE MAGISTRY OF THE ELEMENTS, HAS THE POWER TO REPRESENT THE FULLNESS OF THE SUN, WHEN ITS TWO HALF-CIRCLES ARE JOINED TOGETHER BY ART.

We show that completed CIRCLE (which we just mentioned) noted here letter E [in the illustration]. First, let us remember that this SOLAR GRADE did not, by NATURE, lie in our way, but has been MADE UP ARTIFICIALLY.

Indeed, in its first appearance it preseated itself to us in its Nature (as can be easily seen in B) with its Parts Loose, Flowing, and unconnected, not yet Compacted SOLIDLY into a Solar Appearance.
[in B, the outer tips are unconnected, but in E they are connected]
Let us next remember that the Radius of these Half-Circles is not equal to the Radius of D and C (which were produced for us naturally and are Well-Known to all), but are much smaller. Thus it is clear that B is not of such great magnitude as D and C.

And E confirms this for us very well, as by the operation of [closing] the Circle, B was advanced to the shape of E. Thus, before our eyes appears nothing more than the sign of VENUS.

## 21 verso

Therefore, we have already made it plain by those Hieroglyphic Syllogisms: We may not hope for the true D to be [produced] out of B .
[a syllogism is an argument with two premises and a conclusion]

Nor was there, at first, a true C in the nature of B , and therefore no TRUE, live MOON. Thus, concerning LIFE and Motion, you might be doubting that [a relationship] really exists between them in Nature.

However, as we have already made clear to the wise, ALL THINGS that we have said (about B) in metaphorical phrasing are ad minus ANALOGIES. Also, that which we briefly touched upon regarding C and D applies ANALOGICALLY quite fittingly to B and its ELEMENTS.

Furthermore, what we have said about the Nature of Aries must apply to B, because it carries Aries (though inverted) on its head. That Mystical Sign of the Elements is also joined to B. From this Anatomy of the singular body of the MONAD (thus dissected by art) we see that a new TERNARY has come forth.

Thus we can have no doubt that the MEMBERS, thus Formed, embrace each other closely in a mutual SYMPATHY. They allow, as if by their own accord, a MOST ABSOLUTE MONADIC UNION whose MEMBERS have a strong MAGNETIC virtue.

Finally, we are pleased to note (for the sake of the recreation of the mind) that B most readily presents us with as many RUSTIC letters as it has pointed ends on its Head or, as it were, on
 its Forehead.

The three clearly illustrated here, are very ROUGH
and in want of neatness, yet fluid and rolling. While, in a different way, there are six, (which Summed together make three times three). As you see, they are made from one or more Half-Circles.

Yet in the hands of Experts on the writing of letters [grammarians or literati], there is a stronger, more Enduring Reason for the SHAPING OF THOSE LETTERS. Here I have had before my eyes an infinity of Mysteries, but I wanted to interrupt the Theorizing with this Sport.

Yet, (After restoring our MONAD to its former Mystical Position, Skillfully Compositing its several Members) I understand that I will promote the Efforts of some if I At Least advise them and exhort them to NOW accurately learn WHAT the FIRST TRIPLICITY, the FIRE of ARIES, is. WHAT that Equinoctial is. WHAT caused the SUN to be EXALTED and capable of being RAISED ABOVE ITS ORDINARY GRADE.

And to RUN OVER, IN SECOND AND WISER MEDITATIONS the many things we have previously stated. As we hasten on to other things, we thought it fit to point out to others on the road (on which they should press on) not in only in a friendly way, but also most faithfully, though keeping silent (as we have said) on the CONSPICUOUS infinity of other Mysteries.

THEOR. 22
It's clear that the Mysteries of our MONAD have not yet been exhausted. Now I will show Your Serene Royal Highness more secret Vessels of the HOLY ART (indeed, entirely Kabbalistic ones) carefully chosen from the workshop of the MONAD, and which provide revelations only to Initiates. Therefore, with All of the Connections of our MONAD Wisely DISSOLVED, let us add letters to the various parts (for the sake of distinction), just as you see Marked here.

We point out that $\alpha$ [the lowercase Greek letter alpha] is a certain Artificial Vessel made from A and B , with M (the RADIUS common to both, only now made Evident). As you can see, it differs from the First letter of the Greek Alphabet by only a slight Transposition [Metathesis] of its parts.

We are the first to teach that its True and Mystical Proportion consists of a Straight Line, a Circle and a Half-Circle. Although it can also be made from just a Circle and HalfCircle, as we have shown previously. [in the NOTE at the end of Theorem 15]


## 22 verso

Nevertheless, all these ways fall within one and the same Mystical design.
But $\lambda \& \delta$ are, at least Primarily, like images of other implements (indeed, $\lambda$ is VITREOUS [made of glass], but, $\delta$ is an Earthen one [made of clay, earthware, stone, etc] [ $\lambda$ and $\delta$ are the lowercase Greek letters lamda and delta, which, in uppercase, are $\Lambda$ and $\Delta$ ].

And secondly, $\lambda$ and $\delta$ may remind us of a certain Pestle and Mortar, which have to be made from a material (truly) that with them we can Pulverize into fine Powders, Artificial Pearls without drilled perforations, Plates of crystal or Beryl, Chrysolites and precious Rubies, also Carbuncles and other Most Rare Artificial Stones.

Lastly, that which you see marked $\omega$ is a small vessel which is Full of Mysteries. The vessel differs from the very last letter of the Greek Alphabet (now restored to its originally established Mystagogic [pertaining to mysteries] meaning) by a slight, but obvious, transposition of its parts, which are two half-circles.

It is not Necessary to further discuss the shape of these common Vessels nor the Materials (from which they should be made). Yet it should be noted that $\alpha$ [lower case Greek letter alpha] is waiting for an opportunity to perform its role, by a short, but very Secret ARTIFICIAL air-vent.

## And (

it will draw forth a Primordial Specimen most useful to Beginners of this WORK until a more skillful Way of Preparing SUBTLE [substances] becomes known to them. But any external Air or Wind would do much damage in $\lambda$, the glass [vessel], (in the performance of its principal function).
$\omega$, however, is a MAN of ALL HOURS. [lowercase Greek omega]

## Corollary [Porisma]

Who cannot detect the scent of those sweet and healthful Fruits of The Holy Art [Tes ieras Texnes] that arises (I declare) from the Mystery of just these two letters? We shall bring some of these [fruits] (from our HESPERIAN GARDEN) a little closer, to be seen as if in a mirror.

Yet we still will not be bringing forth anything but our MONAD. For the Straight Line appearing in Alpha is homologous to the part marked by the Letter $\mathbf{M}$ in the most recent Anatomy of the Cross. From this the rest of the chart becomes accesible.


With these few [words in the chart], I know I am providing not only starting points [arormas], but Conclusive Proofs [Apodixes] to those in whom inwardly there blazes a fiery Vigor and a heavenly Origin. May they readily lend an ear to the great Democritus, announcing to those who wish a remedy for their spirit and who, by all means, crave a deliverance from their hard labors, that this Doctrine is not Mythical [Mythakon], but Mystical [Mystikon] and Secret.
[to tes psykes...iama kai pantos moxthou lutêrion kataskseuasai boulomenois]

## 23 verso

As also [they should listen] to he who has asserted that it is the method established by the speech of the maker of the world, that the religious man, born of God, by right-working, may learn by these words, which are theological and mystical.
[lôgo demiourgou (demiurge) xosmou (cosmos) metho denetai: ina o theophron xai o thegenes anthropos, dia tês rutheias ergasias: xai theologixon, xai mustixon logos mathe]

THEOR. 23
We now present the proportions, accurately notated, observed by us in the Hieroglyphical Construction of the MONAD, to be observed by those wishing to bear it on Rings and Seals, or to use it in other ways.

In the Name of JESUS CHRIST who was for us affixed to the CROSS (the pen only of Whose Spirit, writing these things swiftly through me, I Desire and I Hope to be), we shall now endeavor to obtain all these Measurements from our ELEMENTS of our CROSS.

We do this because (in accordance with the SUBJECT MATTER of our INTENDED ARGUMENT) everything that takes the Beginning of its Generation under the Celestial MOON is either composed of the FOUR Elements or is itself on Elementary ESSENCE. And that [is possible] in various ways that are not Commonly Known.

And since these Elements are not in Equal Proportion or strength in any Created thing, yet (as the Wise know) can in certain things be reduced to Equality by Art, we have made our CROSS from equal and unequal parts.

Thus, in another regard, we may call them the Same and the Different, or the One and the Many, while (as we pointed out above) Secretly admitting the qualities Peculiar to the equilateral CROSS.

But, if we were to clearly point out the causes or divulge all the reasons (which we hold fast) for the PROPORTIONS shown here, more than the ones we have explained (to the wise) throughout the whole book, we would be passing beyond our limits, which were not prescribed without intent.

Choose any Point in a plane, for example A. Draw a line through it at sufficient length on both sides. Make this C,A,K. At Point A, on the line KC, erect a Perpendicular.

Extend it to a sufficient Length (in Infinitum, as the Geometers say, and rightly so, to avoid inconveniences). Let this line be DAE. Now, choose a Point anywhere on line AK and let it be B .

Thus, having first of all established AB (which is the common Measure of our work) project its triple [length] from A towards C. This line shall be AC.

Make AE Twice the Length of AB. Also, make AD Twice the Length of $A B$. Thus, the whole DE is Four Times the length of $A B$.

In this way, we have made our CROSS OF THE ELEMENTS from a QUATERNARY of lines: AB, AC, AD, and AE.

Let a straight line of length AD be cut out of the BK and call it BI. With a Centerpoint at I, and a Radius of IB, describe a Circle. The Circle cuts line $A K$ at $R$, so the diameter of the circle is $B K$.

Let a straight line of length AB be drawn from point R towards K , and let it be RK. Then, let a straight line of sufficient length be drawn extending out from both sides points K (at right
 angles to AK ) which shall be line PKF.

Let a straight line of length $A D$ be projected from point $K$ toward F and let it be line KF. With a centerpoint at K and radius KF describe a half-circle FLP, whose diameter is FKP.

Finally, let a perpendicular to the straight line AC be drawn through point $C$. It should extend to sufficient length on either side and be called OCQ.

## 24 verso

Then, on line CO and from point C , make a straight line of length AB , which shall be CM . With a center point at M and radius MC , describe a half-circle CHO whose diameter is CMO. Likewise, a line of length AB shall be made along CQ and from point C , and this line shall be CN . With a centerpoint N and radius NC , describe half-circle CGQ, whose diameter is CNQ.

We now affirm that all the required PROPORTIONS of our MONAD have been explained and described.

We should point out to the Mechanicum that the whole line CK consists of nine equal parts, each the length of our FUNDAMENTAL AB. Thus, he may go about performing this work in another way.

Also, all Diameters and Radii ought to be marked with (as the Mecanici say) invisible lines. Nor should any CENTERS remain visible, except for the Solar Center, which is seen here marked with the letter I. Furthermore, no more letters are to be added.

Now, for the sake of Ornament (there are no Mystical requirements considered by us now) the Mechanicus can add a certain Surface Width to the Solar Circumference (by drawing one concentric circle inside of it). (The distance between the two concentric circles should be approximately one fifth to one quarter of AB [the length of that "common Measure"] ).

The Moon is to be a fully horn-shaped, the way she appears in the Sky after her first Conjunction with the Sun. To do this, measure up from point K, towards point R , a fourth or fifth (as we have mentioned) of the length of line $A B$. Using this as a Center, and line $A B$, which is in fact the Radius of the Moon, draw a second partial-Circumference, which will contact and rest on both sides of the previously drawn Half-Circle.

A similar thing can be done at points M and N . Erect Perpendiculars at these points and measure upwards one sixth the length of $A B$, or even less. With these new points as centers and the previously used radii MC and NC, draw second half-circles, as it were, on the outside.
[A "Mechanicum" is a skilled workman without the knowledge of Mathematical demonstration Dee's definition from the Preface to Euclid]
["invisible" is a translation of Dee's Latin word obscuris, meaning "dark", which poetically means "invisible," as objects become invisible in the darkness.]

Finally, on both sides of the Straight Lines of our Cross, drawn parallel lines at a distance of about one tenth to one eighth of that length $A B$.

Thus, our CROSS is made from FOUR, as it were, Linear Surfaces whose width is about one fifth to one quarter of length $A B$.

In this adjoining illustration, I have sketched in outline one way that this Ornamentation might be done. One may arrange all [these widths] however he sees fit, as long as no harm (not even the slightest) is done to our Mystical PROPORTIONS.


By such negligence, the new Discipline of these true (and essential) Hieroglyphic Measurements may, in the course of time, be thrown into confusion or even perish.

It [this "new Discipline"] is by far more splendid and Grand than we have been able, or indeed, even wanted, to explain in this little book. TRUTH, the Daughter of Time, will teach this, GOD WILLING.

We will now Methodically place a few more things before your eyes, which may be obvious to anyone becoming practiced in the Symmetries of our MONAD. Let's begin with the QUATERNARY of Lines in the Cross.

Some are in the habit of declaring that these lines are, in essence, FOUR. But, this QUATERNARY of lines, rightfully, is capable of a different Mystical partitioning and calculation.
[To summarize these "secondary" circles and half circles:
(1) A circle is drawn inside the Solar Circle.
(2) A half-circle is drawn above the Lunar Crescent.
(3) Two half circles are drawn above the two horns of Aries.]

## 25 verso

Thirdly, we will point out several examples of Numbers, which are used by God in NATURE, that we have skillfully derived from it [the Cross] or from other Theories throughout the book.
[Fourthly] We shall blend in others [other numbers], in apropriate places, which, if understood correctly, will bear not a little fruit. All this we shall do concisely.


## Our Canon of Transposition

" tinuous multiplication from the First to the Last, starting from the First
, Monad and proceeding with the Natural sequence.
, In other words, multiply the First times the second, then that Product by the Third, then that Product by the Fourth, continuing to your last number.

The final product is the number of Possible Permutations in so many places [or how many ways in which the chosen number of digits can be re-ar-
" ranged].
This same procedure of computation can be used anywhere and " for so many diverse things. I highly Recommend this Operation to you (O KING) as the one most useful in every investigation of Nature and also in the Affairs of the Republic. I am in the habit of using it with the greatest of satisfaction in the Tziruph (or Thmura) of the Hebrews.

QUA-


I am Indeed not Ignorant that, from the Arithmetical Virtue and FORMAL NATURE of the QUATERNARY, very many other Numbers could be brought to light.

But HE who does not understand how their greatly concealed Na ture is to be developed and illuminated would feel his intellect
blunted, not sharpened by a greater multitude of them.
Therefore, the carefully considered diagrams which
follow show how our Numbers Originate in the
WEIGHING OF ELEMENTS, marking the
MEASURES OF TIME, and finally in the ordering of the STEPS of the Power and Virtues of Things.



Words cannot express the many things that can be drawn forth from these Diagrams (if they are deeply contemplated).

So we give here one Reason, above all others (which, together with this whole new art, we divulge from the first time) why the QUATERNARY, as well as the DENARY impose, for the common good, certain limits in Numeration.

$$
\begin{aligned}
& \text { We assert that the reason- ing, which our Ancestors extolled } \\
& \text { is not as complete and exact as the one we will now make known. } \\
& \text { It is neither in the power } \\
& \text { of NATURE, nor any ART to any MOVEMENT or progress UNLESS IT BE BY FOUR } \\
& \text { Supercelestial Revolutions. }
\end{aligned}
$$

After this, the MONAD will be wholly and fully Physically Restored (then, indeed, it is a MOST UNITED MONAS, what the Magi proclaim as ONENESS).

## 27 verso

(And thus is brought forth for us, He , whom, on account of his eminence, we wish to denote in this way [as inverted].)

This is so because there is no OVERFLOWING CREATIVE power in the Elemental world, nor the Celestial, nor the SUPERCELESTIAL, with which it has not been most completely enriched and endowed.

FOUR Famous Men who were Philosophizing together (in times past), through their labors, grasped its real Effect. For a long time, they were Astonished by the Great Wonder of the Thing. Then, at length, they devoted themselves entirely to Singing and preaching Praises of the Most Good and Great God. On account of this, they were granted great Abundance, as well as the Wisdom and Power to rule over other CREATURES.

## THEOR. 24

In the Beginning of this Little Book, we started with a Point, a Straight Line, and a Circle.

Now, at the End, like a Circle Completing Itself, we have a POINT, LINE, and our ELEMENTS Flowing Out of our MONAD, which is Analogous to the Equinoctial when a Circuit is completed in 24 Hours.
2. Consummate and Conclude with the METAMORPHOSIS of ALL THE TRANSPOSITIONS OF PARTS OF A QUATERNARY (defined by the Number 24).
3.

HONOR and GLORY to Him, who Sitteth on the Throne (as John, Chief Protector of Divine Mysteries Testifies in the FOURTH, AND LAST verse of the FOURTH Chaper of Revelations).
4.

AROUND Whom were four Animals (each having SIX WINGS), DAY and NIGHT, without rest, declaring Holy, Holy, Holy, Lord God Almighty, Who was, Who is, and Who will come.
5.

And WHOM, 24 ELDERS, in 24 Seats, placed in a CIRCLE, falling forwards prostrate (HAVING CAST OFF THEIR GOLDEN CROWNS) adore, saying:

Thou art Worthy, O Lord, to receive the GLORY and the HONOR and the POWER,
FOR THOU HAST CREATED ALL THINGS.
Because of THY WILL, THEY ARE, AND HAVE BEEN CREATED.

AMEN, SAYS THE FOURTH LETTER,
$\Delta:$

To whom GOD gave the Will and Ability to record this Divine Mystery in a Written Memorial, and to complete these his Labors peacefully on January 25th, having begun on the 13th
day of the same
In the year 1564, Antwerp.


The Eye of the Vulgar
will, here, be Obscured and most Distrustful

ANTWERP:
Prepared by Gulielmus Silvio, royal typo-
GRAPHER: ON THE DAY BEFORE THE
FIRST DAY OF THE MONTH OF APRIL, IN THE YEAR 1564


## Preface to Euclid


f. $\mathcal{D} \varepsilon$.

Hcre haue you(ia:cording to my promiffe) the Groundplat of
my MATHEMATICALL Praface: annexed to Euclide (now firlt) publifhed in our Englifhe tounge. An. 1570 . Febr. 3 .


# swTO THE VNFAINED LOVERS 

 of truthe, and conftant Studentes of Noble Sciences, IO HN DEE of London, bartily wifheth grace from heauen, and moft profperous fucceffe in all their boneft attemptes and exercifes.

Iuine Plato, the great Mafter of many worthy Philofophers, and the conftant auoucher, and pithy perfwader of $V_{\text {rnum }}$, Bo. num , and Ens : in his Schole and Academie, fundry times (befides his ordinary Scholers) was vifited of a certaine kinde of men, allured by the noble famc of $\boldsymbol{\nu l a t o}$, and the great commendation of hys profound and profitabledoctrine. But when fuch Hearets,after long harkening to him, perceaucd, that the drift of his difcourfes iffued out, to conclude, this Vnumz, Bonum, and Ens, to be Spirituall,Infinite, Aternall, Omnipotent, \&c. Nothyngbeyng alledged or expreffed, How, worldly goods: how, worldly dignitie:how, health,Strégth or lufines ofbody:noryet the meanes, how a meraeilous fenfible and bodyly blyffe and felicitie hereafter,might be atteyned: Straightway, the fantafies of thofe hearers, were dampt: their opinion of $P$ lato, was clene chaunged:y ea his doctrine was by them defpifed:and his fchole, no more of them vifited. Which thing, his Scholer, Ariffotle, narrowly cöfidering; founde the caufe therof, to be, For that they had no forwarnyng and information, in gencrall, whereto 'n his doctrine tended.For, fo, might they haue had occafion, either to haue forborne his fctiole hauntyng: (iffthey; then, had milliked his Scope and purpofe) or conftantly to haue continued therin:to their full fatiffaction : iffuch his finall frope \& intent ; had ben to their defire. Wherfore, Ariffote, euer, after that, vfed in brief, to forewarne his owne Scholers and hearers, both of what matter, and alfo to what ", ende, he tooke in hand to fpeake, or teach. While I confider the diuerfe trades of " thefe two excellent Philofophers (and am moft fure, both, that Plato right well, otherwife could teach : and that Arifotle mought boldely, with his hearers, haue dealtin like forte as Plato did) I am in no little pang of perplexitie: Bycaufe, that, which I millike, is moft eafy for me to performe (and to haue Plato for my exäple.) And that, which I know to be moftcommendable: and (in this firt bringyng, into common handling, the © Artes cMathematical) to be moft neceflary: is full of great difficultie and fundry daungers. Yet, neither do I think it mete,forfo fraunge matter(as now is iment to be publifhed) and to fo ftraunge an audience, to be bluntly, at firft,put forth,without a peculiar Preface : Nor (Imitatyng Arijfotle) well can I. hope, that accordyng to the amplenes and dignitie of the State CMathematicall, I am able, either playnly to prefribe the materiall boundes: or precifely to expreffe the chief purpofes, and moft wonderfull applications therof. And though Iam fure, that fuch as didfhrinke from Plato hais ichole, after they had percciued his fiv
nall
F. De $\varepsilon$.
Here haue you(ia:cording to my promiffe) the Groundplat of



## IohnDee his Mathematicall Preface.

nall conclufion, would in thefe thinges haue ben his moft diligenthearers) fo infinitely mought their defires, in finc and at length, by our Artes Mathematicall be fatiffied) yct, by this my Prxface \& forewarnyng, Afwell all fuch, may(to their great behofe) the foner, hither be allured:as alfo the Pythagoricall, and Platonicall perfect fcholer, and the conftant profound Philofopher, with more eafe and fpede, may (like the Bec,) gather, hereby, both wax and hony.
Wherfore,feyng I finde great occafion(for the caufes alleged, and farder, in re, (pect of my Art © Mathematike generall ) to vfe a certaine forewamyng and Praface; , whofe content fhalbe,that mighry, molt plefaunt, and frutefull Mathematicall $T$ ree, The intert of with his chicfarmes and fecond (grifted) braunches: Both, what euery one is, and
tbu Preface. alfo, what commodiry, in gencrall, is to belooked for, afivell of griff as focke:And , forafmuch as this enterprife is fo great, that, to this our tyme, itneuer was (to my ,, knowledge) by any achicued : And alfo it is molt hard, in thefe our drery dayes,
" to fuch rare and ftraunge Artes, to wyn duc and common credit : Ncucrtheles, if, for my fincere endeuour to fatiffic your honctl expectation, you will but lend me your thakefull mynde a while:and, to fuch matteras, for this time,my penne (with ipede) is hable rodeliuer, apply your cye or care attentaffly : perchaunce, at once, 1pede) is hable to dchuer, apply firf faluryng, this Preface you will linde a leffon long cnough, And cither you will, for a fecond (by this) be made much the apter: or thortly become, well hable your felues, of the lyons claw, to coniceture his royall fymmetrie, and eyes, and bend your myndes to that doctrine, which for our prefent purpofe, my eyes, and bend your mynues to thate
Alt thinges which are, \& hane beyng, are found vnder a triple diuerfitie generall. For, cither, they are demed Supernaturall, Naturall, or, of a third being. Thinges Supernaturall, are immateriall, fimple, indiuifible, incorruptible, \& vnchangcable. Things Naturall, are materiall,compounded, diuifible, corruptible, and chaungeable.Thinges Supernaturall, are, of the minde oncly, comprehended:Things Naturall, of the fenfe extcrior, ar hable to be perceiued. In thinges Naturall, probabilitie and conicture hath place: But in things Supernaturall, chief demófration, \& molt fure Science is to be had. By which properties \& comparafons of thefe two, more caffly may be defcribed, the ftate, condition, nature and property of thofe thinges, which, we before termed of a third being: which, by a peculier name alfo, are called Thynges CMathematicall. For, thefe, beyng(in a maner)middle, betwene thinges fupernaturall and naturall:are not fo abfolute and excellent,as thinges fupernatural: Nor yet fobafe and groffe, as things naturall: Butare thinges immateriall : and neuertheleffe, by materiall things hable fomewhat to be fignified. And though their particular Images, by Art,are aggregable and diuilible : yet the generall Formes, notwithflandyng, are conftant, vnchaungeable, vntráfformable, and incorruptible. Neither of the finfe, can they, at any tyme, be perceiued or iudged,Nor yet, for all Neither quall mynde of man, firft conceiued. But, furmountyng the imperfectió that, in the royall mynde of man, firit conceuued. But, jurmountyng the imperfectio of coniciture, weenyng and opinion:and commyng thort of high inteliectuali coeeptio,are the Mercuntal fruite of Dianaricall dichounc, in perfect imagination nubfiftyng. A meruaylous newtralitic haue thefe thinges chrathomaticall. and alio a fraunge participatoó betwene thinges fupernaturall, immortall, intellectual, fimple and indiubilitic and fenfible profe, may well feruc in thinges naturall:and is cominenProbabilitic and fenible profe, may well feruc in thinges naturall: and is cominen-
dable:In Mathematicall reafoninges, probable Argument, is nothyng regarded: dable: In Mathematicall reafoninges a probabe timony of fenfe, any whit credited : Bur onely a perfect demonftranor yet the teltimony of enfe, any whit credited : But onely a perfect dethes certaine, neceffary, and inuincible:vniuerfally and neceffaryly con-
swTO THE VNFAINED LOVERS of truthe, and conftant Studentes of Noble Sciences, IOHN DEE of London, hartily wifheth grace from heauen, and moft prof perousis fucefefs inall their boneff attemptes and exeridifs.


Iuine Plato, the great Mafter of many worthy Philofophers,
and the conftant auouchor, and and the contant auoucher, and
pithy perfwader of $\eta$ nom, Bo. nums, and Ens : in hisSchole and Academie, fandry times (befides his ordinary Scholers) was vifited of a certaine kinde of men, allured by the noble fame of Plate, and the great commendation of hys profound and profitable doctrinc. But when fuch Hearers, after long harkening to him, perccaucd, that the drift of his difcourfes iflied out, to conclude, this $V$ ntion, Bo-
nam, and Ems, to be Spirituall, Infinum, and Ens, to be Spintuall, Infi-
nite, Aternall, Omnipotent, \&c.
Nothyng beyng alledged or expreffed, How,worldly goods: how, worldly dignitie:how, health, Stregth or luftines of body:nor yet the meanes, how a meracilous fenfibleand bodyly blyffe and felicitie hereafter, might be arteyned: Straightway, lenfible and bodyly blyffe and felictie hereafter, might be atteyned: Susightway, ged:yca his doctrine wasby them defpifed:and his fchole, no more of them vifiged:ytahich thing, his Scholer, Arijfotle, narrowly cōfidering, fotnde the caufe therof,to be, For that they had no forwamyng and information, in generall, whereto'n his doctrinc tended. For, fo, might they haue had occalion, either to haue forborne his fchole hauntyng : (ifftey; then, had mifliked his Scope and purpofe) or conhis fchole hauntyng: (if they, then, had milliked his Scopeand purpole or con-
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Iohn Dee his Mathematicall Preface.
cluded:is allowed as fufficient foran Argument exactly and purely Mathematical. w
 nitade, Nember,we dcfine, to be, a certayne Mathematicall Sume, of $P$ nits. And, an Nurethererd
 whofe propetry, any thing, which is in deede, or is counted One, may refonably pe we Grever men and al indill and ailo induinble:becaufe, of it, marerially, Number doth confift: which, princ- ed, enmment. pally, is a thing Mathematicall. Magnitude is a thing Mathematticall, by participation Misnowive. of fome likents of whote nature, any thing is iudged long, broade, or thicke. A Thicke is ilfo broade, \& long. A , or ade mande we call a Suporfies or Plaine Eucry playne magnitude, hath alfo length. A long inagnitude, we terme a Linn. A Lucre is playne magnither thickenor broade, but onely long: Eucry certayne Line hath two
 endes: The cndes of a line, are Pointes called. A Point, is a thing Mattbematicall, indi- A poin uifible, which may hauc a certayne determined fituation. If a Poynt moue from a produced. whereupon, of the auncientMathematiciens, a Line is called the race or $\mathcal{A}$ Line. produced. whereupon, of the auncient Mathematiciens, a Lime is called the race or
courfe of a Point. A Poynt wedefine, by the name of a thing Mathematicall: courfe of a Point. A Poynt wedefine, by the name of a thing Mathematicall:
though it be no Magnitude, and indiuifible: becaufe it is the propre ende, and bound of a Line : which is a true Marnitrde. And Magnitade we may define to be Magmionde that thing Mathernatrall, which is diuifible for ener, in partes diuifible, long,broade that thing Mathenatfrall, which is diuitble for ener, in partes diuifble, long, broad ken ita thing Mathematicall(as I fayd) by reafon it is properly the end, and bound ken it a thi

Neither Number , nor CMagnitude, haue any Materialitie. Firf, we will conlid of Number, and of the Science Mathematicall, to it appropriate, called Aritbmetike: of Number, and of the Science Mathemattrall, to it appropriate, called Anitbmetike and afterward of Maguminde, and hus Science, called Geometrie. But that name conand free from all matter, Number is, who doth not perceane 〔 yea, who doth not and free from all matter, N wimber is, who doth not perceane ¿ yea, who doth no wonderfully woderat it:For, neither pure Element, nor Arifoteles, 2 ainta Efjentia;
is hable to ferue for Number, as his proprematter. Nor yet the puritic and fimple is hable to Ieruefor Number, as his proprematter. Nor yer the puntic and frmple And therefore the great \& godiy Philofopher Anitius Boctius, fayd:Ommis quecumg And therefore the great \& godly Philofopher Anitius Roetius, fayd:Ommia quacung fait principale in animo Conditoris Exemplar. That is: All thinges (volicl) from the very first originall benig of thinges, bane bene framed and made) do appeare to be Formed by the reafon of $N$ Numbers. For this was the principall example or patterne in the minde of the Creator. O comforrable allurement, O rauifhing perfwafion, to deale with a Science, whofe Subiect is fo Auncient,fo pure, fo excellent; fo furmounting all creatures, fo vfed of the Al mighty and incomprehenfible wifdome of the Creator, in the diftinct creation of all creatures: in all their diftinct partes, properties, natures, and vertues, by order and moftablolute number, brought, from 2 Sething, to the Formalitie of their being and State.By Numbers propertie therefore, of vs, by all poffible meanes, (to the perfection of the Science) learned, we may bothwinde and draw our felues into the inward and deepe fearch and vew, of all creatures diftinct vertues, natures, proper ties, and Formes:And alfo, farder,arife, clime,afcend,and mount vp (with Speculatiue winges) in fpirit, to behold in the Glas of Creation, the Farme of Formes, the Exemplar Nember of all thinges Nomerable;both vifible and inuifible : mortall ard

## Iohn Dee his Mathematicall Preface.

immortall, Corporall and Spinituall, Part of this profound and disine Science, had reachan the Propheficr atteyned vnto:by 2 eumbers Formall, Natsy all, and Ration comming, His bookes yet remainyng, hereef,are good profe:And the noble Earle of Niratidula, (befides that, ) a fufficient witneficithat loachim, in his prophefies, proceted $i_{1}$ fo otber pay, then $b_{7}$ 2 $v p 900$.Conclutions, in all kinde of Sciences, openly to be difputed of:and among thereft, in his Conclufions Waathematicall, (in the eleuenth Conclufion) hath in Lain, this Englifh fentencc. By Numbers, a way is had, to the faarchyng out, atud wnderfinstyg af ewery thyng, hable robe knowen, For the varifying of which Conclufion, I premis/ to annfivar re the 7 s. Quefions, wnder writen, by the way of $2 \mathrm{Nambers.Which} \mathrm{Co-}$ clufions, I omit here to rehearfe: afivell auoidyng fuperfluous prolixitie:as, bycaule lownines Prow, workes, are commonly had. But, in any cafe, I would wifh that thofe Conclufions were red diligently, and perceiued of fuch, as are earnett Obferuers and Confiderers of the confant law of nubers; which is planted in thyng Nacurall and Supematurallsand is preferibed to all Creatures, inuiolably to be iept.For,fo,befides many other thinges, in thofe Conclufions to be marked, is Wuald apeare, how fincerely, \& within my boundes, Idifclofe the wonderfall myferies, by numbers, to be atteyned vnto.

Of my former wordes, ealy it is to be gathered, that Number hath a treble flate: One, in the Creator:an other in euery Creature(in refpect of his complete conftirution: )aud the third, in Spirituall and Angelicall Myndes, and in the Soule of má. In the firit and chird flate, Nymber, is termed Number Numbryag. But in all Creazures, otherwife, Number, is termed Nüber Numbred. And in our Soule, Nüber beareth fuch a fivay $y_{y}$ and hath fuch an affinitie therwith: that fonne of the old Phile of phers taught, Mans Soule, to bea Number mounng it felfe. And in dedc, in vs, though it pea very Accident: yer fuch an Accident it is, that beforeall Creatures it had perfect beyng, in the Creator, Sempiternally. Number Nombrrng therfore, is the difcretion differning, and diftincting of thinges. But in God the Creator, This difererion, in the beginnyng,produced ordcrly and diftinetly all thinges. For his Num bnp $弓$, then, was his Creatyng of all thinges. And his Continuall Numbryng, of all thinges, is the Conferuation of them in being: And, where and when he will lacke an Inat: thereand then, that particular thyng fhalbe Dif cruated.Here I fay. But our Seucrallyng, diftinctyng, and Numbrgng, createth nothyng: but of Multitude confidered, maketh certaine and diffinct determination. And albeit thefe thynges be waighry and truthes of great importance, yet (by the infinite goodnes of the Almighry Jornarie, ) Artificiall Mcthods and ealy wayes are made, by which the zelous Philofopher, may wyn nere this Riverim Ida, this Mountayne of Contempla tion:and more then Contemplation. And alfo, though Number, be a thyng fo Immaxeriall,fo divine, and atemall:yct by degrees, by litle and litle, ftetchyng forth, aud applying fome likenes of it as firft, to thinges Spirituall: and then, bryngyng it lower, ro thynges fenfibly perceiued:as of a momentanye founde iterated:then to the leaft thynges that may be feen, numerable: And at length, (moit groffely, to a multitude of any corporill thynges feen, or felt: and fo, of thefe groffe and lenfible thynges, we are trayned to leame a certaine Image or likenes of numbers : and to vfe Arte in them to our pleafure and proffit.So groffe is our conuerfation, and dull is our apprehenfion:while mortall Senic, in vs, ruleth the common wealch of our litle world. Hereby we fay, Three Lyons, are three:or a Ternarie. Three Egles, are
three, or a 7 enerre. Which ${ }^{*}$ Temarries, are eche, the $V$ nion, knot, and $V$ miformitie, of :hree, or a 7 enerie. Which ${ }^{*} T$ embrries, are eche, the $V$ nion, knot, and $V$ nif ormitie, of
thirce dificte and diftinct $V$ nits. That is, we may in eche $T$ ernarit, thrife, feucrally poinre and thew a part, one, one, and ome. Where, in Numbryng, we fay One, two

## Iohn Dee his Mathematicall Preface.

Three. But how farre, thefe vifible Ones, do differre from our Indiuifible Vnite (in pure Arithmetike, principally confidered)no man is ignorant. Yet from thefe (in pure Arinmerike and materiall thynges,may we be led ypward, by degrees,fo, informyng our
 nor admixtyng any thyng created, Corporall or Spinituall, to fupport, conteyne, or
 the T rinttir moft blefied and xternall.
But farder vnderfland, that vulgar Practifers, hane Numbers, otherwife, in fundry Confiderations:and extend their name fardersthen to Numbers, whole leaft part is an Vnit.For the common Logitt,Reckenmafter, or Anthmeticien, in hys Vfing of Numbers:ofan Vnit, imagineth leffe partessand calleth them Fractions. As of an Vnit, he maketh an halfe, and thus noteth it $\frac{1}{2}$, aud fo of other, (infinitely dinerfe) partes of an I'vit. Yea and farder, hath, Fratfions of Fracliems. de And, forafmuch, as, Addition, Sabfiraltion, Multiplucation, Dinifion and Extraction of Rotes, are the chief, and fufficient partes of Arithmetike : which is, the Science that demonfra- Aribbretike teth the properties, of Numbers, and alleperatios, in nombers to be performed: How otten, os therfore, thefe fiue fundry fortes of Operations, do, for the moft part, of their cxe-", Note cution, differre from the fue operations oflike gencrall property and name, in our ". Whole numbers practifable, So often, (for a more diftinct doctrine) we, vulgarly en account and bane it,an other kynde of Arithmatike. And by this reafon:the Con- i. fiderarion, doctrinc, and working, in whole numbers onely: where, of an $V /{ }^{\text {mith}}$, is no leffe part to beallowed:is named (as it were) an Arnthmettke by it iclfe. And fo of the Arithmethle of Fralfions. In lyke forte, the neceffary, wondecfull and Secret doctrine of Proportion, and proportionalytic hath purchafed vnto it felfea peculicr 2. maner of handlyng and workyng:and fo may feme an other forme of Arithmettke. Moreouer, the Aitronomers, for fpede and more commodivus calculation, haue de- 3 .
uifed a peculier maner of orderyng nábers, about theyr circular motions, by Sexanifed a peculier maner of orderyng núbers,about theyr circular motions, by Sexagenes,and Sexagefmes.By Signes, Degrees and Minutes \& c c, which ccenmonly is called the Arithmetike of Aisonomical or Phificall Fyaffions. That, haue I bricfy noted, by the name of Arithmettike Circular, Bycaufe it is alfo vfed in circles, net Aftronomicall. ©c.Practive hath led Numbors farder, and hath framed them, to take vpon 4 them, the mew or Magnimesike, an $\%$ nit, is the common Meafure of all Numbers) nalitte, (Forin pore are become as Lyines. Playnes and Solides: fome Numbers.) And, here, Nübers are become, as Lynes, Playnes and Solides: fome tymes Rationall, fome tymes Irvationall: And haue propre and peculicr chatracters, (as $\sqrt[z]{ }+\frac{C}{}$. anid fo of other. Which is to fignifie Rote Square, Rote Cwbik: and fo forth: \& propre and peculier this, a diuerêe Arithmetike from thic other, Praelife bryngeth in, here, dituerfe comthis, a diuere Arithmettike from the omer, Practire bryngeth in, here, dituene com-
 diuenlly knit, by fighes, of More \& Lefle:as thus $\sqrt{5} 12+\sqrt{c e} 15$. Or thus $\sqrt{ } \% \delta^{2} 19$ $+\sqrt{c e} 12-\sqrt{8} 2 . \& 2 c$.And lome tyme with whole numbers, orfractions of whole Number, anóg them:as $20+\sqrt{8} 24 \cdot \sqrt{ } \cdot 16+33-\sqrt{8} 10 \cdot \sqrt{8} 34+12, \frac{1}{4}+\sqrt{C e g}$. And fo, infinitely, may hap the varietie, After this : Both the one and the other hath frattions incident:and fo is this Arithmetike greately enlarged, by diuert' exhibityng and vfe of Compofitions and mixtynges, Confider how, I (beyng defirous to deliucr the fudent from error and Cauillation)do giue to this Praltife, the nathe of the Arithmettike of Radicall numbers: Not, of Irrathendil or Strd them,

## IohnDee his Mathematicall Prxface.

them, which, A ithmetike of whole Numbers moft vfuall, would fay they had no fuch Roote:and fo account them Surd Nombers: which, generally fpoke, is vntrue as Euclides tenth booke may teach you. Therfore to call them, generally, Redicall Numbers,(by reafon of the ligne $\sqrt{ }$ 'prefixed, is a fure way: and a fufficient generall diftinction from all other ordryng and vfing of Numbers : And yet (befide all this)Confider : the infinite defire of knowledge, and incredible power of mans Scarch and Capacitye:how, they, ioyntly haue waded farder (by mixtyng of fpe culation and practife) and haue found out, and atteyned to the very chief perfection(almoft)of Numbers Practicall vfe. Which thing, is well to be perceiued in tha great Arithmeticall Arte of Aquation : commonly called the Rule of Coff. or Alge-
Ora. The Latines termed it, Regulam Rei \& Cenjus, that is, the Rule of the thyng and bis Dalue. With an apt name : comprehendyng the firt and laft pointes of the worke. And the vulgar names, both in Italian, Frenche and Spanifh,depend(in namyng it,)vpon the fignification of the Latin word, Res: $A$ thing:vnlcaft they vfe the name of Algebra. And therin(commonly) is a dubble crror. The one, of them which thinke it to be of Geber his inuentyng: the other of fuctias call it Algebra. For,firft, though Geber for his great fkill in Numbers, Geonetry, Aftronomy, and other maruailous Artes, mought haue femed hable to haue firft deuifed the fayd Rule:and alfo the name carryeth with it a very nere likenes of Geber his name : yce true it is, that a Greke Philofopher and Mathematicien, named Dioplonntus, befor Geber his tyme, wrote i3.bookes therof (of which, fix are yet extant : and I had them to * we, of the famous Mathematicien, and my great frende, Petrus CMonlailreus:) And fecondly, the very name, is Alguebar, and not Algebra as by the Aiabic Auicen,may be proucd: who hath thefe precile wordes in Latine, by Andreas Alpa gus(moft perfect in the Arabik tung ) fo tranflated. Scientia faciendi Algiebar of Almachabel. i. Scientia inucniendi numerum ignotwm, per additionem Numeri, \&े diwifio. nom ó equationem. Which is to fay:Tbe Science of workyng Algiebar and Al. machabel, that is, the Science of findyng an vnknowen number, by Addyng of a Number, o Dinifion © aquation. Here haue you the name : and alfo the prin cipall partes of the Kulc, touched. To name it, The rule, or Art of Aquation, doth fig. nifie the middle part and the State of the Rule. This Rule, hath his peculier Cha
5. rakers:and the principal partes of Arithmetike,to it appertayning, do differre from the other Arithmeticall operations. This Arithmetike, hath Nübers Simple,Cópound Mixt:and Fractions,accordingly. This Rule, and Arithmetike of Algiebar, is fo pro-
found, fo generall and fo(in maner) contcyneth the whole power of Numbers found, fogenerall and fo(in maner ) conteyneth the whole power of Numbers Application practicall:that mans witt, can deale with nothyng, more proffitable about numbers : nor match, with a thyng, more mete for the diuine force of the
Soulc, in humane Studics, affaires, or exercifes) to betryed in. Perchaunce you Soule,(in humane Studies, affaires, or exercifes)to be tryed in. Perchaunce you looked for, (long ere now, to hauc had fome particular profe, or euident teftimony of the vfe,proffit and Commodity of Arithmetike vulgar, in the Common lyfe and trade of men. Therto, then, I will now frame my felfe: Butheren grcat care haue, leaft length of fundry profes, might make you deme, that either I did mif
doute your zelous mynde to vertues fehole : or els miftruft your hable witts, by doute your zelous mynde to vertues fehole : or els miftruft your hable witts, by
fome,to geffe much more. A profe then, foure,fiue, or fix, fuch, will I bryng, as fome,togeffe much more. A profe then, foure,fiue, or fix, fuch, will I bryng, as any reafonable man, thenwith may be perfuaded, to loue \& honor, yea learne and exercife the excellent Science of Arithmetike.

And firt: who, nerer at hand, can be a better witneffe of the frute receiued by Aruthmettke, then all kynde of Marchants? Though not all, alike, either nede it,
vfe it. How could they forbeare the vfe and helpe of the Rule, called the Golden

## Iohn Dee his Mathematicall Praface.

Rule:Sinple and Compounde:5oth fowsandand backwarde Howmight they miffe Arithmectivall helpe in the Rules of Felowfhyp: either without tyme, or with tymerand betwene the Marchant \& his Fateror? The Bales of Bartering in wares onely:or part in wares, and part in mioney, would they gladly want "O-Our Marchant venturers, and Tranaylers ouer Sea, how could they order their doynges iufly and without loffe, vnleaft certaine and generall Rules for Exchauge of money, and Rechaunge,were,for theirvfe, denifed : The Rule of Alligation, in how fundry cafes, doth ie conclade for them, fach precife verities, as neitherby naturall witt, nor other experience, they,were hable, els, to know : And (with the Marchant then to make an end) how ample \& wonderfull is the Rule of Falle pofitions? efpecially as it is now, by two excellent Mathematiciens (ofmy familieracquayntance in their life time) enlarged !. I meahe Gomma Frifins, and Simon Iacob Who can eitherin brief conclude, the generall and Capitall Rules: or who can I magine the Myriades of fundry Cafes, and particular examples, in Act and earneft, continually wrought, tried and concluded by the forenamed Rules, oncly? How fundry other Arithmeticall pratifes, are commonly in Marchantes handes,and knowledge: They them felues, can, at large, teftifie.

The Mintmafter, and Goldfmith, in their Mixture of Metals, either of diuerfe kindes, or diuerfe values:how are they, or may they, exaltly be directed, and meruailoufly pleafured, if Arithmetike be their guide? And the honorable Phificials, will gladly confeffe them felues, much beholding to the Science of Arithmetike, and that fondry wayes : But chiefly in their Art of Graduation, and compounde Medicines. And though Galenus, Auerrois, Arnoldus, Lallas, and other haue publifhed their pofitions, afwell in the quantities of the Degrees aboue Temperament, as in the Rules, concluding the new Forme refulting : yeta more precife commodious, and eafy çethod, is extant:by a Countreyman of ours (aboue 200. yeares ago) inuented. And forafmuch as Iam vncertaine, who hath the fane: or when that litle Latin treatife, (as thi Author writit,) Shall come to be Printed: (Both to declare the defireI haue to pleafure my Countrey, wherin I may : and al. fo,for very good profe of Numbers vec, in this moft fubtile and frutefull, Philofophicall Conclufion, I I entend in the meane while, moft briefly, and with my farderhelpe, to communicate the pith therof vnto you.

Firt defcribe a circle : whole diameter let be an inch. Diuide the Circumfe rence into foure equall partes. Frob the Center, by thofe 4 , fections, extend 4 -right lines : eche of 4 inches and a halfe long: or of as many as you lifte, aboue 4 without the eircumference of the circle: So that they fhall be of 4 .incheslong (at the leaft) without the Circle. Make good enident markes, at eiery inches end If you lift, yout may fubdiuide the inches igaine into 10. or rz. fmaller partes, equall. At the endes of the lines, write the names of the 4 . principall elementall Qualities. Hote and Colde, one againft the other. And likewife CMoglt and Dry, one againft the other. And in the Circle write Temperate. Which T omperatture hattra good La tritude : as appeareth by the Complexion of man. And therefore we hauc allow ed vnto it the forelayd Circle : and nota point Mathernaticall orPhyficall.

Now, when you haue two thinges Mifcible, whofe degrees are * truely knowen: Ofneceffitie, either they are of one Quantitieand waight, or of diuerfe If they be of one Quantitic and waighit: whether their formes, be Contrary Qualities, or of one kinde (but of diaerle intentions andidegrees) or a T emperatc, and a bis booked Contrary, The forme refulting of their Mixture iss ivisthe Middle betwene the degrees of $Q$ - EJfentis.

Iohn Dec his Mathematicall Prxface.
she fanses mixt. As for example, lee 1, , be $M$ oiff in the firt degrec : and $B$, Dry in che third degree. Adde 1 . and 3 , that maketh 4 + the halfe or middle of 4 , is 2 .
 ucdnone . Andforit, youmult put a Ciphre, if at any time, it beia mixture).


Counting then from $B, 2$. degrees, toward $\mathcal{A}$ : you finde it to be Dry in the fir? degree : So is the Forme refuling of the Mixture of $A$, and $B$, in our example. I will geue you an other example. Suppofe, you haue two thinges, as $C$, and $D$ : and of $C$, the Heate to be in the 4 .degree : and of $D$, the Colde, to be remiffe, euen vnto the Temperament. Now, for C,you take 4 : and for $D$,you take a Ciphre-: which, added vnto 4 , yeldeth onely4. The middle, or halfe, whercof, is 2 . Wherefore the Forme refalting of $C$, and $D$, is Hote in the fecond de;ree: for, 2. degrees, accounted from $C$, toward $D$, ende iufte in the 2 . degrec of heate. Of the third $m 2$ ner, I will geuc alfo an example: which let be this: I haue a liquid Medicine whofe Qualitie of heate is in the 4.degree exaleed : as was $C$, in the example foregoing: Qud an other liquid Medicine I haue : whole Qualitie, is heate, in the firf degree. Of eche of thefe, I mixt a like quantitie : Subtract here, the leffe fró the more , and the rehdue diuide into two equall partes : Whereof, the one part, cither added
the leffe, or fubtraited from the higher degree, doth produce the degree of the

## Iohn Dee his Mathematicall Praface.

to be reduced: \& the Forme refultyng of the fame, toferue the turne) yet thefe Ru-
les aref fufficient:duely repeated and iterated. In procedyng firft, with any two:andthen, with the Forme Refulting, and an other:\& fo forth: For, the laft worke, concludeth the Fornerefultyng of them all: I nede nothing to fpeake, of the Mixture (here fuppofed) whatit is.Common Philofophic hath defined it, faying, whixtia fif mifobiuwn, alteratiorum, per minima coniunciornm, is of great importance. I nede notalfo fpend any time, to fhew, how, the other manner of diftributing of degrees, doth agree to thefe Rules. Neither nedeI of the farder vfe belonging ro the Croffe of Graduation(before defcribed) in this place declare,vnro fach as arecapable of that, which I haue all ready fayd. Neither place declare,vnro fuch as arecapable of that, which I haue all ready fayd. Neither rall Rules, to be ordered. The wirty and Studious, here, haue fufficient:And they rall Rules, to be ordered. The witry and Studious, here, haue fufficient:And they
which are not hable to arteine to this, withour liuely teaching, and more in partiwhlar:would haue larger difcourfing, then is mete in this place to bedealt withall: And other(berchaunce) with a proude fnuffe will difdaine this litle:and would be And other (perchaunce) with a proude fnuffe will difdame this litle:and would be
vnthankefu! for much more. I, therfore conclude : and wifh fuch as haue modeft andeaneft Pinlofophicall mindes, to laude God highly for this:and to Meruayle, and eameft Pimofophicall mindes, to laude God highly for this:and to Meruayle, ther Nathrall, is fo Marchtand maryed with the mont fimple, eaffe, and Diort way of the noble Rule of Algiebar. Who can remaine, therfore vnperfuaded, to loue, athe noble Rule of Algiebar. Who can remaine, therfore vnperfuaded, to loue, athat the lide finger of Arithmetike, is of more might and contruing, then a hunderd thoufand mens wittes, of the middle forte, are hable to perfourme, or truely to conclude, with out helpe thereof.

Now will we farder, by the wife and valiant Capitaine, be certified, what helpe he hath, by the Rules of Arithmetike:in one of the Artes to him appertaininge And " after the beft maner to all purpofes. This Artfo much dependeth vppon Numbers " vife, and the Mathematicals, that Aliamas ( the beft writer therof, ) in his worke, to the Emperear Hadriasus, by his perfection, in the Marhematicals, (beyng greatcr, the Emperour Hadrianus, by his perretion, in olde to paffe all other the excellent then other before him has,, thinketh his. Fooke tite had written Ameas : Cyneas of Theifaly: Pyrrlus Epretdiand Alexander his fonne:Clearchus: Paufanias : Euangelus:
 Polbrus, famlicr Ir cnde to Scipzo : Eupolemus: Ip Princes of Immortall fame and meotber worthy Capitaines, Philolophers and Princes of mmortali fame and memory: Whole fayrett toure of their garland (in tis feat) was areafmetike : and a nettke fand the Capitaine in great ftede. As in proportionyng of vittayles, for netkke ftand the Capitaine in great tede. As in proporcionyng orvitayles, for number of Souldiers :and for a certain ryme. Or by good Art to diminifh his comnumber of Soudiersiands, to make the viftuals, longer to ferue the remanent, \& for a certaine deterni. ned tyme: ifnede fo require. And fo in fundry his other accountes, Reckeninges, Meafurynges, and proportionynges, the wife, expert, and Circumfect Capituine will affirme the Science of Arithmetike, to be one of his chief Counfaylors, diretersand aiders. Which thing(bygood meanes) was cuident to the Noble, GT the Couragious, the loyall, and Curreous Iohn, late Earle of Warwicke. Who nes, force and Shill in Chiualrous feates and exercifes: his humblenes, and frendenes, force, and Skill in Chiualrous feates and exerciles:nis humblenes,and frendefotherwifr,)wertue had faftened in his breft, what Rules of godly and honorable

Iohn Dee his Mathematicall Prefface.
Formereffulting, by this mixture of $C$, and $E$. As, iffrom 4 . ye abate 1.thererefteth 3.the halfe of 3 . is $1 \div$ : Adde co 1 .this $1 \div$ you haue $2 \div$. Or fuburakt from 4 . this $1 \div$; you hauc likewife $2 \frac{1}{2}$ remayning. Which declareth, the Forme effil. ting, to be Heate, in the middle of the third degree.

Butif the Quantities of two thinges Commixr, be diterfe, and the Intenfi- $n$ The Seons (of their Fornes Miffible) bein diverfedegrees, and heigthes. (Whether' ", cond thofe Formes be of one kinde, or of Contrary kindes, or of a Temperate and a "Rale Contrary, What preportion is of the lefle quantitie to the greater, the fame /hall be of the "" difforenes, which is betwene the degree of the Fermerefulting, and the degrec of the greater" gadatitie of the thing mif cible, to the difference, whith is betwene the jame degree of the " Forme ref alting, ond the degree of the loße quantitic. As for example. Lee two pound"," of Liquor be geuen, hote in the 4 . degrec: \&c one pound of Liquor be geuen, hote" in the third degree. I would gladly know the Forme refulting, in the Misture of ", thefe two Liquors. Set downe yout nutbersin order, thus.
Now by the rule of Algiebar, haue I deuifed a very eafie, 5. 2. Hote. 7. bricfe, and generall mancr of working in this cafe. Let vs firf, fuppole that Middle Forme reffilting, to be ire: as that Rule teacheth. And becaufe (by our Rule, here geuen) as
the waightof x is to 2 : So is the difference betwene 4 (the the waight of x .is to 2 : So is the difference betwene 4 . (the
degree of the greater quantitie) and 1 ve . to the difference bet (the degree of the thing tolefie and (the degree of the thing, in leffe quátitie. Ărd with all, $17 e$, being alwayes in a certaine middell, betwene the two heigthes or degrees). For the firt difference, Ifet 4-1ze: and for the fecond, I fet 1 ye, 3 . And, nowy againe, I fay, as n .is to 2 .fois 4-1\%e to Ize-3. Wherfore, of thefe foure proportionall numbers, the firftand
the fourth Multiplied, one by the other do make as mich as the fecond and the third Multiplied the one by werner dingly. And of the firtand the other. Lerthele Multiplications be made accorthird $8-2$ e. Wherfore, our Aquation is berwene $1 \%-3$ and $8-2 z_{0}$. Which may be reduced, according to the Arte of Al giebar:as, here adding 3,to eche part, geueth the Aqquation,thus, ize $=11-2$ re $^{2}$. And yet againe, contracting, or Redugeneth the Æquation, thus, rye $=11-2$ Ye. And yet againe, contracting, or Reduted $3^{\text {te }}=\mathrm{II}$. Wherefore, difuiding in by 3 : the Quotient is $3 \geq$ : the Valfov ofour re Cof r Thing firf Ize, Colf, or $T$ hing, firtfuppofed. And that is the heigth, of Intenfion of the Ferme rfaw, whichk, Ahant in thew of the worke in conclufion, thus. The proufe hercof is eafie-by fubtracting 3 .from $3 \frac{1}{7}$, refteth
$\frac{1}{3}$, Subtracte the fame heigth of the
Forme refilting, (which is $3 \frac{i}{\text { r }}$ ) fro 4 then refleth-

is double to $\frac{i}{2}$
as 2. P. is double to I.R. So fhould it be : by the rule heregenen. Note. As you ad ded to echepart of the Aqquation, 3 : Fo ifyefirft added to eche part $2 z e$, it would
 ly, mo though 1, here, peake onely of rwo thyngs Miscable: and molt common.iiii.

## Iohn Dee hisMatherháticall Preface.

life he had framed to him felfe:swat vices, (in-fome then liuing) rotable, he tooke great care to eichew:what manly vertues, in,other noble men, (fionibing.before his cyes, )he Sythingly af pired atter : what prowefles he purpoled and mentto a chicue: with what feats and'Artes, he began tofurnifh and fraught himelfe, for the better feruike of his Kyng and Countrey, bothinpeace \& warre. Thefe (Ifay) his Heroicall Meditations, forecallinges and dererminations, no twaype; (I thinke befidemy felfe, canfo perféety, and truely report. And therfore, t Cops cience, I countitmy patt, for the honor, prefenment, \&e procuring of vertue (thas, briefly) to hine puthisNamé, in the Registeros Eanze Inmortall.
To our purpofe. This Iobn, by onc of his actes (befides many other: both in $\mathrm{En}_{n}$ gland and Fraunce, by me, in him noted.) did difclofehis harty loue to verruous Sciences;and his noble inten, to excell in Martiall proweffe; When he, with hamble requelf, and inftant Solliciting:got the beft Rples(citherin time paft by Greke or Romaine, or in our tine ved: and new Straragemes therin deuifed) for ordring of all Coinpanies, fummes and Numbers of me, (Many, or few) with onekinde of weapon,ormo, appointed;with Artillery, or without:on horebacke, or on fote: to giue, or take onfer ; to leem many, being few: tofeem few, being many. To marche in battaile or Iónay:with many fuch Feates sto Foughten field,Skarmoufh or Amburhic appartaining: Avid of all thefe, liuely defgnczinentes (molt curioufly) to bein velame parchement defcribed; with Notes \& peculier markes,as the Arte requircthiand all thefe Rules, and deferiptions Arithmeticill, inclofed in a riche Earle,dyed Cafe of Gold, hevied to weare abour his necke, ass his Iuell moft precious, and Anoo. if s 4. Counfaylour moft trufty. Thus, drithnetike, ofhim, was Shryned inigold: Of Numbersfrute, be had good hope. Now, Numbers therfore innumerable, in TKmbers prayfo his drynce liall finde.

What nede I, (for farder profe to you) of the Scholemafters of Iuftice, to require teftimony:how nedefull, how frutefull, how fkllfull a thing efrithonetike is? I meane, the Iawyer's of fll fortes. Vndoubredly, the Civilians, can meruayloufly decfare; how, ncither the Auncient Romane lawes, without good knowledge of $N$ woders art, can be perceiped : Nor (Iuftice ininftnite Cafes) withour due pro portion, (narrowy conifidered,) is hable to be executed. How Iuftly, \& with great knowledge of Atte, did Papmanssin fitute a law of partition, and allowance, betweneman'and wife after a diúorce?But how Accarj futs, Baldus, Baptolus, Iafon, Alexardider, and finally Alciathus, (being otherwife, notably,well learned) do iumble,geffe, and erre,from the $x$ quity, att and Intent of the lawmaker : Avithmetike can dete $A$, and conuince: andiclercly, make the cquth to Shine. Good Bartolits, tyred in the examining \& proportioning of the matter:and with Accurfius Gloffe, much cumbred:burfouc, and fayd: Nulli eff in tota hibro; Bac glo (fa difficilior: Cuins computatianem net Sobpleffici inc Doctiones intelfigust. ©'c. That is: In the whole booke, there is $n 0$ Glo/fe harder then this: Whofe arcomnpt or reckenying, neither the Scho. lers, ïtr the Doetours miderftand. \&cG. What can they day of Inlianus law, $s i$ ite scriphian, do. Of the Teftators willigfty performing, betwene the wife, Sonne and daughter : How can they perçeiue the aquatie of Aphricanus, Arithmeticall Reckenings, where he treateth of Lex Falcidras: How, catto they deliver hitn, from his
 How Iuftly and artificially, was if riothis reckering madee Proportionating to the
Sommes bequeathed, the Contriburions of ecke purt Namely for the hundred Sommes bequeathed, the Contribunions of eche part Namely, for the hundred $\frac{4}{7}$ : which make the 30 :which were tobe contibated by tric legataries ro the heire.

## Iohn Dea his Marhemacicall Praface.

For, what proporion, 100 hath to 75 : the fame hath $17 \div$ to $12 \div$ : Which is Serquitertia:that is, as 4 , $\mathbf{\text { to }}$ 3.which make 9 . Wonderfull 'many places, in the Ciuile Law, require an expert Arithmeticien, to vnderfand the deepp Ludgemét,\& Iuft determinarió of the Auncient Romaine Lawmakers. But much more expert ought he ro be, who thould be hable, to decide with xquitie, the infinite varictic of Cafes, which do, or may happen, vnder cuery one of thof lawes and ordinances Ciuile. Hereby, eafelly, ye may now coniecture: thatin the Canon law: and in the hawes of the Realne (which with vs, beare the chice Authoritic), Juftice and equity mightbe greately preferted, and Kilfully execured, through due fkill of Arithmerike, and proportions appertainyng. The worthy Philolophers, and prudent lawnakers (who haue writen many bookes De Repultic: How the beff fate of Cominon wealthes might be procured and mainteined, ) haue very well deter-
mined of Iuftice: (which, not onely, is the Bafe and foundacion of Common weales:but alfo the totall perfection of all our workes, words, and thoughtes:) de-
$\cdots$ fuing it, to be that vertuc, by which, to euery one, is rendred, that to him appertai. neth. God challengeth thisat our handes, ro be honored as God: ro beloued, as afriher : to be fearcd as a Lord \& mafter. Onr neighbours proportio, is alfo prefcribed of rine Almighty lawmaker: which is, to do to othcr, eucn as wewould be done vato. Thefe proportions, are in Iuftice neceffary:in duety, commendable: and of Common wealthes, the life, frength, tay and florifling. Arifotle in his E:hhkes (rof fatch the fede of Iufice, and light of direction, to vie and execute the fance; was fayne to fy to the peffection, and power of Numbers: for proportions Arithinsticall and Gcomctricall. $P$ theto in his booke called Epinemis ( which boke, is the Ttreafury ofall his doetrine) wherre, his purpofe is, ro ecke a Science, which, when a man had it,perfextly:hemight feme, and fobe, in dede, Wijfe. He, bricfly, of other Sciences difcourfing, findeth them, not hable to bring it to paffe: But of the Science of Numbers, he fayth. Illa, que mumerww mer talium generidedit jid prof flo of fciet Deam axtem aliquem, masug guam forrunam, ad falutem nofiram, hoc munks nobis

 kymde number, fhallbe able to brong it to paffe. And, Ithinke, a certaine God, rather then fortune, , baue ginen 2s this gift, for our bliffe. For, why fould we not Indge bim, upho is the Author of all good things, to be alfo the canfe of the greatef goodtlyng, namely, wi:fedome? There, at length, he proueth Wifedome to be atteyned, by good Skill of Nombers. With which great Teftimony, and the manifola profes, and reafons, before expreffed, you may be fufficiently and fully a:! Sclences, next to $\tau$ heologie, it is mof diuine, moft pure, moft ample and generall, mof profounde, moft tubrile, moot commodious and noof neceffary. Whofe next Sifter, is the Abfolute Science of Magnitudesiof which ( by the Direftion and aide of him, whoofe ctagnitude is Infinite, and of vs Incomprehenfible) I now entend, fo to write, that both with the cMultitude, and alfo with the Magnitude of Meruaylous and frutefull verities, you ( my frendes and Countreymen) may be fird vp, and alvaked, to behold what certaine Artes and ciiences, (to ourvn-
focakable behofe) our heaucnly father, hath for vs prepared, and revealed, by funIpcakable bchofe) our heaucnly father,
dry Pbilo ophors and © Mathematiciens.
BOth, Number and uxagnitude, haue a certaine Originall fede, (as it were) of an BOth, Number and UHagnitude, haue a certaine Originall fede, (as it were) of an Number, an Vnit,and of Magnitude, Poynte, doo feene to be much like Origi-

## Iohn Dee his Mathematicall Præface.

pretence of iuft conrent, and meafure) thofe landes and groundes : greatloffe, dif. quictnes, murder, and warre did(full oft)enfuc: Till, by Gods mercy, and mans In. duffrie, The perfeat Science of Lines, Plaines, and Solides (like a diuine lufticier,) gaue vnto cucry man, his ownc. The people then, by this art pleafured, and grearly relieued, in their landes iuft meafuring:\& other Philofophers, writing Rules for ly relicued, in thcir landes iuft mearuring:s other Philofophers, writing Rules for
lind meafuring. betwene them both, thus, confirmed the name of Geomerria, that is, (according to che very etimologie of the word) Land meafuring. Wherin, the people knew no farder, of Magnitudes ve, but in Plaines:and the P Pilofophers, of thè, ple knew no farder, of Magnitudes vie, but in Plaines :and the Philofophers, of thé, trie. And dhough, thefe Philofophers, knew of farder vfe, and beft vnderflode the tric. And dhough, there Philotophers, knew of farder vie, and bett vnderflode the
etymologye of the worde, yet this name Geometris, was of them applyed generally ctymologye of the worde, yet this name Ceommerisi, was of them applyed generally
 them, studrum quod circa plunam verfatur. But, well you may perceine by Enclides Elementes, that more ample is our Science, then to meafure Plaines:and nothyng lefie therin is tought(of purpofe) then how to meafiure Land. An other name, therforc, mult nedes be had, for our Mathematicall Science of Magnitudes : which regardeth neither clod,nor turff: neither hill, nor dale: ncither carth nor heauen: bur is alifolute Mreget/ ofogsian not creping on ground, and daffeling the eye, with pole O" perche,rod or lyne but lifyng the hart aboue the heauens, by inuifible lincs, and n fo procurcth Ioye, and perfection vnfpcakable. Of which true vfe of our etege. thict,or CMrgethelogia, Divine Plato fecmed to hạue good rafte, and iudgenent; and (by the name of Gcometrrie) fo noted it and warned his Scholers therof a as, in hys feuenth Diteloz, of the Conimon wealth, may euidently befine. Where (in Latin)thus it is:right well tranlated: Profecto, nobis hoc non mestbunt, 2uicunǵ. vel pasu-
 logvantur, qui in in ifaverfantur. In Englifh, thus. Verel) (fayth Plato) solofofoeuer b tue, (but enen Dry litle) tafted of Geometrie, will not denje 2uto vs, this: but that this Science, is of an other condicion, quite contrary to that, which they that are exercifedin it , do speake of it. And there it followeth, of our Geametre,

 Veritutem, minnun atjist, ad Philo ophlandum preparabit cogitationem, vt ad fupera con-
 pratipiendunn flf, vi gui preslanf faman hanc habität Crvitutem, nullo modo, Geometriam fpernant. Nam or que prater p fius propofitum, quodam modo off evidentur, haud exigua
 the knowyng of that, which is ever:and not of that, which, in tyme, both is bred and is broighbt to an ende. © c. Geometrie is the knowledge of that which is ener. laffyng. It will lift $\geqslant p$ therfore ( 0 Gentle Syr) our mynde to tbe V eritie : and by that meanes, it will prepare the $T$ bougbt, to the Pbilofoplicall lowe of wifdome:
 now, otherwifc then becommeth 2s, we calt down on ba/c or inferior things. ©c. Chiefly, therfore, Commaxindement muft be given, that fuch as do inllabit this mo/t honorable (itie, byno meanes, despife Geometrie. For cuen thofe thinges wheb wh which, in manner, feame to be, befide the purpofe of Grometrie: : are of

Iohn Dee his Mathematicall Preface.
nall caufes : But the dinerfitic neuertheleffe, is great. We defined an $V$ nit, to bea thing Mathematicall Indiuifible: A Point, likewife, we fayd to be a Ma thematicall thing Indiuifible. And farder, that a Pointmay haue a certaine de termined Situation: that is, that we may affigne, and prefcribe a Point, to be here there, yonder. \&ec. Herein, (behold) our Vnit is free, and can abyde no bon dage, or to be tyed to any place, or leatiduaifble or indiulible. Agayne, by reaplace and from a place) is to a Point incident and appertainyng. But an $V_{n i t}$, can place, and from a place) is to a Point incident and appertainyng. But an $V$ nit, can not be matically, line:(as we fayd before) which is the firt kinde of Magnitudes, and thematically, line:(as we fayd before) which is the firt kinde of Magnitudes, and moft fimple:An $V$ nit, can not produceany number. A Line, thoughit be produced of a Point moued, yet,it doth notconfilt of pointes : Number, thoughitbe formally, Number, is the Vnion, and Vnitie of Vnits. Which vnyring and knit formally, Number, ts the Vnion, and V nitie of Vnits. Which vnyting and knit- Numbtre keth a Number: by vniformitie, refulting of a certaine multitude of $V$ nits. And $f o$, euery number, may haue his leaft part,giuen:namely, an Vnit:But not of a Magnitude, (no, notof a Lyne, the lealt part can be ginet:bycaufe, infinitly, diuifiontherof, may be conceiued. All Magnitude, is either a Line, a Plaine, or a Solid. Which Line, Plaine, or Solid, of no Senfe, can be perceiued, nor exactly by hād (any way) reprefented:nor of Nature produced: But, as (by degrees) Number did come to our perceiuerance: So, by vifible formes, we are holpen to imagine, what our Line Marbematicall, is. What our Point, is.So precife, are our Magnitudes; thatone Line is no broader then an other:for they haue no bredth : Nor our Plaines have any thicknes. Nor yet our Bodies, any weight:be they neuer fo large of dimenfió. Our Bodyes, we can haue Smaller, then either Arte or Nature can produce any : and Greater alfo, then all the world can comprehend. Our leaft Magnitudes, can be diuided into fo many partes, as the greateft. As, a Linc of an inch long, (with vs) may be diuided into as many partes, as may the dameter of the whole world, from Eaft to Weft : orany way extended: What priuiIedges, aboue all manual Arte, and Natures mighr, haue our two Sciences Mathematicallsto exhibite, and to deale with thinges of fuch power, liberty, fimplicity, puritie, and perfection! And in them,fo certainly, fo orderly,fo precilely to procederas, excellent is that workemã Mechanicall Iudged, who nereft can approche to the reprefenting of workes, Mathematically demonftrated: And our two Sciences, remaining pure, and abfolute, in their proper termes, and in their owne Mat-
terito hauc, and allowe, onely fuch Demonftrations, as are plaine, certaine; vniuerfall, and of an aremall veritye: This Science of Magnitmde, his properties, con ditions, and appertenances : commonly, now is, and from the beginnyng, hath of all Philofophers, ben called Geonetric . But, veryly, with a name to bafeand fcant, for a Science of fuch dignitie and amplenes. And, perchaunce, that name, by cómon and fecret confen, of all wifmen, hitherto hath ben fuffred to tentayne that it inight cairy with it a perpetuall.nemorye, of the firft and notablef benefite, by that Science, tô commonpeop"d ffèwed : Whick was", when Boundes and inceres of land and ground were lof, and confounded (as jn' EBopt, yearely, with fic ouctflowyng of Nilus, the greateftandlongeft riuer in the world) or, that ground bequearhed, were to be affigned;ot; ground fold, were to belayd out: or (whien diforder preazided sthat Commós wcre diffributed into feueralties. For, where, vpon thefe \& fach like oecaliós, Some by ignoráce, fome by negligéce, Some by frapde,
and founc by viotence, did wrongfully limite, meafure, encroach,or challenge (by and fomte byviotence, did wrongfully limite, meafure, encroach, or chalfenge (by

## Iohn Dee his Mathematicall Preface.

nofmallimportance. ©c. And befides the manifold vies of Geometrie, in matters appertaiayng to warre, he addeth more, of fecond vnpurpofed frute, and commo dityc,arriling by Geometrie:faying:Scimus quin etiam, ad Difciplinas omnes facilius per
 drimam, fcondolocodif cendam Inuenibus fatuamus. That is. But, al/o, we knove, that for the more ealy learnyng of all Artes, it importeth much, wolether one baue any knowledge in Gcometrie, or no. ©C. Let ps therfore make an ordinance or decree, that this Science, of young men fhall be learned in the fecond place. This was Diwive Plato his Iudgement, both of the purpofed, chief, and perfect vfe of Ceometrie: and of his fecond, dependyng, deriuatiue commodities. And forvs, Chniten men, thoufand thoufand mo occafions are, to haue nede of tions and Myndes, by lite and litle, to forfake and abandon, the groffe and corruptible Obiectes, of our vtward fenfes : and to apprehend, by fure doctrine demontible Obicacs,ofourveraricall. And by them, readily to be holpen and con ftratiue, Things Mathematicall. And by them, readily to be holpen and conducted to conceiue, difcourfe, and conclude of things Intellectual, Spirituall,
xternall,and fuch as concerne our Bliffe euerlafting: which, otherwife (without $x$ ternall, and fuch as concerne our Bliffe euerlatting: which, othenvie ( without
Speciall priuiledge of Illumination, or Reuelation fro heauen) No mortall mans wyt(naturally) is bable to reach vnto,or to Compaffe. And, veryly, by my fmall Talent(from aboue)I am hable to proue and teftifie, that the litterall Text, and or der of our diuine Law, Oracles, and Myfteries,require more fkill in Numbers, and Magnitudes : then(commonly) the expofitors haue vttered : but rather onely (at the moft)fo warned: \& fhewed their own want therin.(To name any, is nedeles: and to note the places, is, here, no place: But if I be duely afked, my anfwere is ready.) And without the litterall, Grammaticall, Mathematicall or Naturall verities of fuch places, by good and certaine Arte,perceiued,no Spirituall fenfe (propre to thofe places, by Abfolute $T$ heologie) will thereon depend. No man, therfore, can " doute, but toward the atteyning of knowledge incomparable, and Heauenly, Wifedome: Mathematicall Speculations, both of Numbers and Magnitudes: are ," meanes, aydes, and guides:ready, certaine, and neceffary. From henceforth, in ", this my Preface, will I frame my talke, to Plato his fugitiue Scholers:or, rather, to fuch, who well can, (and alfo wil), vfe their vtward fenfes, to the glory of God, the benefite of their Countrey, and their owne fecretcontentation, or honeft preferment, on this earthly Scaffold. To them, I will orderly recite, defcribe \& declare 2 great Number of Årtes, from our two Mathematicall fountaines, deriued into thefieldes of Nature. Wherby, fuch Sedes, and Rotes, as lye depe hyd in the grouid of Neture, are refrefhed, quickened, and prouoked to grow, fhote vp, floure, and gue frute, infinite, and incredible. And thefe Artes, fhalbe fuch, as vpon Mag. nitudes properties do depende, more, then vpon Number. And by good reafon we may call them Artes, and Artes Mathematicall Deriuatiue : for (at this tyme) I Define An Arte, to be a Methodicall cóplete Doctrine, hauing abundancy of fufficient, and peculier matter to deale with, by the allowance of the Metaphificall Philofopher : the knowledge whereof, to humaine ftate is neceffarye. And that Iaccount, An Art Mathemati- Ant Matbecall deriuatiue, which by Mathematicall demonftratiue Method, matisum. in Nübers, or Magnitudes, ordreth and confirmeth his doctrine, as much $\&$ as perfectly, as the matter fubiect will admit. And for that,

I entend
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$\qquad$


## Iohn Dee his Mathematicall Praface.

A Kecha
I entend to vfe the name and propertic of a Mechanicien, otherwife, then(hitherto) it hath ben vfed, I thinke it good, (for diftinction fake) to giue you alfo a brief defcription, what I meane therby. A Mechanicien, or a Mechanicall workman is he, whofe fkill is, without knowledge of Mathematicall demonftration, perfectly to worke and finifhe any fenfible worke, by the Mathematicien principall or deriuatiue, demonftrated or demonftrable. Full well Ikriow, that he which inuenteth, or maketh thefe demonftrations, is generally called 1 §pecalatiue c Mechanicien : which differreth nothyng from a Mechanicall erasthematicien. So,in refpect of diuerfeattions,one man may haue the name of fundry artes: as, fome tyme, of a Logicien, fome tymes (in the fame matter otherwife handled) of a Rethoricien. Of thefe trifles, I make, (as now, in refpect of my Preface,)fmall account:to fyle thé for the fine handlyng of fubtile curious difputers. In other places, they may commaunde me, to giue good reafon:and yet, here, I will not be vnreafonable.

Firt, then, from the puritic, abfolutenes, and Immaterialitic of Principall Gee-
I. metrie, is that kinde of Geometrie deriued, which vulgarly is counted Geometric: and is the Arte of Meafuring fenfible magnitudes, their iuft quátities and contentes. This, teacheth to meafure, either at hand: and the practifer, to be by the thing Meafured: and fo, by due applying of Cumpafe, Rule, Squire, Yarde,Ell,Perch,Pole, Line, Gaging rod,(or fuch like inftrument)to the Length

1. Plainc, or Solide meafured, "to be certificd, either of the length, perimetry, or diftance lineall: and this is called, checometric. Or ${ }^{*}$ to be certificd of the content of any plaine Superficies : whether it be in ground Surucyed, Borde, or Glaffe mea. fured, or fuch like thing: which meafuring, is named Embadometric. "Or els to vnderftand the Soliditic, and content of any bodily thing : as of Tymber and Stone, or the content of Pits,Pondes, Wells, Veffels, fimall \& great, of all falhions. Where, of Wine, Oyle, Becre, or Alc veffells, \&ec, the Mcafuring, commonly, hath a peculier name:and is called Gaging. And the gencrall name of thefe Solide meafures,
2. is Stercometrie. Or els, this vulgat Geometrie, hath confideration to teach the practifer, how to meafure things, with good diftance betwene him and the thing mea1. fured : and to vnderftand thereby, cither *how Farre, a thing feene(on land or wa2. ter) is from the meafurer: and this may be called Apomecometric: Or,how High or depe, abouc or vnder the leuel of the meafurers ftiding, any thing is, which is fene - on land or water, called Hypfometrie. *Or, it informeth the neafurer, how Broad any thing is, which is in the meafurers vew: foit be on Land or Water,fituated:and may be called $P$ latometrie. Though I vee here to condition, the thing meafured, to be on Land, or Water Situated: yet, know for certaine, that the fundry heigthe of Cloudes, blafing Starres, and of the Mone, may(by thefe meanes) haue their diftances from the earth : and, of the blafing Starres and Mone, the Soliditie (afivell as diftances) to be meafured: But becaufe, neither thefe things are vulgarly taught: nor of a common practifer fo ready to be executed : I, rather, let fuch meafures be reckened incident to fome of our other Artes, dealing with thinges on high,more purpofely, then this vulgar Land meafuring Geometrie doth : as in Perfoeffiue and Aitronowic, \&oc.
$\mathrm{O}^{\mathrm{F}}$ thefe Feates (farther applied) is Sprong the Feate of Geodefie, or Land Meafuring: more cunningly to meafure \& Suruey Land, Woods, and Waters, of England and Ireland (whether through ignorance or fraude, I can not tell, in

## Iohn Dee his Mathematicall Prxface.

particular places of daungers, conteyned within the boundes, and Sea coaftes defcribed: as, of Quickfandes, Bankes,Pittes,Rockes,Races, Countertides, Whorlepooles. \&c. This, dealeth with the Eement of the water chiefly : as Geographie did principally take the Element of the Earthes defcription (with his appertenances ) to taske. And befides thys, Hydrographie, requireth a particular
Regifter of certaine Landmarkes(where markes may be had)from the fea, well haRegifter of certaine Landmarkes(where markes may be had)from the fea, well ha-
ble to befkried, in what point of the Seacumpafe they appeare, and what apparent ble to be fkried, in what point of the Seacumpafe they appeare, and what apparent forme,Situation,and bignes they haue, in refpecte of any daungerous placein the what way, the Tides and Ebbes, come and go, the Hydrographer oughtto recorde. The Soundinges likewife : and the Chanels wayes:their number, and depthes ordinarily, at ebbeand flud, ought the Hydrographer, by obleruation and diligence of Meaforing, to haue certainly knowen. Ând many other pointes, are belonging to perfecte Aydrographite, and for to make a Ratter, by : of which, I nede not here fpeake : as of the defcribing, in any place, vpon Globe or Plaine, the 32 .pointes of the Compafe, truely: (wherof, fcarfly foure, in England, hauc right knowledge: bycaufe, the lines therof, are no ftraight lines, nor Circles.) Of making due proiection of a Sphere in plaine. Of the Variacion of the Compas, from true Northe: And fuch like matters (of great importance, all) I leauc to feake of, in this place: bycaufe, I may feame (al ready) to haue enlarged the boundes, and duety of an Hy dographer, much more, then any man (to this day)hath noted, or preferibed. Yet am I well hable to proue, all thefe thinges, to appertaine, and alfo to be proper to the Hydrographer. The chief vfe and ende of this Art, is the Art of Nauigation: but it hath other diuerfe vfes : euen by them to be enioyed, that neuer lacke fight of land.

Stratarithmetrie, is the Skill, (appertainyng to the warre, ) by which a man can fet in figure, analogicall to any Geometricall figure appointed, any certaine number orfumme of men:of fuch a figure capable: (by reafon of the vfiall fpaces betwene Souldiers allowed : and for that, of men, can be made no Fractions. Yet, neuertheles, he can order the giuen fumme of men, for the greateft fuch figure, that of them, ca be ordred) and certific, of the ouerplus: (if any be) and of the next certaine fumme, which, with the ouerplus, will admit a figure exactly proportionall to the figure affigned. By which Skill, alfo; of any arny or company of men : (the figure \& fides of whofe orderly ftanding,or array, is knowen) he is able to expreffe the iuft number of men, within that figure conteined:or(orderly ) able to be conteined. * And this figure, and fides therof, he is hable to know : either beyng by, and at hand:or a farre of. Thus farre,ftretcheth the defcription and property of Stratarithmetrie: fufficient for this tyme and place. It differreth from the Feate twene Stra-", fight, to what purpofe he fo ordreth the men: and Skill full hability, alfo, for
occafion,or purpofe, to deuife and vfe the apteft and moft neceflary order', array and figure of his Company and Summe of men . By figure, I meane: as, either of a Perfelt Square, Triangle, Circle, onale, long fquare, (of the Grekes it is called Eteromikes) Rhombe, Rhomboid, Lwnular, Ryng, Serpentine, and fuch other Geometricall figures: Which, in warres, haue ben, and are to be vfed : for commodioufnes, ne-
ceffity, and auauntage \&cc. And no fmall fkill ought he to haue, that fhould make ceffity, and auauntage \&c. And no fmall fkill ought he to haue, that fhould make
true report, or nere the truth, of the numbers and Summes of footemen or horfetrue report, or nere the truth, of the numbers and Summes, of footemen or horfe-
men, in the Enemyes ordring. A farre of, to make an eftimate, betwene nere men, in the Enemyes ordring. A farre of, to make an eftimate, betwene nere
termes of More and Leffe, is not a thyng very rife, among thofe that gladly would

## Iohn Dee his Mathematicall Prxface.

by vntrue meafuring and furueying of Land or Woods, any way. And, this I am fure: that the Value of the difference, betwene the truth and fich Surueyes, would haue bene hable to haue foúd (for cuer) in eche of our two Vnimerfities, an excellent Mathematicall Reader:to eche,allowing (yearly)a hundred Markes of lawfull money of this realme: which, in dede, would feme requifit, here, to be had(though money of this realme:which, in dede, would feme requifit, here,to be had (though by other wayes prouided for) as well, as, the famous V niuerfitic of Paris, hath two
Mathematicall Readers : and eche, wo hundreth French Crownes yearly, of the French Kinges magnificent liberalitie onely. Now,againe, to our purpofe returning: Moreouer, of the former knowledge Geometricall,are growen the Skills of Geographic, Chorographic, Hydrographie, and Stratarithmetric.
Geographie teacheth wayes, by which, in füdry formes,(as Sphaerike, Plaine " or other), the Situation of Cities, Townes, Villages, Fortes, Caftells, Mountaines, ", Woods, Hauens, Riuers, Crekes, \& fuch other things, vpo the outface of the earth- " y Globe (either in the whole, or in fome principall méber and portion therof có- " tayned) may be defcribed anddefigned, in cómenfurations Analogicall to Nature ", and veritic:and moft aptly to our vew, may be reprefented. Of this Arte how great " pleafure, and how manifolde commodities do come vnto vs, daily and hourely: of noft men, is perceaued. While,fome, to beautifie their Halls, Parlers, Chambers, Gaicries,Studies,or Libraries with:other fome,for thinges paft, as battels fought, carthquakes, heauenly fyringes,\& fuch occurentes, in hiftories mentioned: therby iuely, as it were, to vewe the place, the region adioyning, the diftance from vs: and fuch other circumftances. Some other, prefently to vewe the large dominion of the Turke : the wide Empire of the Mofchouite: and the litle morfell of ground the Turke : the wide Empire of the Morce Chrifendome(by profeffion) is certainly knowen. Litle, I fay, in refpecte of the reft. \&c. Some, either for their owne iorneyes directing into farre landes: or to vnderftand of other mens trauailes. To conclude, fome, for one purpofe : and forne,for an other, liketh,loueth, getteth, and vfeth, Mappes, Chartes, \& Geo* graphicall Globes. Of whofe vfe, to fpeake fufficiently, would require a booke peculiet.

Chorographie feeneth to be an vnderling, and a twig, of Geographie : and yetneuertheleffe, is in practife manifolde, and in vfe very ample. This tea- ", cheth Analogically to defcribe a finall portion or circuite of ground, with the con- ", tentcs:not regarding what commenfuration it hath to the whole, or any parcell," withoutit contained. But in the territory or parcell of ground which it taketh in " hand to make defcription of it leaueth out (orvndefcribed) no notable, or odde " thing, aboue the ground vifible. Yea and fometimes, of thinges vnder ground, " geueth fome peculier marke : or warning : as of Mettall mines, Cole pittes, Stone " quarries. \&c. Thus, a Dukedome, a Shiere, a Lordihip, or leffe, may be defcribed " diftincily. But marueilous pleafant, and profitable it is, in the exhibiting to our eye, and commenfuration, the plat of a Citie, Towne, Forte, or Pallace, in true Symmetry : notapproching to any of them : and out of Gunne fhot.\&c. Hereby, the Architeč may furnifhe him felfe, with ftore of what patterns he liketh : to his the Circbuted may furnime him felfe, with ftore of what patterns heliketh : to his great initruction: euen in thole thinges which outwardly arc proportioned:cither fimply in them flues : or refpectiuely, to Hilles, Riucrs, Haucns, and Woods ad
ioyning. Some alfo, terme this particular defcription of places; Topographie.

Hydrographie, deliucreth to ourknowledge, on Globe or in Plaine, the perfect Analogicall defcription of the Ocean Sea coaftes, through the whole " world : or in the chiefe and principall partes thercof : with thelles and chiefe "

## IohnDee hisMathematicall Preface.

do it. Great pollicy may be vfed of the Capitaines, (at tymes fere, and in places conuenient)as to vfe Figures, which make greatelt (hew, of fo many as he hath: and ving the aduauntage of the threekindes of vfuall fpaces: (betwenefootemen or horfemen) to take the largeft:or when he would feme to haue few, (beyng many: conmarywife, in Figure, and (pace. The Herald, Purfeuant, Sergeant Royall, Iudgement of his expert cye, his fkill of Ordering Tafficall, the helpe of his Geomerricall inftument:Ring, or Staffe Aftrononicall: (commodioufly framed for metricall inftrument:Ring, or Staffe Aftrononucall : (commodioufly framed fo carmage and vie) He may wonderfully helpe him iclife, by perf pectue Glaffes. In which, ( truft) our poiterity will proue more fkilfull and expert, and
purpofes, then in thefe dayes, can (almoft) be credited to be poffible.
purpoles, then in thele dayes, can(almolt)be credited to be poffible.
Thus bauc I lightly pafled ouer the Artificiall Feates, chiefly dependyng vpo vulgar Geometrie : \& commonly and generally reckened vnder the name of Geometrir. But there are other(very many) Methodicall Artes, which, declyning from the purity, fimplicitic, and Immateriality, of our Principall Science of Magnitades do yet neuertheles ve the great ayde, direction, and Method of the fayd principail science, and hate propre names, and dirinct: both from the Science
of Grometree, (from which they are deriued) and one from the other. As Perfpectine, Aftronomic, Mufike, Cofmographie, Aftrologic,Statike, Anthropographie, Trochilike, Helicofophie, Pneumatithmic, Menadrie, Hypogeiodie, Hydragogie, Horomerrie, Zographic, Architecture, Nauigation, Thaumarurgike and Archemaftrie. I thinke it neceflary, orderly, of thefe to giue fome peculier defcriptions : and withall, to touch fome of their commodious vies, and fo to make this Prefice, to be a little fwete,pleafant Nofegaye for you:to comfort your Spinites, beyng almoft out of courage, and in defpayre, (through brutifh brute) Weenyng that Geometrie, had but ferued for buildyng of an houfe, or a curious bridge, or the roufe of Weftminfter hall, or fome witty pretty deuife, or engyn, appropriate toa Carpenter, or a Ioyner \&c. That the thing is farre otherwife, then the world, (commonly) to this
day, hath demed, by worde and worke, day, hath demed, by worde and worke, good profe wilbe made.

Among thefe Artes, by good reafon, Perfpectiue ought to be had, ere of Affronomicall Apparences, perfect knowledgecan be atteyned. And bycaufe of the prerogatine of Light, beyng the firftof Gods Creaturest and the eye, the light,
of our body, and his Senfe moft mighty, and his organ moft Artificiall and Geometricall: At Perfpective,,we will begyn therfore. Perfpectine, is an Art Mathematicall, which demonftrateth the maner, and properties, of all Radiations Direct, Broken, and Reflected.This Defcription, or Notation, is briefibut it reachech fo farre, as the world is wyde. Itconcerneth all Creatures, all Actions, and paffions, by Emanation of beames perfourmed. Beames, or naturall lines, (here) I meane, not oflight onely, or of colour (though they, to eye, giue flew, witnes, and profe, wherby to ground the Arte vpon, but allo of other Fornes, both Subftantiall, and Accidentall, the certaine and derermined actiue Ra-
diall emanations. By this Art (omitting to feake of the higheft pointes) we may diall emanations. By this Art(omitting to feeake of the higheft pointes) we may vec our eyes,and the light, with greater pleafure:and perfecter Iudgement:both of things, in lightfeen, \& of other: which by like order of Lightes Radiations, worke and produce their effectes. Wemay be afhamed to be ignorant of the caufe, why fofundry wayes our eye is deceiued, and abufed: as, while the eye weeneth a roüd Globe or Sphere(beyng farre of) to bea flat and plaine Circle, and folikewife iud.
geth

## Iohn Dee his Mathematicall Præface.

geth a plaine Square, to be roûd:fuppofeth walles parallels, to approche, a farre of: rofe and floure parallels, the one to bend downward, the other torife vpward, at a little diftance from you. Againe, of thinges being in like fwiftnes of mouing, to thinke the nerer, to moue fatter: and the farder, much flower. Nay, of two thinges, wherof the one (incomparably)doth moue fwifter then the other, to deme the flower to moue very fivift, \& the other to ftand: what an error is this, of our eye! Of the Raynbow, both of his Colours, of the order of the colours, of the bignes of it, the place and heith of it, (\&8c)to know the caufes demonftratiue, is it not pleafant, is it not neceflary! of two or three Sonnes appearing: of Blafing Sterres : and fuch like thinges : by naturall caufes, brought to paffe, (and yet neuertheles, of farder \& \& occafion Naturall : Yca,rather, is it not,greatly, againft the Souerainty of Mans nature, to be fo ouerhot and abufed, with thinges (at hand) before his eyes: as with a Pecockes tayle, and a Doues necke : or a whole ore, in water, holden, to feme broken. Thynges, farre of, to feeme nere: and nere, to feme farre of . Small thinges, to feme great : and great, to feme finall . One man, to feme an Anny. Or a man to be curftly affrayed of his owne fhaddow. Yca,fo much, to fcare, that, if you, being(alone) nere a certaine glaffe, and proffer, with dagger or fword, to foyne at the glaffe, you fhall fuddenly be moued to giue backe(in maner) by reafon of an Image, appearing in the ayre, betwenc you \&e the glaffe, with like hand, fword or dagger, \& with like quicknes, foyning at your very eye, likewife as you do at the Glaffe. Straunge, this is, to heare of: but more meruailous to behold, then thefe my wordes can fignific. And neuertheleffe by demonftration Opticall, the order and caufe therof, is certified: eucn fo, as the effect is confequent. Yea,thus much more, dare I take vpon me,toward the fatiffying of the noble courrage, that longeth ardently for the wifedome of Caufes Naturall:as to let him vnderitand, that, in London, he may with his owne eyes, haue profe of that, which I haue fayd herein. A Genteman, (which, for his good feruice, done to his Countrey, is famous and honorable : and for fkill in the Mathematicall Sciences, and Languages, is the Od man of this land. \&cc.) euen he, is hable: and (I am fure) will, very willingly, let the Glaffe, and profe be fene: and fo I (here) requeft him : for the encreafe of wifedome, in the honorable : and for the topping of the mouthes malicious : and repreffing the arrogancy of the ignorant. Yemay calily gefte, what $I$ mcanc. This Art of Per $\beta$ pectiue, is of that excellency, cafily belcue:without Actuall profe perceiued. I peakenothing of Naturall phi. cafly belcuc: without Actuail profe perceiued. If peake nothing of Naturall Phieined vnto. Nor, of Afrowomie: which, without Perßerfiue can not werfectly atded : Nor © Afrologie, naturally Verified, and auouched. That part hereof which ealeth with Glaffes (which name, Glaffe is a generall name in this Are, for any thing, from which a Beame reboundeth) is called Catoptrike and hath fo many vfes, both merueilous, and proffitable: that both it woup therin che principall conclufions, all ready knowne: And alfo(perchaunce) fome thinges, might lacke due credite with you : And I, therby, to leefe my labor:and 63 you,to flip into light Iudgement*, Before you haue learned fufficiently the powre of Nature and Arte.
Now, to procede: Aftronomie, is an Arte Mathematicall, which demonftrateth the diftance, magnitudes, and all naturall motions, apparences, and palsions propre to the Planets and fixed Sterres : for

## Iohn Dec his Mathematicall ${ }^{\prime}$ rreface.

Invifible Shail we ( $\ddagger$ fay) looke vpornthe Ftewnd ; sterres, and Planets, as an Oxe and an Affe doch: no fiurder carefall or inquifitue, whet they are: why were they Created, How do they execute that they were Created for:Seing, All Creatures, were for our fake created and both we, and they, Created, chiefly toglorifie the Almighty Creator: and that, by all meanes, te vs poffible. Nelitc ignorare(faith Plate in Epinomus) Affrowonian, Sappentijsimu quidam t/fe. Beye not tgnorant, Aftron nomie to be a thyng of excellent wyfedome. Afronomie, was to vs, from the bc-
ginning connmended, and in maner commaunded by God him felfe. In afmuch as he made the Somed, M Mone, and Sterres,to beto vs, for Signes, and knowledge of Seafons, and for Diftinctions of Dayes, and yeares. Many wordes nede not. But I wiff, cuery man fhould way this wósd, signes. And befides that, conferre it alfo with the tenth Chapter of Hecremie. And though Some thinke, that there, they hane fouthd a rod: Yet Modeft Reafon, will be indifferent Iudge, who ought to be beaten therwith, in refpect of our purpofe. Leauing that: I pray you vnderftand this :that without great điligence of Obferuation, examination and Calculation, their periods and courfes(wherby Diffinction of Seafons, yeares, and New Mones mighe precifely be knowne) could not exactely be certificd. Which thing to performe, is that int', which we bere haue Defined to be Aflronomic. Wherby, we may haue the diftinct Courfe of Times, dayes, yeares, and Ages: afwell for Confideratié of Sacred Prophefies, accomplifhed in due time, foretold : as for high Myfticall Solcmnities holding: And for all other humaine affuires, Conditions, and cousnantes, vpon certaine time, befwene man and man' : with many other great ves: Wherin, (verely), would be great incertainty, Confufion, vntruth, and brutifh Barbaroufnes:without the wonderfull diligence and fkill of this Arte : continuafly learning and determining Times, and periodes of Time, by the Record of nually learning, and detcrnining Eimes, and periodes of Time, by the Record of
the heunenly booke, wherin all times are written : and to be read with an Afromothe heurenly booke, wherin

Mufike, of Motion, hath his Originall cauk : Therfore, after the motions noof f wiftyand moft Slow, whith are in the Firmament, of Nature perforned:and voder ithe Abironomers Gomfideration now I will Speake of an other kindc of Motion, producing found, audele a and of Man numerable. Chuffike I call here that Science, which of the Grekes is called Harmoxice. Nor medling with the Controuerfie betwinc the auncient Harkemfles, and Casoniffes. Mufike is a Mathematicall Science, which teacheth, by fenfe and reafon, perfectly to iudge, and order the diuerfities of foundes, hye and low. Aitronomic and CMufike ate Siftets, faith Plato. As, for Affronomic, the cyes:So, for Harmonious Motion, the eares were made. But as difronomic hath a more diuine Contemplation, and córtiodity, thentriortall eye cain percciue : So, is CMujike to be confidered, that the *Miride ritay be prefecred, before the eare. And from audible found, we ought to afeende, to the examination : which numbers are Harmoniows, and which not. And why, either, the one are: or the other are not. I could at large, in the heauenly * motions and diftances, deffribe a meruailous Harmonic, of Pythagoras Harpe with eight fringes. Alfo, fomwhat might be fayd of Mercuriu** two Harpes, with eight Itringes. Alfo, romwhat might be fayd of Mercurium two Happes, of the Harmontic, to our ${ }^{*}$ Spirituall part appropriate. As in Ptolomaws third boke, in of the Harmonte, to our (he fourth and fixth Chapters may appeare.* And what is the caufe of the apt the fourth and ixth Chapters may appeare. And what is the caure of the ape groffe \& corruptible body:but a certaine Meane, and Harmonious Spiritwalitic, with

## Iohn Dee his Mathematicall Preface.

any time paft, prefent and to come: in ref pect of a certaine Horizon, or without refpect of any Horizon-By this Arte we are certified of the difance of the Starry Skye, and of eche Plancef from the Centre of the Earth and of the greatnes of any Fixed ftarre fene, or Planite, in relpect of the Earthes greatnes. As, we are fure (by this Arte) that the Solidity, Maffines and Body of the Somme, conteineth the quantitie of the whole Earth and Sea,a hundred thre fcore and two times, leffe by $\div$ one eight parte of the earth. But the Body of the whole earthly globe and Sea,is bigger then the body of the Mone, three and forty time leffeby:- of the Mone. Wherfore the Sonne is bigger then the CMane, 7000 times, lefte, by $59 \frac{\%}{6}$ that is, precifely $694^{\circ} \frac{\pi}{4}$ bigger then the carone. And yet the vnlkillfull man, would iudge them a like bigge. Wherfore, of Necefsity, the one is much farder from vs, then the other. The Somin, when he is fardett from the earth (which, now, in our age, is, when he is in the 8.degree, of Cancer) is, 1479 earth, is 68 Semidiameters of the earth and - - Thenereft, that the CMone commeth to the earth, is Scmidianeters $52 \div$ The diftance of the Starry Skye is, fro vs, in Semidiameters of the earth $20081 \div$ Twanty thoufand fourefcore, one and almoft a halfe. Subtradt from this, the canoes nereft diffance,from the Earth: and therof remaineth Semidiameters of the earth $20029 \div$ Twenty thoufand nine and twenty and a quarter. So thicke is the heanenly Palace, that the P/a. ment and Charge exercie in, and mor omipotent Maieftie of the king of kings. This is that, which in Cencfis is called Ha Rakia. Confiderit well. The Semidiameter of the earth, cobteineth of our common miles $3436 \div$ three thoufand, foure hundred thirty fix and foure eleuenth partes of one myle:Such as the whole earth and Sea, round abour, is 21600 . One and twenty thoufand fix hundred of ou myles.Allowyng for cuery degree of the greateft circle, thre fcoremyles. Now if you sway well with your felfe but this litle parcell of frute 1 fronomicall, as concerning the bignene, Diftances of Sonne, Mone, Sterry Sky, and the huge maffines of Ha Rakis, will you not finde your Coniciences moued, with the kingly Propher,
to fing the confeffion of Gods Glory, and fay, The Heauens declare ebe gloe vy of God, and tbe Firmament [Ha Ratia] peivetb fortb the workes of bis bandes. And fo forth, for thofe fuue firt ftames, of that kingly Pfalme. Well, well, It is time for fome to lay hold or: wifcdome, and to Iudge eruly of thinges: and notfo to expound the Holy word, all by Allegories tas to Neglect the wifedome, powreand Goodnes of God, in, and by his Creatures, and Creation to be feen andleamed. By parables and Analogies of whofe natures and properties, the courfe of the Ho ly Scripture,alfo, declareth to vs very many Myfteries. The whole Frame of Gods Creatures; (which is the whole world;) is to vs, a bright glaffe: from which, by refiexion, reboundeth to our knowledge and perceiuerance, Beames, and Radiations/repreferting the Imäge of his Infinite goodnes, Omnipotécy, and wifedome. And we therby, are taughtiand perfuaded to Glorific eur Creator, as God: and be thankefull therfore. Could the Heatheniftes finde thefe ves, of thefemoft purc, beawtifull and Mighty Corporall Creatures:and hall we, after that the true Sowne of rightwifeneffe is rifen aboue the Horizon, ofour temporall Hemi/fberie, and hath fo abundantly ftreamed intaour hartes, the direat beames of his goodnes, mercy and grace: Whofeticat All Creatures fecle : Spirituall and Corporall: Vifible an

## IobnDec his Mathematicall Praface.

 would Jighty belcqe But of the Iundry Mixture (as I may teme it), and concurfe, diuerfecollarion, zad Application of thefe Hammoniei: as of thre, foure, fue, or me: Maruailous hatue the cfoetes ben: and yet may be founde and prodnced not mo: Reed in An with fome pare State of proportionall conideration for our time, and being : ip refpect of the 8 , bovkeof State, of the thinges then ; in which, and by which, the wondrouseffectes were wrought. Domecritu and T beephrailus affirmed, that, by corufike, grisfes and difeales of the Minde, and body might be cured, or infersh. And we finde in kecorde, thast Teppasder, Arion, if menial, arphews, Amphion, Dauid, Pathagar, ws, Empedo Wherifens cles, Afctepiades and 7 imulbrus, by Harmonicall Confonăcy, haue done, and brought to pas, thinges, morethen meruailous, to here of. Of them then, making no sht fome osinfines der difcourfe, in this place. Sure I am, that Common wafke commonly fry fhatre faf found to the e this place : Surctam, that Common Mujike, commonly ved, is thonk of Ma found to the crivficiens and Hearers, to be fo Commodions and pleafane, That if commeng I would fay and difpute, but thus mach; That it were to be othervife vied, then it thenghrs. is, I fooukd finde more repreeuers, then I could finde priuy, or fkilfull of my meaning. In thinges therfore euident, and better knowen, then I can expreffe: and fo
allowed and liked of, (as I would wifh, fome other thinges, had the like hap) I will allowed and liked of, (as I would wilh,fome other thinges, had the like hap) I will fpare to enlarge my lines any farder, butconfequently follow my purpofe.
OfColmographie, I appointed briefly in this place, to geue you fome intelligence. Cofmographic, is the whole and perfect defcription of the heauenly, and allo elementall parte of the world, and their homologall application, and mutuall collation neceffaric. This Art, requirech Affronomie, Ceographite, Hydrographic and chiufike. Théfore, it is no finall Arte, norfo fimple, as in common pratife, it is (flightly) confidered. This matcheth Heanen, and the Earth, in one frame, and aptly applicth parts Correfpódept:So, as, the Heauenly Globe, may (ini practife) be duely defcibibed vpon the Gcographicall, and Hydrographicall Globe. And there, for vs to conlider an
 Iatitudes, Declinations, and Verticalitie :alfo Climes, and Paallels and by an Hor rison annexed, and renolurion of the carthly Globe (as the Heauen, is, by the Primonum, catied about in 24, rquall Houres) to learnc the Riffinges and Sertinges of Sterres (of Viggil in his Georgikes: of Hefied:of Happocrates in his Medicinel Sphaff, to Perdicca King of the Macedonians: of Diocles, to King Antigozius, and of Other famous Philof ophers prefcribed) a thing neceflary, for dae manuning of the eatth, for Nauigation, tor the Altcration of mans body:being, whole, Sicke, wounded, or how
fed. By the Reuolution, alfo, or mouing of the Globe Cofmogrpe fed. By the and Setting of the Sonne: the Lengthes of dayes and niphogre the Hourcs and times (both night and day) are knowne : with verymany other pleafant and andecefiary vics . Wherof, fome areknowne butberter remaine for pheh to knoty and vfer who of a farke of truefire, can make a wonderfull bonfire, by applying of ducly,
Of Altrologie, here I make an Arte, feuetall from Alfromomic : not bynew deuife, but by good reafon and authoritie : for, Aftrologie, is an Arte Mathematicall, which reafonably demonitrateth the opcrations and effectes, of the naturall beames, of light, and fecrete influence: of the Sterres and Planets: in enery element and elementall body:

Iohn Dee his Mathematicall Praface.
$2 t$ all times, in any Horizon affigned. This Arte is furnifhed with many other grear Artes and experiences: As with perfecte Perpertius, Affronomie, cof mographic, Neturall Philffophie of the 4. Elementes, the Arte of Graduation, and fome good vnderftading in cMry/ike : and yet moreover, with an other grear Arte, heteatrer following, though I, here, fet this before, for fome confiderations me
mouing. Sufficicat (you fee) is the fluffe, to make this rare and fecrete Arte of: moung. Sufkicat (you tee, is the nuffe, 10 make this rareand feccre Artc, of and hard enough to frame to the Conclutson Sylloggsticall. Yet both the maniatteyning of this Arte : and by examples of effettes, to confirme the fame: hath Ifft vnto vs fufficient proufe and witnoffe and we alfo daily may perceane That mans body , and all other Elementall bodies are altered, difpofed, ordred, pleafio red, and difileafured, by the Influenciall working of the Sumne, Mone and the other
 bookes, in the fecond Chapter: Eff axtem neceffario Msindus ine, /upernis lationtbas

 necce Bitie, almoft, next adioyning, to the bearenly motions: That, from tbence, all his vertuc or force may be gouerned. For, that is to be thought the firft Canfe ontoall: from which, the beginning of motion, is. And againe, in the tenth Chapter. opertet igitur of heranm promaipis fumamas, of caufac. omniamn finmittor.
 manifffle Solis latio, evc. And fo forth. His Meterologicall bookes, are fill of argitmentes, and effectuall demonftrations, of the vertace, operation, and power of the heauenly bodies, in and ypon the fower Elementes, and other bodies, of them (either perfestly, or vnperfettly ) compofed. And in his fecond booke, De Genera-
 In Englifhe, thus. Wherefore the 2ppermolt motion, is not the can e of Genc ration and Corruption, but the motion of the Zodiake: for, that, both, is cone tinuall, and is caufed of troo mounges. And in his fecond booke, and fecond Chapter of hys Pbyfikes. Hemio nampof gencrat homisem, atif. Sol. For Man(fayth he) and the Sonne, are caufe of mans generation. Authorities may be brought, very many : both of 1000,2000 .yea and 3000 . yeares Antiquitic : of great Philofophers, Expert, Wijf, and godly men, for that Conclufion: which, daily and boureIy, we men, may difecme and perceaue by fenfeand reafon : All beaftes do feele, and fimply few, by their actions and paffions, outward and inward: All Plants, Herbes, Trees, Flowers, and Fruites. And finally, the Elementes, and all thinges of the Elementes compofed, do geue Teftimonie (as Arifotile fayd) that theyr Whole Difpofitions, Dertises, and naturall motions, depend of the Alfiuitie of the beanenly morions and Infisences. Whereby, befide the fpecificall order and forme, due to every /eede: and befide the Nature, propre to the Indiuiduall Mae trix, of the tbing produced; what Shall be the beaseinly Impreßion, the perf elt and circhm/pelte Aftrologien hat b to Conclude. Not onely (by Iporedfymes) to dri, buthy Naturall and Mathematicall demonftration ridotron. Whercunto, what Sciences are requifife (without exception) I partly hauc here warned: And in my Propelcumes ( befides other matter there diflofed ) I hane Mathematicaly furnShed vp the whole Method: To this our age, not fo carcfully handled by any, euer

## Iohn Dee his Mathematicall Preface.

be had:we call this Art, Statike: that is, the Experimentes of the Balance. Oh, that men wit, what proffit, (all maner of wayes) by this Arte might grow, to the hable exaon miner, and diligent practifer. Thou onely, knoweft all thinges precifely (O God) " who halt made weight and Balance, thy ludgement: who hatt created all thinges " in Number, traight, and Meafure:and haft wayed the mountaines and hils in a Ba" Ince:who haft peyfed in thy hand, both Heauen and carth. We therfore war"I ned Dy the Sacred word,to Confider thy Creatures:and by that confideration, to ". wynne a glyms (as itwere, or fhaddow of perceiuerance, that thy wifedome, ". being farder aduertifed, by thy mercifull goodnes, that, three principall wayes ", were, of the, vfed in Creation ofall thy Creatures, namely, Number, Waight and
 " mous, and to hamaine vfes moft neceflary, are, all ready, fufficiently knowen and ", extant: This thirdkey, we befeche thee (through tiy accuftomed goodnes,) ") thar it may come to thenedefull and fufficient knowledge, offuch thy Seruauntes, " 25 in thy vorkemanllip, would gladly finde, thy true occafions (purpofely of the " vfed ) whereby we fhould glorific thy name, and flew forth (to the weaklinges in nn faith thy wondrous wifedome and Goodnes. Amen.

Meriatile nothing ar this pang(godly frend, you Gentic and zelous Student.) An other day, perchaunce, you will perceiue, what occafion moued me. Here, as now, I will giue you fome ground, and withall fome fhew, of certaine commodities, by this Arte arifing. And by caufethis Arte is rare, my wordes and practifes might be to darke: vnleaft you had fome light, holden before the matter:and that, beft will be, in giuing you, our of Arehimedes demonftrations, a few principal Conclutions, as folowerh.
L.

The Superficies of euery Liquor, byit felfe confiftyng, and in quyet, is Spharicall : the centrewhereof, is the fame, which is the centre of the Earth.

If Solide Magnitudes, being of the fame bignes; or quätitie, that any Liquor is, and hauyng alfo the fame Waight: be let downeinto the lame Liquor, they will fettle downeward, fo, that no parte of them, fhall be aboue the Superficies of the Liquor: and yet neuertheles, they will not finke vterly downe, or drowne.
3.

Ifany Solide Magnitude beyng Lighter then a Liquor, be let downe into the fame Liquor, it will fettle downe, fo farre into the fame Liquor, that fo great a quantitie of that Liquor, as is the parte of the Solid Magnitude, fettled downe into the fame Liquor : is in W'aght, xquall, to the waight of the whole Solid Magnitude.

Any Solide Magnitude, Lighter then a Liquor, forced downe
into

## Iohn Dee his Mathematicall Preface.

cuer I faw, or heard of. I was, (for * 21 .yeares ago) by certaine carncft difputations, of the Learned Cierardrs Mercator, and Antonius Gozans, (and other, ) therto fo and 1549.15 prouoked:and (by my conftant and inuincible zeale to the veritic) in obferuations Leusyn. of Heateniy Influencies(to the Minute of time,)than,fo diligent: And chiefly by theSupernaterall infleence, from the Starre of lacob,fo dirccted:That any Modef and Sober Student, carcfully and diligently feking for the Truth, will both finde \& ciffelfe, therin, to be the Veritie, of thefe my wordes: And alfo become a ReafonableReformer, of three Sortes of people: about thefe Influentiall Operations, greatly eraing from the truth. Wherof, the one, is Light Beleuers, the other, Light Defpifers, and the third Light Practifers. The firt, \& moft cómon Sort, thinke the Heauen and Sterres, to be anfwerable to any their doutes or defires:which is not fo: and, in dede, they, to much,oucr reache. The Sccond forte thinke no Influentiall vertue (fró the heauenly bodics ) to beare any Sway in Gencration and Corruption, in this Elementall World. And to the Sarme, Mone and Sterres(being fo many, fo pure, fo bright, fo wonderfull bigge, fo farre in diftance, fo manifold in their motions, fo conftant in their pcriodes. \$sc. ) they affigne a fleight, finple office or two, and fo allow vnto thé(according to their capacities) as much vertuc, and power Influentiall, as to the Signe of the Sumne, Mone, and feuen Sterrcs, hanged vp(for Signes) in London,for diftinction of houfes, \& fuch groffe he'pes, in our wordly affaires: And they vnderftand not(or will not vnderfand) of the other workinges, and vertues of the Heaucnly Sunne, Mone, and Sterres : not fo much, as the Mariner, or Hufband man : no, not fo much, as the Elephant doth, as the Cynocephalus, as the Porpentine doth : nor will allow thefe perfeat, and incorruptible mighty bodics, fo much vertuall Radiation, \& Force, as thcy fee in a litlc pecce of a Magnes itonewhich, at great diftance, fheweth his operation. And perchaunce they thinke, the Sea \& Riuers (as the Thames ) to be fome quicke thing, ard fo to ebbe, and flow, run in and out, of them felues, at their owne fantafics. Godhelpe,God helpe. Surely, thefe men, come to fhort : and cither are to dull: o: willfully blind:or,perhaps, to malicious. The third man, is the common and valgarc 1 ifrelugien, or Practifer: who, being not duely, artificially, and perfectly furaithed:yet, either for vaine glory, or gayne :or like a fimple dolt, \& blinde Bayard, both in matter and maner, erreth:to the difcredit of the Wary, and modeft $A$ firologien:and to the robbing of thof moft noble corporall Creatures, of their Na turall Vertuc:bcing moft mighty : moft beneficiall to all elementall Generation, Cormptionand the appartenances : and moft Harmonious in their Monarchie: For which thinges, being knowen,and modeftly vfed:we might highly, and continuzlly glorifie God, with the princely Prophet, faying. I he Heakens declare the Giorie of God:who made the Heanés in bis wifedome: wolo made the Sonne, for to baue dominion of the day: the Mone and Sterres to bauc dominion of the nyght: whereby, Day to day Dttereth talke: and night, to night declareth know* ledoc. Prayje bim, allye Sterres, and Light. Amen.
IN order, now foloweth, of Statike,fomewhat to fay, what we meane by that name:and what commodity,doth,on fuch Art, depend. Statike, is an Arte Mathematicall, which demonftrateth the caufes of heauynes, and lightnes of all thynges : and of motions and properties, to heauynes and lightnes, belonging. And for afmuch as, by the Bilanx, or Balance(as the chicffenfible Inftument, ) Experience of thefe demonfrations may

## Iohn Dee his Mathematicall Preface:

into the fame Liquor, will moue vpward, with fo grear a power, by how much, the Liquor hauyng xquall quantitie to the whole Magnitude, is heauyer then the fame Magnitude.

Any Solid Magnitude, heauyer then a Liquor, beyng lee downe into the fame Liquor, will finke downe veterly: And wilbe in that Liquor, Lighter by fo much, as is the waight or heauynes of the Liquor, hauing bygnes or quantitie, xquall to the Solid Magnitude. 6.

If any Solide Magnitude, Lighter then a Liquor, belet downe into the fame Liquor, the waight of the fame Magnitude, will be, to the Waight of the Liquor. (Which is xquall in quantitic to the whole Magnitude, )in that proportion, that the parte, of the Magnitude fettled downe, is to the whole Magnitude.
BY thefe verities, great Errors may be reformed, in Opinion of the Naturall Motion of thinges, Light and Heauy. Which errors, are in Naturall Philofophie (almo(t) of all me allowed tro much trufting vo Authority zand fale Suppofitions. As, Of any two bodyes, the heauyer, to moue downward fafter then rhe lighter. This error, is not firlt by me, Noted: but by one lohn Baptivf de Be sedifits. Thechief of his propofitions, is this:which feemeth a Paradox.

If there be two bodyes of one forme, and of one kynde, xquall in ouantitic or vnxquall, they will moue by xquall fpace, in $x q u a l l$ tyme:So thar borf cheyr mouynges be in ayre, or both in water : or in anyone Middle.
Hereupon, in the feate of Gunnyng, certaine good difcourfes (otherwife) may receine great amendement, and furderance: + Fa the entended purpore, alfo, The thontor. allowing fomwhatto the imperfection of Nature: notaunfwerable to the preci- full oje of fenes of demonftration. Moreouer, by the forefaid propofitions (wifely vfed.) thofe Propgf. The dye, the water, the Earth, the Fire, may benerely, knowen, how lighror hea- tiownuy they are (Naturally) in their afligned partes', orin the whole. And then, to thinges Elementall, ruming your practife: you inay deale for the proportion of the Elementes; in the thinges Compounded. Then, to the proportions of the Hu mours in Man: their waightes: and the waight of his bones, and fefh. \&c. Than, by waight, to haue confideration of the Force of man, any maner of way: in whole orin part-Thens,may yod, of Sbips water drawing, drucrfly, in the Sea and in frefl waterithiue pleafant confideration' and of waying vp of any thing, fonken in Sea or infreilh water \&ic. And (rolift vp your head a loft:) by waight, you may, as precifly, as by any inftrumentels, meafure the Diameters of Sonne and exone. ofc. Frende, I ptay yous way thefe thinges, with the iut Balance of Reafon. And you will finde Meruailes vponi Meruailes: And effemle ohe Drop of Truth ( yea in Naturall Phillolophie) more worth, then whole Libranies of Opinions, vndemon-
Arated:or not Itratedfor not aunfivering to Natures Law, and your experience. Leaning thef
c.j.

Anno. 1548
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## Iohn Dee his Mathematicall Praface.

thinges, thus: I will giuc you two or three, light practifes, to great purpofe : and fo finifh my Annotation Staticall. In Mathematicall matters, by the Mechanicien ayde, we will behold, here, the Commodity of waight. Make a Cube, of any

Thepratilis
Statical, to
Staticall, to
Portion, be-
fuce the
Cubb, and
Sphert. or Globe,precifely, of a Diameter xquall to the Radicall fide of the Cube. Your
ftuffe,may be wood, Copper, Tinne, Lead, Siluer.\&c. (being,as I fayd,oflike naftuffe,may be wood, Copper, Tinne, Lead, Siluer.\&cc. (being, as I fayd, of like na-
ture, condition,and like waight throughout.) And you may, by Say Balance, ture, condition, and like waight throughout.) And you may, by Say Balance, can be diferned or tryed: and fo, haue proceded to make you a perfect Pyle, comcan be dwcerned or tryed:and fo, haue procededio $\&$ Number your molt diligently tryed, all. And of cuery one, the Content knowen, in your leaft mott diligently tryed,all. And of cuery one , the Content knowen, in your leart
waight, that is wayable. They that can not haue thefe waightes of precifenes: waight, that is wayable. (They that can not haue there waightes of precirnes: what nere precifenes: by halfing euer the Sand : they flall at length, come to a reaft common waight Thercin, lleaue the farder matrer, to their ditcretion, whom nede fiall pinche The Venctions confideration of waight, may feme precife enough: by cightdefcentes progrefionall, औ halfing, from a grayne. Your Cube, enough:by eight defcentes progressionall, haifing, from a grayne. Your Cube, way your Cube.Note the Number of the waight. Wav, after that, your Sphare. way your Cube.Note the Number of the waight. Way, after that, your Sphare. Notelikewif, the Nuber of the waight.1f you now find the waight of your Cube,
to be to the waight of the Sphxre, as 21. is to II: Then you fee, how the Mechanito be to the waight of the Sphare, as 21 . is to II: Then you fee, how the Mechanieffect )tought the proportion of the Cube to the Sphere : as I haue demonftrated effect)tought the proportion of the Cube to the Sphere : as thaue demonitratcd it, in the end of the twelfth boke of Ewclide. Often, try with the fame Cube and Sphxre. Then, chaunge,your Sphrre and Cube, to an other matter: or to an othe bignes : till you haue made a perfect vniuerfall Experience of it. Pofsible it is, hat you fhall wynne to nerer termes, in the proportion.
When you haue found this one certaine Drop of Naturall veritie,procede on, to Inferre, and duely to make affay, of matter depending. As, by caufe it is well demonitrated, that a Cylinder, whofe heith, and Diametcr or of the Sphxre , is Sefquilter to the fame Sphxre (that is, as 3. to 2:) the Diameter of the Sphxre, is Sefquialter to the fame Sphxre (that is, as 3 . to $2:$ )
To the number of the waight of the Sphare, adde halfe fo much, as it is : and fo hauc you the number of the waight of that Cylinder. Which is alfo Comprehended of our former Cube:So, that the bafe of that Cylinder, is a Circle defcrihended of our former Cube:So,that the bafe of that Cylinder, is a Circle deicri-
bed in the Square, which is the bafe of our Cube. But the Cube and the Cy linder, being both of one heith, haue their Bafes in the fame proportion, in the which, they are, one to an other, in their Mafsines or Soliditic. But, before, we haue two numbers, exprefsing their Mafsines, Solidities, and Quantities, by waight:wherfore, we haue ${ }^{*}$ the proportion of the Square, to the Circle, inferibed in the faine Squarc. And fo are we fallen into the knowledge fenfible, and Expein thenentall of Suarchimedes great Secret: of him, by great trauaile of minde, fought rimentall of Archimedes great Secret: of him, by great trauale of minde, fought
and found. Wherfore, to any Circle giuen, you can giue a Square xquall: * as and found. Wherfore, to any Circle giuen, you can giue a Square xquall: *as
I hauc taught, in my Annotation, vpon the firft propolition of the twelft boke, And likewife,to any Square giuen, you may giue a Circle xquall: "If you defcribe a Circle, which thall be in that proportion, to your Circle infcribed, as the Square is to the fame Circle-This, you may do, by my Annotations, vpon the fecond propofition of the welfth boke of Euclide, in my third Probleme there. Your dilipofition of the twelth a
gence may come to a proportion, of the Square to the Circle inferibed, nerer the truth, then is the proportion of 14.to II. And confider, that you may begyn at the Circle and Square, and fo come to conclude of the Sphxre, \& the Cube, wha

## Iohn Dee his Mathematicall Praface.

wayes you may conclude your purpofe : it is to wete, either by numbers or lines. By numbers: as, if you diuide the fide of your Fundamentall Cube into fo many xquall partes, as it is capable of, conueniently, with your eafe, and pre-
cifenes of the diuifion . For, as the number of your firt and leffeline (in your cifenes of the diuifion. For, as the number of your firt and leffe line (in your hollow Pyramis or Cone,) is to the fecond or greater (both being counted from the vertex) fo thall the number of the fide of your Fundamentall Cube, be to the núber belonging to the Radicall fide, of the Cube, dubble to your Fun-
damentall Cube:Which being multiplied Cubik wif, will fone fhew it felfe, whether it be dubble or no, to the Cubik number of your Fundamentall Cube. By ther it be dubble or no, to the Cubik number of your Fundamentall Cube. By
lines, thus:As your leffeand firft line, (in your hollow Pyramis or Cone,) is to the fecond or greater,folet the Radical fide of your Fundmétall Cube, be to a fourth proportionallline, by the 12 . propofition, of the fixth boke of Eaclide . Which proportionalline, by the 12 - propofition, of the fixth boke of Euclude. Which Fundamentall Cube : which is the thing we defired. For this,may I (with ioy) fay, Еүрнка, еурнкл, еуряка: thanking the holy and glorious Trinity: hauing greater caufe therto, then ${ }^{*}$ Archimedes had (for finding the fraude ved in the Kinges Crowne, of Gold):as all men may cafily Iudge : by the diuerfitic of the frute following of the one, and the other. Where I pake betore, of hollow $\mathrm{Cu}-$ Lik Coffen:the like vfe, is of it:and without waight.Thus. Fill it with water, precifely full, and poure that water into your Pyramis or Cone. And here note the lines catting in your Pyramis or Cone. Againe, fill your coffen, like as you did before. Put that Water, alfo, to the firf. Marke the fecond cutring of your lines. Now, as you proceded before, fo muft you here procede. *And if the Cube, which you fhouid Double, be neucr fogreat: you haue, thus, the proportion (in finall) betweic your two litle Cubes:And then, the fide, of that great Cube(to be doabled) being the third, will hauc the fourth, found, to it proportionall: by the 12.of the fixthof Euclide.
Note, that all this while, I forget not my firf Propofition Staticall, here rehearfid:that, the Supcricies of the watcr, is Spharicall. Wherein, vfe your difcretion:
to the lif:line, adding a finall heare breadth,more:and to the fecond, half fe heare to the lir:t line, adding a fmall heare breadth, more: and to the fecond, halfe a heare
breadtuore, to hislength. For, vou will cafily perceaue, that the difference can breatamore,to his ength. For, you will cafly perceaue, that the difference can
be no thus tive. For firding the frolling of the water atorne lewell. Square the Semidiamerer, fiom the Centre of the earth, to your firt Waters Superficies. Square then, " halfe the Subtendent of that warry Superficies (which Subtendent muf haue the " equart partes of his meafure, all one, with thofe of the Semidiameter of the earth ", take tie Rote Square. That Rote, Subtraacte from your firt Semidiameter of the " earth: :o your watry Superficies : that, which remaincth, is the heith of the water, in the middle, abouc the leuell. Which, you will finde, to be a thing infenfible. And theugh it were greatly fenfible,* yet, by helpe of my fixt Theoreme vpon the Laft Propofition of Euclides twelfth booke, noted: you may reduce all, to a true Leuch. But, farther diligence, of you is to be vfed, againf accidentall caufes of the waters fwelling: as by hauing(fomwhat) with a moytt Sponge, before, made moyft your hollow Pyramis or Cone, will preuent an accidentall caufe of Swelling, \&ec. Experience will teach you abundantly : with great eafe, pleafure, and cómoditic. Thus,may you Double the Cube Mcchanically, Treble it, and fo forth, in any Note thii A. proportion. Now will I Abridge your paine, coft, and Care hercin. Without all
trid-rwent of Dabituz the For, that, was rather akinde of Experimentall demóftration, then the fhorteft way;

## IohnDee his Mathematicall Preface.

their proponion is:as now, you came from the Sphare, to the Circle. For, ofSiluer, or Gold, or Latton Lamyns or plates (thorough ohe hole drawé,as the maner is) if you malkea Square figure:\& way it:and then, defcribing theron, the Circle in Icribed: \&cut of, \& file away, precifely (to the Circle) the ouerplus of the S quare: you fhall then, waying your Circle, fee, whether the waight of the Square, be to your Circle, as I4, to II. As I haue Noted, in the bcginning of Eachader tweith boke. \&ceafter this refort to my latt propofition, vpon the laft of the nveirn. And there, helpeyour felfe, to the end. And, here, Note this, by the way. That we may Square the Circle, without haning knowledge of the proportion, of tire Cir-
cumference to the Diameter: as you haue here perceited. Andotherwayes cumference to the Diameter: as you haue here perceitued. And otherwayes alfo, I can demonftrate it. So that, many hatue cumberd thern felues fupetiuouly,
by trauailing in that point firt, which was nor of necefsitie, firft : and alfo very inby trauailing in that point firit, which was not of necefsitic, firft : and alio very intricate. And earty, you may, (anditiat denerence:the Circles Ouantite, bnowen. Which thing, Ileaue Circumference:the Circles Quantitic, being firt knowen. Which thing, Ileaue to your confideration:making halt to defpatch an other Magifrall Probteme: and ter. fore this day, had it for you, that I can tell of.And that is, 1 Afechamicall Dubblyng of the Cuberioc. Which may, thus, be done: Make of Copper plates, or Tyn plates, a fourfquare vpright Pyramis, or a Cone: perfectly fafhioned in theholow, within. Wherin, let great diligence be vfed, to approche (as nere as may be) to the Mathematicall perfection of thofe figures. Ar their bafes, let them be all open:enery where, els, moft clofe, and iuft to. From the vertex, to the Circumference of the bafe of the Cone: \& to the fides of the bafe of the Pyramis: Lec.4. Atraight lines be drawen, in the infide of the Cone and Pyramis, makyng at sheir fall, on the perimeters of the bafes, equall angles on both fides themielues, with the fayd perimeters. Thefe 4 .lines (in thePyramis:andas many, in the Cone)diujde:one, in 12 . xquall partes : and an other, in 24 -an other, in 60 , and an other, in 100 . (reckenyng vp from the vertex.) Orvfeother numbers of diuifion, as experience fhall teach you. Then, ${ }^{\text {f }}$ fetyour Cone or Pyramis, with the vertex downward, perpendicularly, in refpect of the Bale. (Though ir be otherwayes, it hindreth nothyng.) So let thé moft ftedily beftayed. Now, if there be a Cube,which you wold haue Dubbled. Make you a prety Cube of Copper, Siluer, Lead, Tynne, Wood, Stone, or Bone. Or els make a hollow
Cube,or Cubik coffen, of Copper, Siluer, Tynne, or Wood \&c. Thefe, you may Cube, or Cubik coffen, of Copper, Siluer, Tynne, or Wood \&ce. The efe, you may
fo proportió in refpet of your Pyramis or Cone, that the Pyramis or Cone, will be hable to conteine the waight of them, in water, 3 . or 4 . times sat the lealt: what Stuff fo eucr they be made of, Let not your Solid angle, at the vertex, be to fharpe: but that the water may come with ease, to the very vertex, of your hollow Cone or
Pyramis.Put one of your Solid Cubes in a Balance apt:take the waight therof exPyramis.Put one of your Solid Cubes in a Balance apt: take the waight therof exactly in water. Powre that water, (without lofle) into the hollow Pyramis or
Cone, quietly. Marke in your lines, what numbers the water Cutteth: Take the Cone, quietly, Marke in your lines, what numbers the water Cutteth: Take the
waight of the fame Cube againe : in the fame kinde of water, which you had beWaight of the fame Cube againe : in the fame kinde of water, which you had be-
fore : pur that ${ }^{*}$ alfo, into the Pyramis or Cone, where you did put the firt. Marke fore : pur that* alfo, into the Pyramis or Cone, where you did put the firt. Marke
now againe, in whatnumber or place of the lines, the water Cutteth them. Two now againe, in what number or place of the lines, the water Cutteth them. Tw

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## Iohn Dee his Mathematicall Preface.

andall, vpon one Mathematicall Demooltation depending - Take water (as " much as conueniently will ferue your tume: as I wamed before of your Funda- "刀 mentall Cubes bignes) Way it precicely, Put that water, into your Pytamis or "" Cone. Of the fame kinde of water, then take againe, the fame waight your tad "
before: pue that likewife into the Pyramis or Cone. For, in eche time, your mar- $"$ king of the lines, how the Water doth cut them, (hall geveyou the proportion be- twen the Radicall fides, of any two Cubes, wherof the one is Doubleto the other: " working as before I hauetaught you:* fauing that for you Fundamentall Cube his Nots." Es Radicall fide: herey you may rake a rightline, ar pleafure.
Yet farther proceding with our droppe of Naturall truth: you may (now) Togine Cuber geve Cubes, one to the other, in any proportió geué: Rationall or Ir- weretheogeue Cubes, one to the Make hollow Parallelipipedon of Copper or Tinnc: with one Bafe wating, or opentas in our Cubike Coffen. Fró the bottome of that Raplemalier with one Bare wating, or openias perpendiculars, in euery of his fower fides. Now if $Z_{\text {mwnenalh, }}$ any proportion be affigned you, in rightlines. Cut one of your perpendiculars/or ", aline equall to it, or leffe then it ) likewife: by the ro, of the fixth of Enclide. And? thofe two paztes, fet in two fundry lines of thofe perpendiculars (or you may fet, " them both,in one line ) making their beginninges, to be, arthe bafe: and fotbeir " lengthes to extend vpward. Now, fee your hollow Parallelipipedon, ypright, , perpendicularly, feadic. Poure in water, handfomly, to the heith of your thorter, line. Poure that warer, into the hollow Pyramis or Cone. Marke the place of, the rifing. Settleyour hollow Parallelipipedon againe. Poure water into it: ""
vnto the heirl of the fecond line, exacty. Poure that water " duely into the "\% "Emptrvnto the heith of the fecond line, exialy. Poure that water duety into the "; Empty
hollow Pyramis or Cone; Marke nowagaine, where the water cuttect the fame ;" ing thi time which you marked before. For, there, as the firt marked line, is to the fe- $\Rightarrow$ friff. cond: So fhall the two Radicall fides be, one to the other, of any nwo Cubes: which, in their Soliditie, fhall hane the fame proportion, which was at the firt af: ," figned : wereit Rationall or Irrationall.
Thus, in fundry waies you may furnifhe your felfe with fuch ftraungeand promonftration Mastematicall. Which is, this : Alwaies, you haue two Like Pyramids : or two Like Cones, in the proportions afligned : and like Pyramids or Cones, are in proportion,one to the other, in the proportion of their Homologall fides (or lines) mipled. Wherefore, if to the firt, and fecond lines, found in your hollow Pyramis or Cone, you ioyne a third and a fourth, in continuall proportion : that fourth line, fhall be to the firf, as the greater Pytamis or Cone, is to the lefle : by the 33.0 the eleuenth of Euctide . If Pyramis to Pyramis, or Cone to Fundamentall Cube, to the Radicall fide of the Cube to be made, or to be doubled : and therefore, ro thofe wwaine alfo, a third and a fourth line, in continuall proportion, ioyned : will geue the fourth line in that proportion to the firft,as our ourn Pyramidall, or Conike line, was to his firt : buit that was double, or tre ble, \&ecas the Pyramids or Cones were, one to an other(as we haue proued) ther-
fore, this fourth, fhalbe allo double or treble to the firt, as the Pyramids or Cones were one to an other: But our made Cube, is defcribed of the fecond in proportion, of the fower proportionall lines; therfore ${ }^{*}$ as the fourth line, is to the fiff, fo "hyuthen is that Cube, to the firlt Cube : and we hane proted the fourch line, to be to the firft, as the Pyramis or Cone, is to the Pyramis or Cone: Wherefore the Cube is
ciij. to the

## Iohn Dee his Mathematicall Praface.



Nowehit
to the Cube, as Pytamis is to Pyramis, or Cone is to Cone. But we*Suppofe Pyramis wo Pyramis, or Cone to Cone, to be double or treble.\&c. Therfore Cube, is to Cube, double, or treble, \&cc. Which was to bedemonftrated. And of the Parallelipipedó, ir is cuidér, that the water Solide Parallelipipedons,are one to the other, as their hetthes are, feing they haue one bafe. Wherforethe Pyramids or Cones, made of thofe water Parallelipipedons, are one to the orther, as the lines are (one to the orher)lietwene which,our proportion was affigned. But the Cubes made of lines,atter the proportio of the Pyramidal or Conik homologall lines, are one to the other, as the Pyramides or Cones are, one to the other (as we before did proue) therfore, the Cubes made, fhalbe one to the other, as the lines affigned, are one to the other: Which was to be demonftrated. Note. *This,my Demonftratio is more generall, then oncly in Square Pyramis or Cone: Confider well. Thus, haue I, both Mathematically and Mechanically, ben very long in wordes:yet (I truft) nothing redious to them, who, to thele thinges, are well afreced. And verily 1 am forced (auotding prolixine)to me me forear Threafure t and to the Mechanicien to the Mathematricn, would be a grear Threafure : and to the Mechanicien, no
finall gaine."Now may you, Betwene two lines ginen, finde two middle proportionals, in Continuall proportion: by the hollow Parallelipipedon, and the hollow Pyramis, or Cone. Now, any Parallelipipedon rectangle being given:thre right lines may be found, proportionall in any proporlipipedon giuen. Hereof, I noted fomwhat vpon the 36 , propofition, of the Ir,boke of Ewdide. Now, all thofe thinges, which Vitrwaius in his Architeeture, fpecified hable ro be done, by dubbling of the Cube . Or, by finding of two middle proportionall lines, betwene two lines giuen, may eafely be petformed. Now, that Probleme, which I noted vnto you, in the end of my Addition, vpon the 34 -of the IT. boke of Enclide, is proued pofsible. Now, may any regular body, be Tranfformed into an other, \&c. Now, any regular body:any Sphere, yea any Mixt Solid: and
(that more is) Irregular Solides, may be made (in any proportió affigned) like vnto (that more is) Irregular Solides, may be made (in any proportio affigned) like vnto
the body, firft given. Thus, of a Manneken, (as the Datch Painters terme it) in the Gme Symonetrie, may a Giant be made: and that, with any gefture, by the Manncken vied : and contrarywife. Now, may you, of any Mould, or Modell of a Ship, make one, of the fame Mould (in any afligned proportion) bigger orleffer. Now, may you, of any ${ }^{\circ}$ Gunne, or little pecce of ordmauce,make an other, with the fanc
5 ymmeric ( in all pointes) as great, and as little,as you will.Marke thata on it. Infinitely, may you apply this, folong fought for, and now fo cafily concluded : and withall,fo willingly and frankly communicated to fuch, as faithfully deale with vertuous ftudies. Thus, can the Mathematicall minde, deale Speculatiuety in his own Arte: and by good meancs,
Mount aboue the cloudes and ferres : And thirdly, he can, by order, Defcend, to frame Naturall thinges, to wonderfullyfes and when he lift, retire home into his owne Centre : and there,prepare more Meanes, to Afcend or Deficend by : and, all, to the glory of God, and our honeft delectation in earth.
Although,the Printer, hath looked for this Praface, a day or two, yet could I not bring my pen from the paper, before I had giuen you comfortable warning, In the reft, I will therfore, be as brief, as ir is possible:and with, all, defcribing them, Somwhat accordingly. And that,you fhall perceine, by this, which in order com-

## Iohn Dee his Mathematicall Præface.

they can not prefcribe a certaine number of Artes:and in eche,cerraine vnpaffable boundes, to God, Nature, and mans Induftrie.New Artes, dayly rife vp: and there was no
man, be made knowen to the world.Let vs embrace the giftes of God, and wayes to wifedome, in this time of grace, from aboue, continually beftowed on them, who thankefully will receiue them: Et bonis Ommsa Copocrabuntur in bonum.

Trochilike, is that Art Mathematicall, which demonftrateth the properties of all Circular motions, Simple and Compounde. And bycaute the frute hercof, vulgarly receciued, is in Wheles, it hath the name of Trochilike: as a man would fay, Whele Art.By this art, a Whele may be geuen which Thall moue ones about, in any tyme affigned. Two Wheles may be giuen, whofe turnynges about in one and the fame tyme, (or cquall tymes), frasl haue, one to the othcr, any proportion appointed. By Wheles, may a fraightline be defcribed: Likewife, S Spirall line in plaine, Conicall SeCtion lines, and other Irregular lines, at pleafure, may be drawen. Thefe, and fuch like, are principall Conclufions of this Arte : and helpe forward many pleafant and profitable Mechanicall workes: 'As Milles, to Saw great and very long Deale bordes, no man being
by. Such haue Ifeene in Germany: and in the Citie of Prage : in the kingdome of Bohemia : Coyning Milles, Hand Milles for Corne grinding: And allmancr of Milles, and Whele worke: By Winde, Smohc, Water, Waight, Spring, Man or Beaft,moucd. Take in your hand, Carricola Dere Mectallica : and then ihall you (in all Mines) perccaue, how great nede is, of Whele worke.By Wheles, ftraunge workes and incredible, are done as will, in other Artes hereafter, appe.re. A wondeffull example of farther poffibilitie, and prefent commoditic, was fenc in my time, in a certaine Inffrument: which by the Inuenter and Artificer(before) was folde for xx. Talentes of Golde: and then had (by miffortunc)receaucd fome iniurie and hurt: And one Lanellus of Cremona did mend the fame, and prefented it vnto the Emperour Charles the fifth. Hereronymus Carrdsnus, can be my witneffe, that therein, was onc Whele, which mooced, and that, in fuch rate, that, in 7000 .yeares onely, his owne periode fhould be finiihed. A thing almoft incredible: Buthow farre, l keepe me within my boundes: very many men(yetaliue) can tell. Helicofophie, is nere Sifter to Trochilke: and is, An Arte Mathematicall, which demonftrateth the defigning of all Spirall lines in Plaine, on Cylinder, Cone, Sphree, Conoid, and Sphxroid, and their properties appertayning. The vfehereof, in Architecture, and diuerfe Inftrumentes and Engines, is moft neceffary. For, in many thinges, the Skrue worketh the feate, which, els, could not be performed. By helpe hereof, it is recorded, that, where all the power of the Citie of Syracuaf,was not hable to Engine, caufed Hirro the king, by him felf, at cafe, to remoue her, as he would.
 From this dav,
focure be fath.

Pneumatithmie demonftrateth by clofe hollow Geometricall Figures,(regular and irregular) the ftraunge properties (in motion or ftay) of the Water, Ayre, Smoke, and Fire, in theyr cótinuitie,

## IohnDee hisMathematicall Pratace.

meth next. - For, wheras, it is fo ample and wonderfoll, that, an whole yearelong, one might finde fruitfull matter therin, to fpeake of: fure endeles:yet will I glanfe ouer it, with wordes very few.

This do I call Anthropographie. Whicli is an Arreftored, and of my preferment to your Seruice. I pray you, thinke of it, as of one of thechicf pointes, of Humane knowledge. Although it be, but now, fint Coffirmed, with this new name : yet the matter, hathfoin the beginning, ben in confideration of all perfect Philofophers. Anthropographie, is the defcription of the Number, Meafure, Waight, Gigure, Situation; and colour of enery diuerle thing, conteyned in the perfect body of MAN : with certain knowledge of the Symmetrie, hgure, waigho, Characterization, and due locall motion, of any parcell of rhe fayd body; afsigned. and of Nubers, to the fayd parcell appertainynge This, is the one part of the Definition,mete for this place:Sufficicnt to notifie, the particularitie, and excellency of the Aree:and why it is, here, afcribed to the-Mathematicals. Yf the defcription of the heatuenly part of the world, had a peculier Art, called ©jfronomic : If the defcription of the carthly Globe, hath his peculier arte, called Gegraphic. If the Matching of both, hath his peculicr Artejcalled cof mograpthe: Which is the Defcriptió of the whole, and vaiucrfall frame of the world: Why fhould not the defcription of him; who is the Leffe world:and,fró the beginning; called eaicrecof mus (that is. MerN N The LeßeWorld. And for whofe fake, and feruice, all bodily creatures cls, were the Leffe created : Whocalfo,participateth with Spirites, and Angels:and is made to the Irather, then, either to want a name, or to haue to bafe and improprea name: You rather, then, either to want a name, or to haue to baie and improprea name: You
muft offiudry profeffions, borow or challenge home, peculier partes hercof:and farder procedé:as, God, Nature, Reafon and Experience fhall informe you. The Anatomiftes will reftore to you,fome part:Thic Phyfiognomiftes, forme: The Chyt Anatomintes wifrettore to you,fome part:ince Phytiognomites, fornc: the Chyt
 Hipocrates; $i^{1}$ lato; Galenus, Meletins, \& many other (in certaine thinges) will be ConHipocrates; Plato;Galenus, Meletiks, 8 many other (in certaine thinges) will be Con-
míbutaries. And farder, the Heauen, the Earth, and all other Creatures, will eche fhew, ard offertheir Harmonious feruice, to fill $v p$, that, which wanteth hereof and with your, own Experience, concluding: you may Methodically regitter the whole, for the pofteritie; Whereby, good profe willbe had, of qurHarmonious, and Microcofmicall conftitution. The outward Imyge, and yew hereof to thic Art of Zograpbeve and Painuing, to Sculpture, and Archiriecture: (for Church, Houtfe, Forgor Ship) is moft neceflary ant profitable for that, it is the chiefe bafe and foumdation oftiem. Iooke in wirwaus, whether I deale fincerely for your
 der the Apkc of N ece. And by that, wade farther. Rememberthe Delphicall oracle
 many a Philofopher repeated : and of the Wifeit attempted, And then, you will perceave, how lóng agoe, you hate bene called to the Schote, whete this Arte might be logined. Well. Iam nothingeftaydejef che difdayne offone fuch, as rance, and fhame enougb, come fiort of them Scuen alfo:, and yer newertheleffe rance, and fhame enougb, come fhort of them Scuen aifo:, and yet nenertek
c.iiij.

## Iohn Dee his-Mathernaticall Praface.

and as they are ioyned to the Elementes next them. This Arte, to the Naturall Philolopher, is very proffitable: to proue,that Vacuum, or Emptines is not
in the world. And that all Nature, abhorreth it fo much:that, contrary to ordinary law, the Elementes will moue or ftand. As,Water to afcend:rather then betwene him and Ayre,Space or place fhould be left, more then(naturally)that quaftitic of Ayre requireth, or can fill, Againc, Water to hang, and not defeend:rather then by defcending, to leaue Emptines at his backe. The like, is of Fire and Ayre: they will defcend: when, either, their Cótinuitie Chould be diffolued:or their next Element forced from them. And as they will not be extended,to difcontinuitie: So,will they not, nor yct of maps force, can be preft or pent, in fpace, not fufficient and aunfwerable to their bodily fubftance. Great force and violence will they vfe, to enioy their naturall right and lioertie. Hereupon, wo orthree mein together, Togos ath by keping Ayre vnder a grear Cauldron, and forcyng the fame downe, orderly, may without harme defcend to the Sea bottome : and continue there a tyme \& C. Where, Note, how the thicker Element(as the Water) giucth place to the thynner (as, is the ayre:) and receiueth violence of the thinner, in raner. \& \&c. Pumps and
all maner of Bellowes, haue thcir ground of this Art: and manyy all maner of Bellowes, haue their ground of this Art: and many other ftraunge dcuifes,As,Hydraulica, Organes goyng by water.\&c. Of this Feat, (called common-
ly Pneumatica, ) goodly workes are extant, both in Grekc; and Latin. With old ly Pnewmatica, ) goodly workes are extant, both in Greke, and
and learned Schole men, it is called Scientia de plenoc vacwo.

Menadrie, is an Arte Mathematicall, which demonftrateth, how, aboue Narures vertue and power fimple: Vertue and force may be multiplied : and fo, to direct, to lift, to pull to, and to put or caft fro, any multiplied or fimple, determined Vertue, Waight or Force:naturally, not,fo, directible or moucable. Very much is this Art furdred by other Artes : as, in fome pointes, by Pofpective: in fome, by Statike : in fome, by Trochalke and in othcr, by Helicofophie and Pnewm.ttithmie. By this Art, all Craves, Gybbettes, \& Ingines to lift vp, or to force any thing, any maner way, are ordred: and the certaine caufe of their force, is knowne: As, the force which one men hath with the Duche waghen Racke :therwith, to fet vpagayne, a mighty waghen laden, being oucrthrowne. The force of the Croffebow Racke, is certainly ,here, demonftrated.The reafon, why one ma, doth with a leaucr, lift that, which
Sixe men, with their handes oncly, could not, fo eafily do. By this Arte in our Sixe men, with their handes oncly, could not, fo cafily do. By this Arte, in our common Cranes in London, where powre is to Crane vp, the waight of 2000. pound: by two Wheles more (by good order added) Arte concludeth, that there may be Craned vp 20000 .pound waight \&c. So well knew Archimedes this Arce:
that he alone, with his deuifes and engynes, (twife or thrife) (poyled and difcomfited the whole Army and Hes and enges, (wife or dieing pyreced and dircomficellus the Conful, being their Gencrall Capinine. Such huge Stones, fo many, with celuas the Conjul, being their Gencrall Capitaine. Such huge Stones, 1 o many, with nuewione. Citie. And by Scalikewitc : the cu/d , yet hee vtterly confounded the Romaine Nauye. What with his mighty (4f/a, yet hee vtterly confounded the ciomaine Nauye. What with his mighty ced almoft a quarter of a myle:What, with his catchyng hold of their Shyps, and hoy fing them vp aboue the water, and fuddenly letting them fall into the Sea againe:what with his* Burning Glaffes:by which he fired their other Shippes a fargaine:what with his Burning Glaffes:by which he fired their other Shippes a far- qumen
of: what, with his other pollicies, deuifes, and engines, he fo manfully acquit him felfe : that all the Force, courage, and pollicic of the Romaines (for a great fafon) d.j.

## Iohn Dee his Matherraticall Preface．

couldnothing prcuaile，for the winning of Sytaculd．Wherupon，the Romanes named Archimedes，Briar ous，and Cortimanus．＇Zonuras maketh mention of one Pros chus，who fo well had percenved Arclimedes Arcé of CHemadrie，and hatd fo wellitit uented or his owne，that wath his Burning Glaffes，being placed vpon the walles thefame againit his enemies Nauie with fuch force and fo fodeinly（like Fighte ning that he burned and defroyed both manand fhip．And Dron＇fpeciffeth of Prijcuspa Geopetrition in Byfance，who inuented and ved doindry Engins，of Force muluiplied：Which was caufe，that the Emperour Sewerns patrdoned him，his life，af ter he had wonpe Byfance：Bycaufe he honored the Arte，wytt，and rareandufrie of $P$ rijans．But oothing inferior to the intucntion of thefe engines of Forçe，was the inuention of Guanes．Whicia，from an Enslifh man，had the occafion andd order
of fint inuenting：thoughin arrocher hand；and by other men，it was firf execated． And they thas fhould fee therecosd，wherethe occafion and order generailf，of
 $n$ commingto wife mens confideration，and induftrieus mens handling，nay grow ＂，to be of furce incredible．

Hypogäodie，is an Arte Mathematicall，demonftratyng，how， vnder the Sphrricall Superficies of the earth，at any depth，to any perpendicular line afsigned（whofe diftance from the perpendicular of the erstrance：and the Azimuth，likeivife，in ref pect of the Gaid en－ trance，is knowen）certaine way may be prefcribed and gone ；And how，any way aboue the Superficies of the carth defigned，may wn， fer earth，at any depth limited，be kept ：goyng alwayes，perpendi－ cularly，vnder the way，on earth defigned ：And，contrarywife，Any way，（itraight or croked，）vnder the earth，beyng giuen ：vppon the vtfaze，or Superficies of the earth，to Lyne out the fame：So，as，from theCentre of the earth，perpendiculars drawen to the Spharicall Superficies of the earth，fhall precifely fall in the Correlpondent pointes of thofe two wayes．This，with all other Cafes and cir－ cumftances herein，and appertenances，this Arte demonftrateth This Arte，is very ample in varietie of Conclufions：and very profitible fundry wayes to the Common Wealth．The occaffon of iny Inuentingthis Arte，was a the requeft of two Gentlemen，who had a certainev orke（of gainc）vnder ground：
and theirgroundes did ioyne ouer the worke ：and by reafon of the crokednes， and theirgroundes did ieyne ouer the worke ：and by reafon of the crok and
diuers depthes，arid heithes of the way vnder ground，they were in doubr and at controucfic，vnder whofe ground，as then，the worke was．The name oncly（be－ corethis）was of me publiflied，De Ittinere Subterrance：The reft，be at Gods will． For Pioncrs，Miners，Disgers for Metralls，Stone，Cole，and for fecrete paffages For Pioners，Miners，Diggers for Mettalls，Stone，Cole，and for fccrete paflages
vnder ground，betwene place and place（as this land hath diterfe）and for other purpofes，any man may eafily perceaue，both the great fruite of this Arte，and alfo in this Arte，the great aide of Geometrie．

Hydragogie，demonttrateth the poffible leading of Water，by Natures lawe，and by artificiall helpe，from any head（being a Spring，ftanding，or running Water ）to any other place affigned．

## Iohn Dee his Mathematicall Prxface

by Sunne or Sterres direftion（in certaine time）require ouerfight and reformati－ on，according to the heauenly Æquinoctiall Motion：befides the inxqualitie of their owne Operation．There remayneth（without parabolicall meaning herein） ous way，then all thefe：of hauing ellent，more commodious，and（or firf xquino－ ctiall motion，）by Nature and Arte，Imitated：which you fhall（by furder fearch in waighticr ftudyes ）hereafter，vnderftand morc of．And fo，it is tyme to finifh this Annotation，of Tymes diftinction，vfed in our coinmon，and priuate affaires：The
ommoditie wherof，no man would want，that can tell，how to beftow his tyme．
Zographie，is an Arte Mathematicall，which teacheth and de－ monftrateth ，how ，the Interfection of all vifusll Pyramides，made by any playne afsigned，（ the Centre，diftance，and lightes，beyng de－ ermined ）may be，by lynes，and due propre colours，reprefented． A notable Arte，is this＇and would require a whole Volume，to declare the proper－ ty thereof：and the Commodites enfuyng．Great fkill of Geometrie，Arithme－ fike，Perfpefliue，and Anthropographe，with many other particular Artes，hath the Zo． rapher，nede of，for his perfection．For，the moft excellent Painter，（who is but the propre Mechanicien，\＆Imitator fenfible，of the Zographer）hath atteined to fuch perfeciion，that Senfe of Man and beaft，haue iudged thinges painted，to be things naturall，and not artificiall：aliue，and not dead．This Mechanicall Zographer（com－ monly called the Painter）is meruailous in lus fkill：and feemeth to haue a certaine diuine power：As，of frendes abfent，to make a freadly，prefent comfort：yea，and our pofteritie，formany Ages．And fo procedyng，Confider，How，in Winter he our pofteritie，for many Ages．And io procedyng，Confider，How，in Winter，he he countenance of Winters dolefull State and nakednes．Cities，Townes，Fortes Woodes Armyes，yea whole Kingdomes（be they never fo farre，or greate）can Woodes，Arnyes，yea whole Kingdomes（be they neuer fo farre，or greate）can of the thinges rehearfed．In one little houfe，can he，enclofe（with great pleafure of the beholders，the portrayture lively，of all vifible Creatures，either on earth，or in the earth，lining：or in the waters lying，Creping，fly ding，or fwimming：or of any foule，or fly，in the ayre flying．Nay，in refpect of theStarres，the Skie，the Cloudes： yea，in the fhew of the very lightit feffe（that Divine Creature）can he match our eyes Iudgement，moft nerely．Whata thing is thist thinges not yet being he can reprefent fo，as，at their being，the Pifture flall feame（in maner）to haue Created them．To what Artificer，is not PiCture，a great pleafare and Commoditie！Which of them all，will refufe the DireCion and ayde of Picture？The Architett，the Gold－ inith，and the Arras Weauer：of Picture，make great account．Our liuely Herbals， our portritures of birdes，beaftes，and filices ：and our curious Anatomies，which way，are they moft perfectly made，or with moft pleafure，of vs beholden：Is it not， by Pictulc onely？And if Pieture，by the Induftry of the Painter，be thus commo－ dious and meruailous：what fhall be thought of Zograp prie，the Scholemafter of Pi－ ture，and chief gouernor！Though I mencion not Scu／ptare，in my Table of Artes Mathematicall：yet may allmen percciuc，How，that Picture and Sculpture，are Si－ fers germainc：and both，right profitable，in a Commó wealth．and of Sculpture，af－ well as of Picture，excellent Artificers haue written great bokes in commendation． Witneffe I take，of Georgio Vafari，Pittore Arctino：of Pomponius Gauricus：and other． To thefe two Artes，（with other，）is a certaine od Arte，called Althalma／at，much beholdyng：more，then the common Sculptor，Entayler，Kerucr，Catter，Grauer，Foun－
der，

## IohnDee his Mathematicall Praface．

Long，hath this Arte bene in vee：and much thereof writeen ：and very marueilous Workes thercin，performed ：as may yet appeare，in Inly：by the Ruynes remaining
of the Aqueduetes．In other places，of Kiners leading through the Maine land， of the Aqueductes．In other places，of Riners leading through the Maine land， rer to Afcend ．which all，declare the great fill，to be required of him，who fhould in this Arte be perfecte，for all occafions of waters poffible leading．To fpeake of the allowance of the Fall，for euery hundred foote：or of the Ventills（if the wa－ ters labour be farre，and great）Incede not：Seing，ar hand（aboutvs）many expert men can fufficiently teffific，in cffeete，the order：though the Demonftration of the Neceffitic thereof，they know not ：Noryet，if they fhould be led，vp and downe，and about Mountaines，from the head of the Spring：and then，p pace be－ rep pette of the head，from which（fo crokedly，and yp and downe）they be come： Pethaps，they would not，or could nor，very redily or nerely affoyle that gueftion． Gemerrie therefore，is neceffary to H y dragegie．Of the fundry wayes to force wi－ ter to afcend，eyther by Tympane，Kettell mills，Slerae，Cteflijke，or fuch like：in $/ 2$ trumiw，Usrued，（and other）fully，the maner may appeare．And fo，thereby，allo be molt euident，how the Artes，of Peaunatithonie，Helitofephic，Statike，Trochilike， and Crenadrie，come to thefurniture of this，in Speculation，and to the Commo－ ditie of the Common Wealth，in practife．

Horometrie，is an Arte Mathematicall，which demöfrateth， how，at all times appointed，the precifervfiall denominatió of time， may beknowen，for any place affigned．Thefewordes，are fmothand plaine eafic Englifhe，but the reach of their meaning，is farther，then you woulde of lare，Horologrigrathta：and in Englifhe，may be temned，Distling．Auncient is
 bene（at the lealt）aboue two thoufand and three hundred yeare agoe ：in ${ }^{*}$ King 4. Rtg．ao， Cchate Diall，then，by the Sunne，fhewing the diftinction of time．By Sumne， Mone，and Sterres，this Dialling may be performed，and the precife Time of day or nighitknowen．But the demonftratiue delineation of thefe Dialls，of all fortes， requireth good／Kill，both of Aifirenownie，and Geometricie Elementall，Sphaxicall，Phx－ nomenall，and Conikall．Then，tove，the groundes of the Arte，for any regular Superficies，in any place offred ：and（in any pofible apt pofition therof）theron，
to defcribe（all maner of wayes）how，vfial dow ）truely deternined ：will be found no fleight Painters worke．So ro Paint， and prefcribe the Sunnes Motion，to the breadth of heare．In this Feate（in my youtb）I Inuented away，How in any Horizontall，Murall，or．Equino． ciall Diall，\＆c．Atall howers（theSunne fhining）the Signe and De－ gree afcendent，may be knowen．Which is a thing very neceffary for the Rifing of thofe fixed Sterres：whofe Operationin the Ayre，is of great might， euicently．Ifpeake no further，of the vie hereot．But forafimuch as，Mans affures
feguireknowledge of Times $\&$ Momentes，whei，neither Suinne，Mone，orSterre， regureknowiadge of T toes \＆Momentes，when，neither suntie，Mone，or Sterte，
cantefence：Therefore，by Induftrie Mechanicall，was iniented，firt，how，by Wa－ ter running onderly，the Time and howersimightbe knowen：whereof，the famous Cigitiou，was Inuentor ：a man，of $V$ itruyise，to the Skic（juefly）extolled．Then， after that，by Sand rumining，were howers meafured＇Then，by Trochilke with waight：Andoflatetine，by Trachiluke with Soring：withotit waight．All theff，
dij．by

## IohnDee his Mathematicall Preface．

der，or Paynter（ $(\dot{C})$ know their Arte，to be commodious．
Architecture，to many may feme not worthy，or not mete，to be reckned An obiectien， anong the Artes Afathematicall．To whom，I thinke good，to giuc fome account of my fo doyng．Not worthy，（will they fay，）bycaufc it is but for building，of a houfe， Pallace，Church，Forte，or fuch like，gronte workes．And you，alfo，defined the Antes fodiddcmonftratiuely procede in their faculty by Number or Marnitude．Firto you fec，that I count here，Archite fivre，among thofe Artes Matliematicall，which The Amfow． you fe，that I count，herc，Archintecture，among thoie Chrtes，Mathemaficall，winch
are Deriued from the Principals ：and you know，that fuch，may deale with Na － are Deriued from the Principals：and you know，that fuch，may deale with Na －
turall thinges，and fenfible matter．Of which，fomedraw nerer，to the Simple and turall thinges，and fenfible matter．Of which，fome draw nerer，to the Simple and
abfolute Mathematicall Speculation，then other do．And though，the Architect procureth，enformeth，\＆directeth，the Mechanisiem，to handworkc，\＆the building＂ actuall，of houfe，Caftell，or Pallace，and is chicf fudge of the fame：yet，with him＂， felfe（as chief C Mafter and Architect，）renaincth thic Demonitratiue reafon and＂， caufe，of the Mechaniciens worke in I．yne，plaine，and Solid ：by Geometricall，A．＂， rithmetticall，opticall，Muficall，sironomicall，Cofmegraplicall（\＆to be brief）by all the＂， former Deriued Artes Mathematicall，and other Naturall Artes，hable to be confir－ med and fablifled．If this be fo：then，may youthinke，that Architeflure，hath good and due allowance，in this honeft Company of Artes © AFathematicall Deriuatiue． I will，hercin，craue Iudgement of two moft perfect Irchitelies：the one，being $V t_{\text {，}}$ ， trawiss，the Romaine ：who did write ten bookes thereof，to the Emperour CAugu－ Hus（in whofe daies our Heauenly Archemafter，was borne ）：and the other，Lee Baptifta Albertue，a Florentine ：who alfo publithed ten bookes therof ．Archi－ tectura（ fayth Vitrunins）eit Scientiap pluribiss difciplinis of varrijs crudisionibus ornata： coius Indicio probantur omnia，que ab ceteris Artificibus perficientur opera．That is． Architecture，is a Science garnifhed with many doctrines \＆diuerfe inftructions：by whofe Iudgement，all workes，by other workmen finifhed，are Iudged．It followeth．Ea nafcitur ex Fabrica，\＆Ratiocinatione．\＆＇c． Ratiocinatio antem eit，quec，res fabricatas，Solertiz ac ratione proportionis，demenfirare at ofs explicarepoteit．Arclitetiure zroweth of Framing，and Reafoning．心c．Rea－ joning，is that，which of thinges framed，with forecaft，and proportion：can make demonstration，and manifeft declaration．Againe．Cinr，tn omnibus enim re－ bus，tium maximè ctiam in Architcifura，hac duo inf sunt：quod fignificatur，of quod figni－ ficat．Significatur propofita res，de qua dicitur ：hanc autem Significat Demonfiratio，rati－ ounibus docirinarum explicata．Forafmuch as，in all thinges therefore chiefly in Architelfure，thefe two thinges are ：the thing（ignified ：and that which fig： nificth．The thing propounded，vebereof we peake，is the thing Signified． But Demonftration，expreffed with the reafons of diverfe doctrines，doth figni－ fie the fame thing．After that．Vt literatus fit，peritus Graphides，eruditus Geometrie， or optcice non ignarur ：infruchus Anithmetica：bylarias complares nowerit，Philof ophos

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nowerit：Afrologiam，Caltíg rationes coonitas habrat．An Architedf（fayth he）ougbt nowerit：Afrologiam，Caltog rationes cognitas habrat ．An Arcbitelt（fayth he）ougbt
to onderftand Languages，to be fkilfull of Painting，well inftaffed in Geomeo to Inderftand Languages，to be f kilfuill of Painting，well inftracted in Geome－ trie，not ignorant of Perjpeltiue，furnifhed with Arithimetike，bane knowledge of many biftories，and dilivently baue heard Philofophers，hawe fkill of Mu－ fike，not ignorant of Pbylike，know the aunfiveres of Lavyers，and lawe Aftro＊

Iohn Dee his Mathematicall Prxface.
nomic, and the courfes Celestiall, in good knowledge. He geucth reafon, or dcrly, wherefore all thefe Artes, Doetuines, and Inftructions, are erequifite in an cxcellent Architrif. And (for breuitic) omitring the Latin texe, whus he hath:
Secondls, it is bebof efull for an Arclitectit to bane the knowledge of Paintmg: that he may the nore eaf ihe fafpion out, in patternes painted, the forme of what zorke ke liketh. And G cometrie, geuetb to Architecture many belpes : and first reasheth the V/e of tbe Rule, and the Compaa Be: wherby (chiefy and eaflice) the deforiptions of Buildinges, are def patched in Groundplats: and the direetrions of Squires, Levells, and Lines. Litewije, by Perfpectiuc, the Lightes of the bean wen, are well led, in the bsildinges: from certaine quarters of the world. By Arithmetike, the charges of Buildinges are fummed together: the meaf fures are Arithmetike, the charges of Buildinges are fummed together: the meaf fures are exp Metbods dif conred ed on. GC. Defides this, of the Nature of thinges (Thict in Greke is called poveeneria) Pbilofophie dotb make declaration . Which, it is neceflary, for an Archirett, with, diligence to haue learned: becaufe it hatb mavo und dikers naturall queftions: as fpecially, in Aquedubfes. For in their coarfes, leadinges about, in the lewell gromod, and in the mountinges, the natue rall Sp pirites or breathes are ingendred disers wayes: The bindrances, which,
 they caufe, no man can belpe, but be, which ont of Pbitlo oppint, bath learned the
criginall canfes of thinges. Likewife, woho oener Mall read Cefibius, or Are
 theo do: vileffe be hall bauce receaued of Philofopbers, infirubtions in thefe thinges. And Muifike be muft nedes know : that be may batic onderstanding, both of Regnlar and Afathematicall Mufike: that he may temper well his BaIiftes, Catapultes, and Scorpions. ©c. Moreoner, the Brafen Veffels, which in Theatres, are placed by Matbematicall order in ambries, wnder the Steppes: and the diuer fties of the foum des (wbichy G Grecians call incüa) are ordred according to Mu/ icall Symphonies is Harmonies:being diflributed in' ' Circuites, by Dis atrfjaron, Diapente, and Diapg fon. That the conuenient nogre, of the players fownd, wk'it came tothrfe preparations, made in order, there being increafed: with 'j incresfing, might come more cleare or pleaf ant, to jeares of the lokers on. Ec. And of Afirmomie, is kuowe"f Eadt, wr est, Soutt, and Nortb. The fa foion of the leaucn, the Equinox, the Solfticie, and the conrfe of the ferres. Which thinges, vulceff tone knop:be cannot perceine, any thyng at all, the reafor of Ho-

 connt then felwes Architedes, of the Jxddeyme. But they onely, who from their childes geares, afcendyng by thefe degrees of knowledges, beyng foisered vp with the attrynung of many Languages and Artes, baue wonne to the bigb Taber= गidcle of Archiffure. © C. And to whom Nature bat b given Juch quicke Circum: Jidicico Archith, (h. ypure of witt, and Memorie, that they may be pery abfolutel) Joill. fulin Grometric, Aftronomie, Mufke, and the reftof the Arter Mathematio
rall

Iohn Dechis Mathematicall Preface.
call:Suth jfurmanit and paffe the callyng; anilfate, of Architeffes: and are bee A Whatie: come Matbematiciens:ivc. And they are fownd, feldome. $A s$, in $y$ mes pad $f$; was maticien.
 Eratofthones Crrencus:Arcbimedes, and Scopas, Syracufians. Who aljo, left to ther poferitice,many Engines and Gnomoncall workes: by numbers and natso rall meanes, inuented and declared.
Thus miuch, and the fame wordes (in fenfe) in one onely Chapter of this Incoí parable Architeal Yitruutus, fhall you finde. Arid if you fhould, but tikel his boke in your hand and flightly loke thorough it, you would fay fraight why: This 's Geo
 and/(to cōclude the Storchoufe ofall workmallip, Now, ,let vs liften to our otice Iudge,our Florecitine, Lre Emptiffyenid narrowly confide, how he doth determme
 (faytilie) I thinke, that Iought to expreffe, what man I would bane to bee al lowedan Architeef. For, I will not brymg in place a Carpenter :as thowgh yous mighe Compare bim to the Chief Maflers of otber Artes. For the band of the Carpeniter, is the Architettes In Itrament. But I willappoint the Arccuitedito be Vyho in an


 dyes, maj most aptly be Commodious for the woorthief V V fx of Man. And it bat be," may be abie to performe thefe thinges, be bath nede of attennng dad knowiledge of the beft, andmoft worthy sly yiges, EC. The tidole Feate of Architecture in buiddong, confiseth in Lineedmentes and in Framyigs And the whole power bud b in of Linementes tendemto this: that the right and abbolute ix is mai be biad of Coapteng and tionimg Lines and an gles:ly which, the face of the buil
 dnig or frame, may be comprelended and concluded. Ana tris tre propery of O certainge nuib cr: a vorthy maner, and a /enety order: that, $f 0, j$ whole forme and figave of the buildyng, mayreft in the very Lineamentes. OC. And we may *The tow. prgcribe in mynde and imagination the whole formes, "all materiall fulfe be marmintie yyg jectudd dwhich poimt we /hallatte jue; by Nootjog and forepointyng the an. gies, and Lnes, by a furre and certaine direffion and connexion. Sonng thpen, the fe
 and weyt. We thanke yoù Mafcr Baptijit, hat you haue fo apdy brought your , Arre, and phrafe therof, to hauefome Matheimaticall parfetion: by certaine or-", शeote.
 part. Now, then, it is cuident, (Gente reader) how aprely and worthely, I haue Prefared Xrchitecilure, tobe bred ind fofteridxpp in thit Dominionrof the perces


 Wherupont,hé is neither Soith, nior Builder:uorseparately, any Artificer: but the
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Hed,

## Iohn Dee his Mathematicall Praface.

opportunitatef:g tomporum prefentire, nor minus rei miltari, guàm Agricalture, Naniga. tuonig. conucrit. T'o forefee the alterations and opportunities of tymes, is conve. nient, no lejse to the Art of Warre, then to Huj bandry and Nauigation. And befides fuch cunnyng meancs, more cuident tokens in Sonnc and Mone, ought of hym to be knowen: fuch as (the Philofophicall Poëte) V rrgilius tcacheth, in hys Gieorgikes. Where he fiyth,

Sol quage cc cxoricoss ó quan fe condet in vondes,
Signa dalit, Solem certijomat figna fqquuntar -óc.

- 2 - $m$ Jape videmus,

Pfons in seitrn evirios crrare colores.
Sin mucule incipiont ratilo immnf corier igni,
Ommid tum partice vento, mombifor vadd is
Forere: non illa quifquam me nolle per altuis
Ire, neg, a terra amoncat connellere funcm. oc
Soltibit figns dabit Solom quis diccre falfom
Audent? - óc.
And fo of Mone, Sterres,Water, Ayre,Fire, Wood,Stones, Birdes, and Beaftes, and of many thynges els, a ccrtaine Sympathicall forewarnyng may be had: fometymes to griat pleafure and proffit, both on Sca and Land. Sufficicntly, for my prefint purpole, it doth appeare, by the premifles, hcw Mathematicall, the Artiof Nuseigation, is:and how it nedeth andalfo veth other Mathematicall Artes : And now, if 1 would so about to fpeake of the manifold Commodities, commyng to this Land, and othets, by Shypps and Nasugation, you might thinke, that I catch atoccafions, to vfe many wordes, whereno nede is.

Yet, this one thyng may I,(iufly)fay. In Nanigation, none ought to haue greater care, to be fkillfull, then our Englifh Pylotes. And perchaunce, Some, would more attempt: And oher Some, more willingly would be aydyng, it they wift cer-
tainely; What Priuiledge, God had endued this Iland with, by reafon of Situation, moft commodious for Natrization, to Places mof Fanous \& Riche. And though, (of* Late) a young Gentlcman,a Courragious Capitaine, was in a great ready- Anno. $5 \varsigma 67$ nes, with good hope, and great caufes of perfuafion, to haue ventured, for a Dif. S.H.G. nes, with good hope, and great caufes of perfuafion, to haue ventured, for a Dirccuě̀ye, (cither Wofferly, by Cape de Paramantia : or Effcrly, aboue Nous Zemlt, at.d the Cyromiffes and was, at the very ncre tyme of Attemptyng, callcd and cmFioyed otherwife(both then, and fince,) in great good feruice to his Countrey, as the Inifh Rebels haue *taftcd: Yct, I fay, ( though the fame Genticman, doo not *Anno. 1569 Lereatter,deale therewith) Some onc, or other, fhould liften to the Matter: and by cood aduile, and dircrete Circumpection, bylittle, and little, wynne to the fufficient knowledge of that Trade and Voyage:Which, now, I would be fory, (through Carelefncffe, want of Skill, and Courrage, ) Mould remayne Vnknowne and vnheard of. Seyng, alfo,we are hercin, halfe Challenged, by the learned, by halfe reçuef, publihed. Therof, verely, might grow Commoditye, to this Land hiefly, and to the reff of the Chriften Common wealth, farre paffing all riches nd vorldly Threafure
Thaumaturgike, is that Art Mathematicall, which giueth certaine order to makeftraunge workes, of the fenfe to be perceiued, and of men greatly to be wondred at. By fundry meanes, this wordar. worke is wrought. Some, by Pvenomatithmic. As the workes of Ctefibies and flero,

## Iohn Dee his MathematicallPraface.

Some by waight.wherof T imats fpcaketh.Some, by Stringes frayned, or Springs, therwith Initating liuely Motions.Some, by other meanes, as the Images of Mcrcurie: and the bralen hed, made by Albertus Magnew, which dyd feme to fpeake. Boc. thaus was excellent in thefe feates. To whom, Cafiodorur writyng, fayth. Your purpofe is to know prof ound thynges:and to gheio mernagles. By the dispofition of jour Arte, Metals do luw: Diomedes of braße, doth, blow a Trumpet loude : a brafon Serpent biffeth:byrdes made, fing/wetely. Small thynges we rehearfe of yon, who can Imitate the beanen.ecc. Of the ftraunge Selfnouyng, which, at Saint Denys, by Paris, 1haw, ones or twife (Orontias beyng then with me, in Company) it were to ftraunge to tell. But fome have written it.And yct, (I hope) it is there, of other to be fene.And by Per/pectiue allo Itraunge thinges, are done.As partly(before)I gaue you to vnderfand in Perfectiue.As, to fee in the Ayre, a loft, thelyuely Image of an other man, either walkyng to and fro: or ftandyng fill. Likewife, to co:ne into an houfe, and there to fee the liucly fhew of Gold, situer or precious ftones :and commyng to take them in your hand, to tinde nought but Ayre. Herchy, haue fome men (in all orher marters counted wifc) fouly ouerhot

 a dayes, tre /ce fome men, yea of great learnyng and reputation, to Indge certain woykes as meruag lous, abone the power of Natare: Of whlich workes, one that were $\int$ killfull in Perspetfiue might eafely baue ginen the (anfe. Of Archimedes Sphare, Cuere witaefferh. Which is very fraunge to thinke on. For when Archi. medes(Gyth he) did faften in a Sphare, the monyuges of the Sonne, Mone, and of the five other Planets, be did, as the God, which (in Timeus of Plato) did make the world. T bat, one tsrnyg, fhould rule motions moft mnlike in flownes, and fiviftnes. Buta greater caufe of meruayling we haue by cluwdunum report hereof. Who affirmeth this Archimedes worke, to haue ben of Glaffe. And difcourfeth of it
more ar large:which I omit. The Doue of wood, which the Mathematicien Armore at large:which I omit. The Doue of wood, which the Nathomaticies Ar-
 flotle, in hys Politikes, of both, maketh mention. Mcruaylous was the workemanShyp, of late dayes,performed by good fkill of T rochilike. ofc. For in Noremberge, A flye of Icra, beyng let out of the Artificers hand, did (as it were)fly about by the geftes,at the eable, and ar length, as though it were weary, retourne to his maffers Towne, a mighty way, and that a loft in the Ayre, toward the Emperour commings thether:and followed hym, beyng come to the gate of the towne." Thus, you fee, whar, Arte Mathematicall can performe, when Skill, will, Induftry, and Hability, are duely applyed to profe.

ANd for thefe, and fuch like marueilous AAtes and Feates, Narurally, Mathematically, and Mechanically, wrought and contriued : ought any honeft Student,
and Modef Chriftian Philofopher, be counted, \&called a Coniurer ? Shall and Modef Chriftian Philofopher, be counted,\& called a Coniurer ? Shall the folly of ldiotes, and the Mallice of the Scornfull, formuch preusile, that He, who fecketh no worldly gaine orglory at their handes : But onely, of God, the threafor of heaucnly wifedome, \& knowledge of pure veritic : Shall he (I fay) in the mean
fpace,

## Iohn Dee his Mathematicall Praface.

dumnation? To forfake the light of heauenly Wifedome: and tolurke in the dungeon of the Prince or darkenefie? To forlake the Veritie of God, \& his Creatures and to fawne vpon the Impudent, Craftie, Ob/tinate Lier, and continuall difgracer of Gods Veritie, to the vetermoft of his power? Toforake the Life \& Bliffe Arernall : and ro cleaue vnto the Author of Death euerlafting ? that Murderous Ty rant, moft gredily awaiting the Pray of Mans Soule ? Well : I thanke God and our LordeItefus Chril, forche Comforr which I haue by the Examples ofother men, bcfore my time: To whom, ncither in godlines of life, nor in perfection of learning, I an worthy to be compared: and yet, they fuftained the very like Iniu nes, that I do : or rather, greater. PacientSocrafte, his apologie will cetific : Apu Earle of Mirandula, his Apolegie will teach you, of the Raging flaunder of the Ma Earle of Mirandula, his Apologie will teach you, of the Raging flaunder of the Mahe had occafion romake publike Proteftation : as well by reafon of the Rude Sim rle : as alfo, in refpect offuch, as werecounted to be of the wifeff fortofmen. Many could I recire: But I deferre the precife and determined handling of this mat", rer: being loth ro detect the Folly \& Mallice of my Native Countrey men.* Who, ", fo hardly, can difgett or like any extraordinary courfe of Philofophicall Stadies: n not falling within the Cumpaffe of their Capacitic: or where they are not made " provic of the true and fecrete caufe, of fuch wonderfull Philofophicall Feares, Thefe men, are of fower fortes, chiefly. The firf, I may name, Vaine pratling binfie lodies: The fecond, Fond Frendes : The third, Imperfeally zeloas: and the fourth Walhioms Igmant. To eche of thefe (briefly, and in charitic) I will fay a word 3. Drtwo, and!o returne to my Praface. Vaine pratling bufie badies, vfe your idle affemblies, and conferences, otherwife, then in talke of matter, either aboue your Capacirics, for hardneffe : or contrary to your Confciences, in Veritic. Fonde 2. Fremaes, leaue of, fo to commend your vnacquanied frend, vpon binde affection As, becuufe he knoweth more, then the common Student: that, therfore, he muft needes be fallul, and a doer, in fuch mater and maner, as you terme Coinging Weening, thereby, you duancehis learned frend. Ceafe to aferibe Impreat where you pretend Anitic. For, if your tounges were true, then were that your frend, rontrar, both to God, and his Soueraigne. Such Frendos and Fondirgese, I Thake of, and renounce you: Shake you of, your Folly. Imperfeefly zelous, to you, 3. do I Gay: that (perhaps) well, do you Meane : But farre you miffe the Marke: If a Lambe you will kill, to feede the focke with his bloud. Sheepe, with Lambes bloud, haue no naturall fuffenaunce : No more, is Chriftes flocke, with horrible Quanders, duely adibed. Nor your fuire pretenfe, by fuch rathe raggedRhetonite, any whit, well graced. But fuch, as fovfeme, will finde a fowle Cracke in their Credite. Speake that you know : And know, as you ought: Know nor,by Heare Ey, when lite lieth in duunger. Search to the quicke, \& let Charitie be your guide-
CMatiriaus Ignorant, what Ahall fay to thee? Prohibe linguam tuan a malo. ©de-
 from flewmler. Though your tounges be fharpned, Serpent like, \& Adders poy fon lye in your lippes : yer takeheede, and thinke, betimes, with your felfe, Fir lin.
 Thus, 1 require you, my aflured frendes, and Countrey men (you Mathematiciens, Mechaniciens, and Philofophers, Charitable and difcrete) to deale in my
behalfe,

## IohnDee his Mathematicall Preface.

fpace, be robbed and fpoiled of his honcet name and fame? He that feketh (by S. aules aduertiement) in the Creatures Properties, and wonderfall vcrtues, to main, be (in hugger inugger) condemned, as a Companion of the Helhoundes, and a Caller, and Coniurer of wicked and damned Spirites; He that bewailcth his grear want of time, fufficient(to his contentation)for learning of Godly wildume and Godly Verities in : and oncly therin fetteth all his delight: Wiil that má leeff and abufe lis time, in dealing with the Chiffe enemice of Chrift our Redemer: the daddy foc ofall mankinde : the fubtile and impudent peruerter of Gouly Veritie the Hypoctiricall Crocodile ; the Enuious Bafilifke, continually defirous, in the twinke of an cye, to deftroy all Mankinde, both in Body and Soule, aternally Surcly(for my part,fomewhat to fay hercin) I haue not leamed to make fo brutih, and fo wicked a Bargaine. Should I, for ny xx.or xxv. yeares Studie : for tivo or three thoufand Markes fpending: feuen or cight thoufand Miles going and trauailing,oacly for good learninges lake: And that, in all maner of wethers: in all in:ner of wates and paffages : both carly and late $:$ in daunger of violence by man : in daunger of detruction by wilde beaftes: in hunger : int thirit: in perilous heates by day, with toyle on foote : in daungerous danpes of colde,by neght, almoft be reving lefle fecuitie And formure (thenall his) donc \& fifficd for Lear time toletle fecuntic. And for muchmore (dien all this) done \& uifed, for Leas normorewarily or (by Gods mercifelnes) numureluwily haue, large, and coftly, Netre, folorgtinc in drawing (and thar with the helpeand ad ufe of Lady Plulofophie, \& Queene Theologic) : bur ar length, to haue catched and drawen vp, * Frog? Nay, Deuill : For,fo, doth the Common peuifh Pratler Ioracine and lagile: And,fo, doth the Malicious fkomer,fecretly withe,\& braucly and botdly fice down,lehinde my backe. Ah, what a miterable thing, is this kind of Men : How great is the blindnes \& boldnes, of the Multitude, in thinges aboue their Capacine! What a Land : what a People: whatManers : what Times are thele \{ Are they become Deuils, them felues: and, by falfe witneffe bearing againf their Neighbour, would they alfo, become Murderers : Doth God,folong geue them refpire, to reclaime them felues in, from this horrible fluundering of the gits leffe : contrary to their owne Confciences : and yer will they not ceafe? Doth the Innocent,forbeare the calling of them, Iuridically to aunfivere him, according to the rigour of the Lases : and will they defpile his Charitable paciencee: As they, apainiी him, by nanse, do forge, fable, rage, and raife flaunder, by Worde \& Print: Will they prouoke him, by worde and Print, likewife, to Note their Names to the World : with their particular deuifes, fables, beaflly Inaginations, and vnchriften-
like flunders: Wcll : Well. like fluunders: Well: Well. O (you fuch) my vnkinde Countrey men, O vnnaturall Countrey men. O vnthankfull Countrcy men. O Branficke, Rafhe,
Spitefull, and Difdainfill Countrey men. Why opprefle you me, thus violently, Spitefull,and Difdainfull Countrey men. Why opprefle you me, thus violently, with your llaundering of me: Contrary to Veritie: and contrary to your owne Cone, ny way hurdull danageable, or iniurious wo youc, decde, or thought, hau bene, iny way, hurfull, daungeable, or iniurious to you, or yours ! Haue 1, fo long,
fodeariy, fo furre, fo carcfully, fo painfully, fo daungeroufly fought \& trauailed for fodeariy, fo furre, fo carcfully, lo painfully, fo daungeroufly fought \& trauailed for
the learning of Wifedome, \&atreyning of Vertuc: And in the end (in your iudgethe carning of Wifedome, $\alpha$ atteyning of Vertue : And in the end (in your iudge-
net) an I become, worfe, then when I begã? Worfe,thé a Mad man? A dangerous Member in the Common Wealth: and no Member of the Church of Chrilf?Call you this, to be Learned? Call you this, to bea Philofopher ? and a louer of Wite-dome? To forfake the ftraightheauenly way :and to wallow in the broad way of A.ij.

## Iohn Dee his Mathematicall Preface.

behalf, with the light \& vntrue tounged, my enuious Aduerfaries, or Fond frends. And farther, I would wiithe, that at leylor, you would confider, how Befiunes Mag. nus, layeth eriges and Danich, bcfore the cyes of thofe, which count all fuchStudies Philofophicall (as mine hath bene) to be vngodly, or vnprofitable. Waye
 or cat potess in verbis of apoibne fuis. Mo fes was instructed in all maner of wife dome of the Egyptians: and he was of power both in his roordes, and workes. Youfee this Philofophicall Power \& Wiledome, which UWe/er had, to be nothing milliked of the Holy Ghoft. Yet Plinjus hath recorded, Mofes to be a wicked Magto cien. And that(of force) mult be, either for this Philofophicall wifedome, learned, before his calling to the leading of the Children of 1 frael: or for thofe his wonders, wrought before King Pharas, after he had the conducting of the If raelifes. As concerning the firft, you perceaue, how S.Stephes, at his Martyrdome (being full of the Holy Ghoft) in his Recapitulation of the olde Teftament, hath made mention of Mofes Philofophic: with good liking of it: And Dafilises Magnms alfo, auoucheth it, to haue bene to Mofes profitable (and therefore, Ifay, to the Church of God, neceflary). But as cócerning Mofos wonders, done before King Pharae: God,
 Sec that thou do all thofe wonders before Pharao, which I haue put in thy hand. Thus, you euidently perceauc, how raflily, Plinins hath flaundered Mofor, of vayne Litb. 30 .

 fore, who, in Iudgement and Skill of Philofophie, are farre Inferior to Plinit, take ", good heede, leaft they ouerhoote them felaes rafhly, in Iudging of Pkilefophers ", firaunge Ades : and the Meanes, how they are done. But, much more, oughr they to beware of forging, deuifing, and imagining monftrous feates, and wonderfull workes, when and where, no luch were done : no, not any parke or likelinode, on fuch,as they, without allmame, doreport. And (to concinde) moft of all, let lintly or Maliciously tenife, and then deuilifhly to father theirnew fond Mon-
 God, or Man, in any my Studies or Exercifes, Philofophicall, or Mathematicall: As in due time, I hope, will be more manifeft.

Nowend I, with Archemaltrie. Which name, is not fo new, as this Arte is rare.For an other Arte, vnder this, a degree(for fill and power) hath bene indued with this Englith name before. And yet, this, maag ferue for our purpofe, fofficiently, at this prefent. This Arte, teacheth to bryng to actuall experience fenfible, all worthy conclufions by all the Artes Mathematicall purpofed, \& by crue Naturall Philofophie concluded: \& both addeth to them a farder fope, in the termes of the fame Artes, \& alfo byhys propre Method, and in peculier termes, procedeth, with helpe of the forelayd Artes, to the performance of complet Experiéces, which of no particular Art, are hable(Formally) to be challenged. If you remember, how we confidered Arclitedinure, in refpett of all common handworkes: fome lightmay you haus, therby, to vnderftand the Souerainry and propertie of this Science. Science I may callit, rather, then an Arte:for the excellency and Mafterflyyp it fiath, ouer fomany, and fo mighty Artes and
A.iij.
Sciences.

IohnDee his Mathematicall Praface.
Sciences. And bycaufe it procedeth by Experiences, and fearcheth forth the caufes of Conclufions, by Experiences: and alfo putteth the Conclufions them felues, in Experience, it is named of fome, Scientia Experimentalis, The Experimentall Science. Ntelaus Cufanus termeth it fo, in hys Experimentes Statikalf, And an other Philofopher, of this land Natiue (the floure of whofe worchy fame, can neuer dye nor wither) did write theroflargely, at the requeft of clement the fixt. The Arte carrieth with it, a wonderfull Credir: By realon, it certefieth, fenfibly, fully, and completely to the vtmoft power of Nature, and Arte. This Arte, certifieth by Exferitnce complete and abolute : and other Artes, with their Argumentes, and Demonfrations, perfuade: and in wordes, proue very well their Conclufions. * But Sciences practilable. And though fome Artes, haue in them, Experiences, yet they are not complete, and brought to the vttermoft, they may be ftretched vnto, and applyed feninbly. As for example:the Naturall Philofopher dilpleeth and maketh fome thynges in Experience bur neither, all, that they may:nor yet fufficiently, and to the vemolt, thofe, which they do, There, then, the Archemafter fteppeth in, ind leadeth forth on, the Experiences, by order of his doctrine Experimentall, to the chief and finall power of Naturall and Mathematicall Artes.Of two or three men, in whom,this Defcription of Archemaifry was Expcrimentally, verified, I haue read and hard:and good record, is of theirfuch perfection. So that, this Art, is no fancufticall Imagination: as fome Sophilter, mighr, Com fuis In ofiabilibus, make a florifh: and daffell your Imagination: and dath your honelt defire and Courage, from beleuing shefe thinges, fo vnheard of, fo meruaylous, \& of fuch Importance. Well: as you will. I haue forewarned you.I haue done the part of a frende: I haue difchatged my Duety toward God:for my fmall Talent, at hys mof mercyfull handes recciued. To this Science, doth the Science Alnirurgiat, greatSeruice. Mufe nothyng of this name. I chaunge not the name, fo vied, and in Print publifhed by other: beyng a name, propreto the Science. Vader this, commeth © Ars Sintrillia, by Artephius, briefly written. Bur the chief Science, of the Archematter, (in this world) as yet knowen, is an other (as it were) OPTICAL. Science: wherof, the name fhall be rold (God willyng) when I fhall haue fome, (more iuft) occafion, therof, to Difcourfe.
Here, I muft end, thus abruptly (Gentie frende, and vnfayned louer of honeft and neceffary verities.) For, they, who haue(for your fake, and vertues caufe) requefted me, (an old forworne Mathematicien) to take pen in hand: (through the confidence they repofed in iny long experience:and tryed fincerity) for the decla rving and reportyng fomewhat, of the frute and commodity, by the Artes Mathemaricall, to be atteyned vnto:enen they, Sore agaynif theit willes, are forced, for fundry caufes, to fatiffie the workemans requelt, in endyng forthwith: He , fo fearech this, fo new an attempt, \&\& fo coftly: And in matter forlenderly (hetherto 'anong the common Sorte of Studentes, confidered or eftemed.
And where I was willed, fomewhat to alledge, why, in our vulgare Speche, this part of the Principall Science of Geometrie, called Euclides Geometricall Elomentes, is publithed, to your handlyng : being vnlatined people, and not Vniuerfitie
Scholers: Verily, I thinkeirnedelefe. For, he Honour and Efinatio receaue all this Bencfite : how great focuer it be.

## Iohn Dee his Mathematicall Praface.

fightagainftryye owne fhadowe. For, no man ( $\operatorname{I}$ and furc) will open his mouth aganith his ionterprife, No má (I fay) who eithcr hath Charitie toward his brother (and woald be glad of this furcherance in yettuous knowledge) : or that hath any carc \& zeale for the bettening of tie Cumonifate of this leame. Nejthcrany, that utike accongt, what the wier fort of men (Sage and Srayed) do thenke of them, fo noice ( thetctors) will I make any Apelage, for a vertuous aste doing : and for comending, or futing forth, Profitable Artes, to Englith men, in the Englifh toung But, nute God our Crentor, let vs all be thankefull : for that, As he, of his Goodn nes, by bis Powre, and in his wifedome, batl, Created all tlynger, in Number, T3 Waight, and Mea/wre:So, to vs, of hys gicarMcrcy, be hath reucaled Meanes " whereby, to arteyne the fufficient aud neceffary knowledge of the forefiyd hys stree principall Initrumentes: Which Meanes, I haue abundantly proued voto " you, to be the Seriences and Sirtes ctaathomaticall.

And though I haue ben pinched with fenighmes of tymethat, no way, I could fo pen downe the marter(in my Mynde) as I derernined: hopyng of conuenien layfure: Yet, if vertuous zeale, and bonefIntent prouoke and bryng you to the readyngand eraminyng of dhes Comperidious treatie, 1 do not doute, but,as the ventic therot accorayng to our purpore) will be cuident noto you : So the pith and force therof, will perfaade you: and the wonderfall frute therof, highly plez fure you. And that you may the calier percciuc, and better remember, the prinThe Greand cipall pointes, whercoftiny Preface treatech, I will give you the Groundplate phen of inas of my whole difcourfe, ina Table annexed:from the firt to the laft, fomewhat Me
Table. $\quad$ IFHaff, hath caufed my poore pen, any where, wo flumble : You will, (I am fure) in part of recompence, (formy carneft and linceregood will ro plea(are you), Confider the rockinh huge mountaines, and the perilons vibeaten wayes, which (both night and day, for the while ) it hath royled and labored through, ro bryng you this good Newes, and Coinfortable profe, of Vertues frute. So, I Commityou vnto Gods Mercyfill direction, for the reft : hartely befechyng hym, to profper your Srudyes, and honeft Intentes:
whis Glory, \&e the Commodiry of our Countrey. Ames.

Wrisen at wo poore Hourge AI CIfortlafe.: Anno.l 57 e. Fctrivary.g.
[Henry Billingsley's note to the reader]
f $\boldsymbol{\sim}$ The Tranflator to the Reader.


Herc is (gentle Reader) nothing (the word of God onely fet apart) which fo much beautifieth and adorneththe foule and minde of mă, as dotb the knowledge of good artes and fiences: as the prowledge of naturall and morall Ph lofopbie. The one fetteth before our eyes, the creatures of $\mathcal{G}$ od, both in the beauens aboue, and in the carth beneath: in whbich as in $\llcorner$ gla $\beta e$, we beholde the exceding maieftie and wifedome of God, in adorning and beaurifying them as we fee : ingeuing onto them fuch woonderffull and manifolde proprieties, and naturall workinges, and that fodiuerfly and in fucbsarietie: farther in maintaining and conferuing them continually, whereby to praife and adorc bim, as by S.Paule we are taught. The other teacheth vs rules and preceptes of vertue, hom, in common life a.mongeft men-, we ought to walke uprightly : what dueties pertaine to our (elues, whatpertaine to the gouernment or good orderboth of an boubbolde, and alfo of a citie or common wealth. The reading likerwif o of hiftories, conduceth not a litle, to the adorning of the foule co minde of man, aftudie of all men commended: by it are feene and knowen the artes and doinges of infinite wife men gone before vs. In biftories are contained infinite examples of heroicall vertues to be of is followed, and horrible examples of vices to be ofys efchewed. Many other artes alfo there are which beautifie the minde of man: but of all otber none domore garni/be co beautifie it, then thofe artes which are cal. led Mathematicall. Unto the knowledge of whichno man can attaine, without the per ecte knowledge and imftruction of the principles, groundes, ana Elementes ofGeometrie . But per6. fectly

## suThe Tranflater to the Reader.

well perceaue. The fruite and gaine which I require for thefe my paines and trauaile, fall be notbing els, but onely that thou gentle reader, will gratefully accept the fame : and that thou mayeft thereby receaue fome profite:and moreouer to excite and ftirre up otbers learned, to do the like, \&o to takepaines in that behalfe. By meanes wherof, our Englifhe tounge f hall no leffe be enriched with good Authors, then are otberftraunge tounges: as the Dutch, French, ftalian, and Spani/be : in wbich are red all good authors in a maner, found amongeft the Grekes or Latines. Wbich is the chiefeft caufe, that amongeft théd doflorijhe fo many cunning and kilfull men, in the inuentions of ftraunge and wonderfull thinges, as in thefe our daies we /ee there do. Which fruite and gaine if Iattaine vnto, it /hall encourage me bereafter, in fuch like
fort to tranflate, and fet abroad fome other
good autbors, botbpertaining to religion
(as partly I baue already done) and
alfo pertaining to the ©Mathematicall Artes. Tbus gentle readerfarewell. (? $?_{i} \quad \boldsymbol{\sigma}^{i j}$


## sw The Tranflator to the Reader.

fectly to be infltucted in them, requireth diligent fludie and reading of olde auncient autbors. Amongeft which, none for a beginner is to bepreferred before the moft auncient Pbilofopher Euclide of Megara. For of all others be bath in a true methode and iufe order, gathered together what Jever any before bim bad of thefe Elementes written: inuenting alfo and adding many thinges of his owne: wherby be hath in due forme accomplifhed the arte.firft geuing definitions,principles, wr groundes, wherof be deducetb bis Propofitions or conclufions, in fuch wonderfull wife, that that which goeth before, is of neceßßitie required to the proufe of that which followeth. So that without the diligent ftudie of Euclides Elementes, $i t$ is impoßible to attaine vnto the perfelite knowledge of Geometrie, and confequently of any of the other Matbematicall ciences. Wherefore con/idering the want \& lacke of Juch good autbor's hitberto in our Englifhe tounge, lamenting alfotbe negligence, and lacke of zeale to their countrey in tho fe of our nation, to whom God bath geuen both knowledge, \& alfo abilitie to tranflate into our tounge, and to publifhe abroad juch good autbors, and bookes (the chiefe inftrumentes of all learninges ): Feing moreouer that many good wittes both of gentlemen and ofothers of all degrees, much defirous and ftudious of the fe artes, and feeking for them as much as they can, /paring no paines, and yet fruftrate of their intent, by no meanes attaining to that which they feeke: I haue for their Jakes, with fome charge do great trauaile, faithfully tranflated into our vulgare toüge, 心 fet abroad in Print, this booke of Euclide. Whereunto I baue added eafie and plaine declarations and examples by figures, of the definitions. In which booke alfo ye /ball in due place finde manifolde additions, Scholies, Annotations, and Inuentions:which Ibaue gathered out of many of the moff famous or chiefe Mathematiciès, both of old time,and in our age: as by diligent reading it in courfe, ye fhall

[Introduction and Definitions written by John Dee]

## - The firlt booke of Eu- <br> clides Elementes.



NTHISFIEST-BOOKEis intreated of the moft fimple, eafie, and firft matters and groundes of $G e o-$ meiry, as, namely, of Lynes, Angles, Triangles, Paralle iss, Squares, and Parallelogrammes. Firft of theyr definitions, hewyng what they are. After that it teas ehecth how to draw Parallel lynes, and how tofarme diverfly figures of three fides, \& foure fides, according to the varietie of their fides, and Angles: \& cópatetir them all with Triangles, \& alfo together the onc with the other. In italfo is taught how a figure of any forme may be chaunged into a Figure of an other forme. And for that it entreateth of thefe moft common and generall thynges, thys booke is more vniuerfall then is the feconde, third, or any other, and therefore iuftly occupieth the firtt place in order : as that without which, the other bookes of Euclide which follow, and alfo the workes of others which haue written in Geometry, cannot be perceaued nor vaderftanded. And forafinuch as all the demonftrations and proofes of all the propofitions in this whole booke, depende of thefe groundes and principles following, which by reafon of their playnnes neede no greate deciaration, yet to remoue all (be it neuer fo litle) obfcuritie, there are here fet certayne fhorte and manifeft expofitions of them.

## $\$ 2$ Definitions.

## 1. Afigne or point is that, vibich bath no pare.

The better to vider ftand what manerofthing a figne or point is, ye muft note that the nature and propertie of quantitie (wherof Geometry entreateth) is to be deuided, fo that whatfoeuer may be deuided into fundry partes, is called quantitie. But a point, although it pertayne to quantitie, and hath his beyng in quantitie, yet is it no quantitie, for that it cannot be deuided. Becaufe (as the definition faith) it hath no partesinto which it fhould be deuided. So that a pointe is the leaft thing that by minde.and vnderftanding can be imagined and conceyued : then which, there can be nothing leffe, \#s the point $A$ in the margent.

[^4]Definitian of apoyntaften Pichagoras.

## The first Poke

so thee three dimensions, three kyndes of continual quantities : a lyme, a fuperficies, or paine, and a body. The firft kynde, namely, a line is here defined in the fe wordes, ed lye is length without breadth. A point, for that it is no quantitie nor hath any pates into which it may be decided, but remaineth indiuifible, hath not, nor can have any of there three dimenfions. It neither hath length, breadth, nor thickenes. But to a line, which is the firft kynde of quantitie, is attributed the firf dimenfion, namely, length, and onely that, for it hath neither breadth nor thicknes, but is conceaued to be drawne in length onely, and by it, it may be deuided into partes as many as ye lift, equall, or vnequall.But as touching breadth it remaineth indiuifible. As the lyme AB, which is onely drawn in length, may bedeuidedin the point $C$ equally, or in the point $D$ unequally, and fo into as many partes as ye lift. There are alpo of diners other geuen other definitions of a lyme: as | $A$ | $\vec{C} \vec{D} \quad \vec{B}$ |
| :--- | :--- | :--- | thee which follow.

An offer deftnotion of a line. An otter.

The codes of $A$ lime.

A tyne is the mouyng of a poynte, as the motion or draught of a pine or a penne to your fence maketh a lyme.

Agayne, of lyme is a magnitude hating one onely pace or dimension, namely, length wanting breadthandthicines.

## 3 The endes or limites of a lone, are points.

For a line hath his beginning from a point, and likewife endeth in a point: fo that by this alpo it is manifeft, that pointer, for their fimplicitie and latke of compofition, are neither quantities, nor partes of quantities, but only the termes and andes of quantities. As the pointes $A, B$, are onely the andes of the line $A B$, and no pates thereof. And herein differeth a poynte in quantitie, from vnitie in number: for that although vnitie be the beginning of nombers, and no number( as a point is the beginning of quantities, and no quantitie) yet is vnitie a part of number. For number is nothyng els but a collection of vanities, and therfore may be deuided into them, as into his partes. But point is no part of quantitie,or of a lyme: neither is a lyme compofed of pointes,as number is of vanities. For things indiuifible being never fo many added together, can never make a thing diuifible, as an infant in time, is neither tyme, nor part of tyme, but only the beginning and end of time, and couplet \& ioyneth partes of lyme together.

## 4 A right tyne is that which teth equally betivene bis points.

As the whole line $\mathcal{A} B$ lyeth ftraight and equally betwene the poyntes $A B$ without any going vp or comming downe on eyther fide.

Campanus and certain others, define a right line thus: A B
A right line is the Shortest extenfion or draught, that is or may
be from one point to an other. Archimedes defineth it thus.
Aright line is the fhortes7 of all lines, wb which base one and the faff fanse limsites or endes: which is in manner al one with the definition of Campanus. As of all there lines $A B C, A D C, A E C$, $A F C$, which are all drawee from the point $A$, to the poynte $B$, as Campanns fpeaketh, or which have the Self fame limites or andes, as Archimedes Speaketh,the lyme $A B C$, beyng a right line, is the fhorteft.
Plato defineth a right line after this meaner: Aright
Definition thereof after Plato. Campinas. Definition thereof after Archimodes.
Definition of *right line.line is that whole middle part §hadoweth the extremes. As if you put any thyng in the middle of a right tyne, you fall not fee from the one ende to the other, which thyng happeneth not in a crooked lyme. The Ecclipfe of the Sane( $\sqrt{2} 2$ Aftronomers) then happeneth, when the Sane, the Moose, \& our eye are in one right line. For the Moose then being in the midft betwene vs and the Sunne, caufeth it to bedarkened.Diuers other define a right line diuerfly, as followeth.

A night lye is that which fandeth forme betwene his extremes.
Agayne, Aright line is that which with an other line of lye forme cannot make a figure.

## of Euclides Elementes.

Agaync, A right lyne is that which hath not one part in aplaine fuperficies, andan other ereited anorher. on bight.
Agayne, A right lyne is that, all whofe partes agree together with all bis other partes.
Agayne, Aright lyne is that, whofe extremses abiding, cannot be altered.
Enclide doth not here define a crooked lyne,for it neded not.It may cafely be vnderftand by the definition of a right lyne, for euery contrary is well manifefted \& fee forth by hys contrary. One crooked lyne nay be more crooked then an other, and from one poynt to an other may be drawen infinite crooked lynes: but one right lyne cannot be righter then an other, and therfore from one point to an other, there may be drawen but oneright lyne. As by the figure aboue fet, you may fee.

## 5 AJuperficies is that, which bath onely length and breadth.

Dffinition of 4 Superficies.
A fiperficies is the fecond kinde of quantitie, and to it are attributed two dimenfions, namely length, and breadth. As in the fuperficies $\mathcal{A} B C D$. whofelength is taken by the lyne $A B$, or $C D$, and breadth by the lyne $A C$. or $\mathcal{B} D$ : and by reafon of thofe two dimenfions a fuperficies may be deuided two wayes, namely by his length, and by hys breadth, but not by thickneffe, for it hath none. For, that is attributed onely to a body, which is the third kynde of quantitie, and hath all three dimenfions, length, breadth, and thicknes, and may be de-
 uided according to any of them.

Others definea fupeif ficies thus: A fuperficies is the terme or ende of a body. As a line is the ende and terme of a fuperficies.

## 6 Extremes of afuperficies, are lynes.

As the endes, limites, or borders of alyne, are pointes, inclofing the line:fo are lines the limites, borders, and endes inclofing a fuperficies. As in the figure aforefayde you maye fee the fuperficies inclofed with foure lynes. The extremes or limites of a bodye, are fuperficiefles. And therfore a fuperficies is of fome thus defined: $A$ fuperficies is that, Which endeth or inclofet b body: as is to be fene in the fides of a die, or of any other body.

## 7 A plaine fuperficies is tbat ${ }_{2}$ vobich liethequally betwene bis lines.

As tinefuperficies $A B C D$ Iyeth equally and finoothe betwene the two lines $A B$, and $C D$ : or betwene the two lines $A C$, and E $\cdot D$ : fo that:no part therof eyther firelleth vpward, or is depreffed downward.And this defnitió much agreeth with the definition of a right line. A right line licth equally betwene his points,
 and a plaine fuperficies lyeth equally betwene his lynes. Others define a plaine fuperficiesafter this maner:
A. plaine fuperficies, is the 乃hortest extenfion or drakght from one lyne to an ot her : like as a right lyne is the fhorteft extenfion or draught from one point to an other.
Euclide alfo leaueth out here to fpeake of a crooked and hollow fuperficies, becaufe it may eafely be vaderftand by the diffinition of a plaine fuperficies, being hys contrary. And euen as from one point to an other may be drawen infinite crooked lines, \& but one right line, which is the fhorteft: fo from one lyne to an other may be drawen infinite croked fuperficiefles, $\&$ but one plain fuperficies, which is the thorteft. Here muft you confider when there is in Geometry mention madeof pointes, lines, circles, triangles,or of any other figures,ye may not conceyue of them as they be in matter, as in woode, in mettall, in paper, or in any fuch lyke, for fo is there no lyne, bur hath fome breadth, and may be deuided: nor points, but that fhat haue fome partes, and may alfo be dcuided, and fo of others, But you muft conceiue them in mynde, plucking them by imagination from all matter, fo fhall ye vndertande them truely and perfcetly, in their owne nature as they are defined. As a lyne to be long, and not broade: and a poynte to I. ij.
be
["Brief Treatise" by Flussas annexed at the end of Book 16]

## Flußas, of mixt and

50 A briefe treatife, added by Fhiffas, of mixt and
compofedregular folides.


Egular folides are fayd to be compofed and mixt, when ech of them is tranfformed into other folides, keeping ftill the forme, number, and inclination of the bafes, which they
before hadone to theother: fome of which yet are tranfformed into mixt folides, and other fome into fimple. Into mixt, as a Dodecahedron and an Icofahedron : which are tranfformed or altered, if ye diuide their fides into two equall partes, and take away the folide angles fubtended of plaine fuperficiall figures made by the lines coupling thofe middle fections \& for the folide remayning after the taking away of thote folide an ${ }^{3}$ gies, is called an icolidodecahedron. If ye durde the endes of a cubc and of an tended of the plaine fuperficieces made by the coupling lines, being raken away, there iball be left a folide, which is called an Exoitohedron. So that both of a Doan Icofidodecshedron: and likewife the folide enade of a Cube \& alfo óf añoctohedron, (hall be called an Exoctohedron. But theother folide, namely, a Pyranis (or Tetrihedron) is rranfformedinto a fimple folide : for if ye dimide into two equall partes euery one of the fides of the pyramis, triagles defcribed of the lines which couple the fections; and fubtending, and talang away folide angles of the pyranis, are equall and like ynto the equilater triangles left in cuery one of the bales af ofll which triangles is produced an Oathedron, namely, a fimple and not accompofed folide. For the OCtohedron hath fower bafes, like in number, forme, and mutuatl inclination with the bafes of the pyramis: and basth the other fower bales with like fituation oppofice and paralle to the former. Wherefore the application of the pyramis takea twife, maketh a limple Ottohedron, as the orher fopides make a mixt compound folide.

$$
\Phi \text { Firjt Definition. }
$$

Th Exotiobedron is a folide figure contarined of fixe equallfquares, and eigbt equilater and equall triangles.

1Second Definition.
An Icofidodecabedron is a folide figure, contained onder twelue equi. later equall and equiangle Pentagons, and twentir equall and equilater triangles.

For the better vnderfanding of the two former definitions, and alfo of the two Propofitions following, I haue here fet two figures, whofe formes, if ye firt

## Flupas, of mixt and

in the bafes of the cube, be fquates: and they fhall be fixe in number, aceørding to the núber of tie bales of thecubes. $K$ IN fubstendeth the folide angle D of the cube, and likewife the triangle K G L the folide angle C, \& Go the reft which fubrend the eight folide angles of the cube: and thefe triangles are equall and equilater, namely, being made of equall fides \& they are the limmits orborders of the fquares, and the fquares the limmits or borders of thé, as hath before bene proued: wherefore L MNOPHGK is an exoctohedró, by the diffinition, and is equilater, for it is contayned of equall fubtendent linessit is alfo equiangle,
 for euery folide angle thereof, is contayned vnder two fuperficiall angles of two fquares, and two fuperficiall anles of two equilater triangles
Andnow forafmuchas the oppofite fides and dimeters of the bafes of the allelogramme. And for that alfo in that playnelyeth QR the diameter of the cub¢, and in the fame plaync alfo is the line MH, which diuideth the fayd playne into two equall parts, and alfo coupleth the oppofite angles of the exoctohedron his line MH therefore diuideth the dameter into two equall partes, by the cocollary of the 34 .of the firf, and alfo diuideth it felfe in the fame poynt, which let beS, into two equall partes, by che 4 of the firf. And by the fame reafon may we proue that the reft of the lines, which couple the oppofite angles of the exoctohedron, doo inS the centre of the cube divide the one the other into two equall parts. For enery one of the angles of che exoctofiedron are fet in euery one of the afles of the cube. Wherefore making the centre the poynt S, and the fpace SH or S M; deferibe a fphere, andit fhall touch cuery onc of the angles equediftant from thepoynts,

And forammuth as $A B$ the diameter of the fphere geuen, is put equall to the equall to the line M H , by the 33 . of the firt: which line M H coupling the oppofite angles of the exottohedron is drawne by the centre: wherefore it is the diameter of the fphere geuen which contayneth the exoetohedron.

Finally forafinuch as in the triangle R F T, the line P O doth cutte the fides into two equall partes, it thall curte them proportionally, with the bafes, namely, as Pby fiopofition: whercfore $\mathrm{R} T$, orme diameter H M , is alfo double to the line PO thefide of the exoctohedron. Wherefore we hauedefcribed an equilater \&equiangle exottohedron, and comprehẹnded it in a fphere geuen,and haue proued that the dismeter of the fphere is double to the fide of the exoctohedron.
compofedregular folides, Fol.459.
defrilieypon pafted paper or fuch like matter, and then cut them and folde them accordingly, they will reprefent vnto you the perfets formes of an Exoctohedron and of an Icofidodecahedron.


The first Probleme.
Todefribe ar equilater and equiangle exoctobedron, and to contayne it in a phere geven:and to prone that the diameter of the phere is double to the fide of the fayd exoctobedron.

W9. 1 Wh ppofe that there be a phere geuen, whofe diameter let be A B. And the fourthand vpon the f quare let there be defcribed a cube by the 15 . Nenas of the thirtenth: which let be CDEF QTVR: and let the diameter dates. in the poyntes G;H,I,K, $\mathrm{L}, \mathrm{M}, \mathrm{N}, \mathrm{O}, \mathrm{P}$. by theright lines IN,NO,O P,PI and fuch like, which fubrend the angles of the fquares brbafes of the cube: and they are equall by the 4 , firt, and contalne right angres,ris the angle N IP. For the angle NID which is at the bafe of the Iforcele triangle ND I, is the halfe of a right angle, and folikewie is theopporite angleR IP. Wherefore the refidue N I P is a right angle, and fo the reft. Wherefore N IP O is a fquare.And by the fame reafon fhall the eft N M L K, K GHI \&c.juifcribed DDD.ij. 4
compofed regular folides.
Fol. 460.

## ITbe' 2. Probleme.

Todefribe an equilater © equiangle Icofidodecabedron, \& to coprebend it in afphere genen:and to proue that the diameter being dinided by an extreame and meane proportion, maketh the greater fegment dowble to the fide of the Fofidodecaluedron.


## Flußas of mixtand

Now let vs proue that it is contained in the $S_{\text {phere }}$ geuen, whofe diameter is That tbe Tow NL. Forafmuch as perpendiculars drawen'fío the centres of the Dodecahedron,
 geses.

 the one the other intotwoequall partes: thereforeright lines diritwen from that point to the angles of the Icofidodeachedron (which are fet ind dhofé midle fections ) are equall: which lines are 30 . in number according to the nurnber of the fides of the Dodecahedronasfonetery: one 0 ethe angles of the IEcofidodecahedron are ferin the midle festions sofecuery one of deefides of che Dodecahedron:Wher-Core makugg zhesentro wecentse of the Dodecaliedron, and the pace any one of
the lines drawen from the esenrec to the midle fettions, defcribe al Sphere, and it thall parfe by all the angles of the Icofidodecahedron, and fhall containe it:
And forafinuch as the diamerer of this folide, is that rightline, whofe greaterfegment is the fide ofthe cube infcribed in the Dodecahedron, by the'4. Corollary of the 17 . of the thirtenth, whicande is N1,by dipports. whe to be the line NL
Thatebectis-
prterbeverg dexilidity an extrone and mesuepropo
tion.Es. Now let vs prouc that the greater fegment of the diameter is duple to QV the fide of this folide. Forafmuch as the fides of the triangle A EB are in the pointes $Q$ and $V$ diuided moo two equall partes, the lines QY and BEarepa. rallels, by the Corollary of the 39. of the firf. Wherefore is AE is to AV, fo is EB to VQ, by the 2 . of the fixth.
But the line AE is doubleto But the line AE is doubleto
thetine AV :-Whereforethe line $B E$ is deuble to the line QV: bysthe, 4 of the fixth. Now the diacBE is equallto Nf, onto thefide of the cube, by the 2. Corollary of the 17 :
 of she thitenth, which-line
$\mathrm{NI} I$ is the gieater egment of diameter NE . Wherefore the greater fegment NI is the greater fegment of the dimeter N E: Wherefore the greater fegment
of that diameter geuen, is double tot the fide of the I cofidodecahedron inferibed in the Sphere geuen, Whereforewe haue defcribed an equilater and equiangle IcoGdodsçhedron, and contained it in a Sphere geuen; and haue proued that the diamerer thereof being diuided by an extrene and meane proportion, maketh hys greates fggensp double to the fide of the Icofidodecahedron.

> IT Anduduertifment of Flugfas.

Tonthemdertanding of the nature of this Icofidodecahedron, yemult well gonceaue thepaffons and proprieties of both thofe folides, of whofe bafes itconifteth, mapelv, of he İcof haedron and of the Dodecahedron. And although in it
compofed regular foldes. $\mathrm{Fol}_{4}$ бr. the bafes are placed oppofitely, yet bane cticy one to the oukerone \&idhe fathe int. clination. By realon wherof therelie hiddeninit the zotions and pubtions of flie other regular folides. And $\%$ weuld haue thoughtitnotimperanent to the purpofe to haue fet forth the infcriptions and circumsctiptions of this folide jif want of time had not hindred. Bur to the end the reader may the better artaine to the vnderftanding therof, I haue here following briefly fetforth, how it may in or aboute uery one of the: fiue regular folides be inferibed or dracumferibed: by the helpe
 fed and coufidteced the deinonftratiois pertaynuing to the fortelayd fiue regular fo-
lides, demonftrate both the infctiption of the fayd folides in it, and the inffription Lides, demonftrate both
of it in the fayd \{olides.

## - Of the infcriptions and circuimfcriptions of

 an Icofidodecahiedron.An Icofidodecahedron may containe the otherfueregular bodyes. For it will receaue the angles of a Dodecabedron, in the centres of the triangles which fubtend the folide angles of the Dodecahedron: which folide angles are 20 .in néber,and are placed in the fame ordef in whichthe folide angles of the Dodecahedron taken away or fubtended by themi, are. And by that reafon it fhall receauca Cube and a Pyranis concayned inche Dodecahedron: when as the angles of the one arefer in the angles of the othef.

An Icolrdödecathedron receadeth an OCtohedron, in the angles cutting the fixe oppotite fections of the Dodecathedron, euen as if it were a fimple Doderon.
Anditcontaineth an Icofahedron, placing the 12 -angles of the Icofahedron in whe elfe fante céntres of the ri. Péntagons.
Itmay alo 0 by the farue reatortbeinicribed in euery one of the fine regular bo dies : hamety pida Pyiazinis, if ye place 4 .triangular bafesconcentricall with 4 .bafe of likewife may it bine ame maner, that ye micribed an icofahcorosin 2 Pyramis, centricall with the $8 . \mathrm{b} \sqrt{ }$ fes of the O a hedron if ye place the angles which receaue the Oetohedroninfcribed in it, in the centres
 of the bales of the Cube. Moreouer, ye lhallincribeit man ancoahedran, when
the triatigles compafed if of the Pentagon Eafes, sare concentricall with the triamgles, whicturuake folide angle of the Icofabearoñ. Finally, ic fhall be inceribed in a Dodecahedron, ifye place euery one of the angles thereof in the midle fections of the fides of the Dodecahedron, according to the order of the conftruction thereof.

The oppofite plaine fuperficieces alfo of this folide are parallels. For the oppofite folide angles are fubtended of parallel plaine fuperficieces, as well in the angles of the Dodecahedron fubtended by tiiangles, as in the angles of the foofahear of it is compofed.

Whereforeit is manifeft thata Dodecahedron \&an Icoohedron, mixed, are
uranformed

## Flapaus, of mixatand


 feqfolidesamely into an OCtohedton.
If wewill baxe thefeswo folides ioyned rogether into one-Solide this onely mult weebferuce:
In the pentagon of a dodecahedrominferibed ilike pentagon,föthat let the angles of the paricion infcribed befer in the midele fections of the fides of the pen-

 ypon thefe peatagons fhall produce a folideconfifting of the whole Dodecahe dron, and of the whole Icofahedron. In like fort, if in euery bafe of the Icofahedró, the fidespcing douided iuta twg qquill pates boinfaribed an equilater triangte and vponcuccy one of thotec cquatater riangles le eera folide angle ofz Dodeca hedron: there flall be produced the fole faine folite confilting of the whote tcofohedron, \& of the whole Dodecabedron.

Andaret the fime order, if in the bules of ficabe be ijfccibed diviates fubtey-

 andof the whole Oetohcdron.
 fet in the midle fections of the fides of the pytanis and the folide anges of apyra-
 Andnow if in thefefolides thus
 taken away from a D odecahedron and an 1 ied fatcedron : nampy, the folice angles fhalbe left an Icofidodecahedron:the folide angles takē away from 2 cubc and an

 belfatinoctotitifon
 ple erguar bodis: whic aithouggrie demonifrateth hot yetare they not hard to bedemonftizted, we welpeafe and conceite that, wifinin the formicr bookes hath betre tang hirrouchngig thofe folides.

## O fthe nature of a trilater and equilater Pyramis.

A rrilater equilater Pyramis,js decided into two equaf paites; by threecqual Iquares, which ing the centre of the pyrmais cuite the one the othor into two eq al partes, andperpendiculatly, and winafe angles are fer in che midleff̈ctions of the whole, whech.vuterly take away thesides of the fyranis, and that which is left
compofad regular Falide's. Fol.462. is an ofohedró infcribed in the pyranys m whichall the folides inforibed in the pyramis are contained. A perpendicular drawne from the angle of be pyramis
to the bafe, is double to the diameter of the cube infribed in it. And a coupling the mide fections of the oppofirefides of the pyramis is minleto hat linc coupling ue midecretions of the oppoite indes or the pyramis, is ciple to the fide bafe of the cube. Wherefore the fame fide of the pyramis is in power duple 20 the right line which coupleth the midle fections of the oppofire fides. And it in power fequialter to the perpendicuar whach is drawne from the angle to the bale. Wherefore the peppendicular is in powcr fefquitertiz to the line which cow ple th the midle foctions of the oppofite fides. A pyramis, and an O aohedronier fetribed in it,alfo an Icolfahedron infcribed in the tame OQchedron, doo sonsains
oneand the felfe (ame folicre.

Of the nature of an Octohedron.
Fotacperpendicalars of an OAtohedrop, drawne in 4 .bafes theroffrom rwo oppofitte angles of the faid Oftohedron, and coopled together by thofeq 4 bres ple to the other diameter. For it hathethe fame proporio thay thic diameter of the OAtohedron, hath to the fide of the $O$ Atohedror. An Octobiedron \& in Icofthedroin inferibed in it, do containe one and the felfe fame fphere. The diameter of the \{olide of the Octobedton, is in power fCfquailter to the diameter of the circde which containeth the bafe:and is in power triple ro the right line which coapleth
the cetres of the oppofite bafes:and is in power*duplefuperbipaticns tercias to
 the perpedizular or fide of the forefaid Rhombus: and moreoucr is in legth uiple to
to the line which coupleth the ceates of the next bafes. The angke of the inclnation of the bales of the Ocrohedron, doth with the angle of the inclination of the bafes of the pyramis, make abgles equalio wo right angles.

## Of the nature of a Cube.

The diameter of a cubeisin power fefquialterto the diameter of his bafe and is in power tuple to his fide : and vnto the line which coupleth the centers of the next bafessit is in powerfeeruple. Moreouer the fide of dhe cube is to the fidc of the Icofahedron inicribed init as the whole is to the ercase fegment : vnio
the fide of the Dodecahedron, it is as the whole is to the leffegment: vnto the fide of the OAohedron, it is in power duple: and vnto the fide of the pyramis, it is in power fubduple. Moreoner the culbe is triple to the pyramis : but to the cube the Dodecahiedron is in a maner duple. Whetfore the fame Dodecelhedron is in a mancriextuple to the fayd pyramis.

## Of the nature of an Icofahedron.

Fiuetriangles of an Icefahichron, do makea folide angle, the befes of shist tiangles inake apentagon. If theffore from the oppofire bales of the Licofihadr


Imprinted at London by Iohn Daye.

## Notes on this Modernization

On the facing page is a modernization of Dee's "Groundplat," which serves as a comprehensive index to all the things he discusses in the Preface. You'll see words you never knew existed. That's because Dee coined many of them (and they never really caught on).

Why bother translating an English book into English? One reafon is fimple. Few folks feel like wading through a fwamp ftrewn with s's that look like f's. Second, for cost considerations, Elizabethan typesetters filled the pages chockablock with words. The text has been graphically lightened by adding much-needed breathing room.

For the sake of clarity, I have made other alterations. Chapter headings have been added that correspond with the Groundplat. Sentences have been shortened and rearranged. Words whose main definitions have morphed during the past centuries have been changed. Some spellings has been modernized (like Zography for Zographie). I have eliminated much of Dee's ubiquituous italicizing, but I have kept his emphatic capitalzations.

Some might feel that Dee's words should not be changed at all, much as Shakespeare's original words are often held sacrosanct. (To modernize or not to modernize, that is the question.)

To those traditionalists, and indeed to everyone, I recommend you plod through at least parts of Dee's Elizabethan English. I'll admit that certain subtle word meanings and alliterative phrases have been lost in my translation. But too me, it's better that this priceless antique is dusted off, polished up, and brought to light rather than let it remain in its original condition in a dark corner of the attic of history.

Dee's Preface provides an interesting overview of the main branches of science, but its real value is that it contains hidden clues that help unravel the puzzle of the Monas Hieroglyphica, as well as design of the John Dee Tower.

## Jim Egan <br> (2010)

## J. DEE

Here you have (as promised) the Groundplat of my Mathematical Preface annexed to Euclid's Elements of Geometry published for the first time in our English tongue.

In the Year1570, February 3.


[^5]fe TO THE GENUINE LOVERS
of truth and diligent Students of the Noble Sciences,
JOHN DEE, of London, heartily wishes grace from heaven, and most prosperous success in all their honest attempts and exercises.


Ivine Plato, the great Master of many worthy Philosophers and the constant avoucher and pithy persuader of Unum, Bonum, and Ens [Truth, Goodness, and Beauty] in his School and Academy, was visited occasionally by certain kind of men (besides his ordinary scholars), allured by the noble fame of Plato, and the great commendation of his profound and profitable doctrine.

But such Hearers, after long harkening to him, perceived from the drift of his discourses that Unum, Bonem, and Ens was Spiritual, Infinite, Eternal, and Omnipotent. When they realized that nothing was being alleged or expressed about
worldly goods, worldly dignity, health, strength, lustiness of body, nor anything about the way to attain marvelous bodily bliss and happiness for the senses, immediately their fantasies were dampened. Their opinion of Plato was completely changed. Indeed, they came to look down scornfully on his doctrine and left his school, never to return.

Plato's student, Aristotle, felt the cause of this was that they had no forewarning or information $\quad \sim$ about the general direction of his doctrine. Being aware of the scope of Plato's intentions beforehand, they could have better decided whether to stay away from the school or to study there to their full satisfaction. Thus, Aristotle learned to explain beforehand what he was going to speak about and the extent to which he would cover the subject.

As I think about the diverse styles of these two excellent Philosophers (though both certainly were a great teachers, and they often spoke without prefacing their teaching), I am in no little pang of perplexity. It would be easier for me to simply not write a Preface at all (using Plato as my example). Writing a Preface is more commendable and even essential (to introduce the Mathematical Arts into common use), but it is full of great difficulty and sundry dangers. Starting unceremoniously without an introduction would not be appropriate in presenting such unfamiliar matters to an audience so unacquainted with the subject.

I trust (now imitating Aristotle) that I can do justice to the full breadth and dignity of the Mathematical State by clearly prescribing its range, and precisely expressing its chief purposes and most wonderful applications.

I am certain that those diligent students, who listen to Plato all the way through his final conclusion, had their desires so infinitely fulfilled. Likewise, those who read my Preface introducing the Mathematical Arts will be greatly satisfied.

The quicker the Pythagorical, and Platonical perfect scholar and the determined, profound Philosopher is allured to this work, the sooner and faster he will (like the Bee) gather both wax and honey.

Thus, I consider it a great occasion (for the reasons just mentioned and also with respect to the

The general Mathematical Art), to use a certain forewarning and Preface, whose content shall be that mighty, most pleasant and fruitful Mathematical Tree, with its chief arms and second (grafted) branches. I will both explain and show the usefulness of these arms and branches. This enterprise is so great that (in these days) it has never accomplished by any one else (to my knowledge). Also, it is quite difficult, in these our dreary days, for such rare and strange Arts to gain the respect to which they are entitled.

In exchange for my sincere endeavor to satisfy your honest expectations, all you have to do is lend me your thankful mind for a while. I will be as succinct as my speedy pen will allow. Apply your eye or ear attentively. Perhaps after reading the Preface you will find the lesson long enough. But more likely you will be hooked by the lion's claw and, being much more well-informed, make your own conjectures about its royal symmetries and other properties. Now, my gentle friends and countrymen, turn your eyes and bend your minds to that doctrine, which, for our present purpose, my simple talent is able to provide.

## [three kinds of things in the Universe: Supernatural, Natural, and Mathematical]

There are three generals categories of all things which have being: Supernatural, Natural, and a third kind. Supernatural Things are immaterial, simple, indivisible, incorruptible, and unchangeable. Supernatural Things can only comprehended by the mind. Natural things are able to be perceived by the senses.

Natural things can involve probability and conjecture, but Supernatural things are the chief demonstration of a most absolute science. By comparing the properties of the two types, we can better describe the state, the condition, the nature and the property of the third thing I mentioned.

This third type is given a special name: Mathematical things. They are (in a manner of speaking) in the middle between Supernatural and Natural things. They are not as absolute and excellent as Supernatural things, but not as base and gross as Natural things. They are immaterial but, nevertheless, are they somewhat able to be signified by material things.

And though their particular Images are aggregable and divisible by art, their general Forms are always constant, unchangeable, untransformable, and incorruptible. They cannot, at any time, be perceived or judged by the senses, but they also can't be considered to have been first conceived in the royal minds of Man. Above the imperfection of conjecture, supposing, and opinion, yet just below high intellectual conceptualizing, are the Mercurial fruits of Dianetical discourse [the use of Reasoning], which exist in perfect imagination.

These Mathematical things have a marvelous neutrality, yet they also have a strange participation between Supernatural, immortal, intellectual, simple, indivisible things and Natural, mortal, sensible, compounded, divisible things.

Probability and sensible prose may well serve in natural things, and is commendable. However, in Mathematical reasonings a probable argument is not regarded as useful, nor can its testimony serve as proof. Only a perfect demonstration of certain essential and invincible truths (which have been universally concluded with certainty) will suffice for an exact and pure mathematical argument.

## [the two Principal kinds of Mathematical things: <br> Number and Magnitude]

There are two principal kinds of Mathematical things, namely, Number and Magnitude.
We define Number to be a certain mathematical sum of Units.
A Unit is a mathematical thing that cannot be divided. Because of some likeness to this property of the Unit, something which acts like one, or is counted as one, may reasonably be called One.

We consider a Unit to be a Mathematical thing, though it be no Number, as it is indivisible. Actually, Number is a principal Mathematical thing because it consists of Units.

Magnitude is also a Mathematical thing. Anything whose nature involves length, width, or breadth is a Magnitude.

A Magnitude that has all three dimensions we call a Solid or a Body.
Number
Note the word Unit to express the Greek Monas\& not Unity as we have allcommonly, until now, used.
A magnitude with only two of these dimensions we call a Surface or a Plane.
A magnitude with only one of these dimensions we call a Line.
Every line has two ends. The ends of a line are called Points.
A Point is an indivisible Mathematical thing, which has a certain determined position. Moving a point from a determined position mathematically produces a Line in the direction it moved. In this respect, the ancient Mathematicians referred to a line as the race or course of a Point.

We also refer to a Point as Mathematical thing, even though it is not a Magnitude. It is indivisible because it is an end or boundary of a Line, which is a true Magnitude. We may define a Magnitude to be that Mathematical thing which is infinitely divisible into parts, whether it is a solid, a plane or a line. As I said, though a Point is not a Magnitude, Terminatively we regard it as a Mathematical thing because it is the end or bound of a line.

Neither Number nor Magnitude have any Materiality. First, we will consider Number and the Mathematical Science that pertains to it, which is called Arithmetic. Then we will consider Magnitude and its Science, which is called Geometry. (But I am not content with that word Geometry, for reasons I will discuss shortly).

How Immaterial and free from all matter Number is. Who does not perceive, or wonderfully wonder about this? For neither the pure Elements nor Aristotle's Quinta Essentia [Fifth Essence] can represent the proper matter of numbers. Nor is the purity and simplicity of spiritual and angelical substance proper enough to represent numbers.

As the great and godly Philosopher Anitius Boetius, said " Omnia quacuna a primeva rerum natura constructa sunt, Numerorum videntur ratione formata. Hoc enim fuit principale in animo Conditoris Exemplar."

That is, "All things (which from the very first original being of things, have been framed and made) do appear to be formed by the reason of Numbers. For this was the principal example or pattern in the mind of the Creator."

O comfortable allurement, O ravishing persuasion, to deal with a Science whose subject is so ancient, so pure, so excellent, so surmounting all creatures, and so used by the Almighty and incomprehensible wisdom of the Creator in the distinct creation of all creatures. The distinct parts, properties, natures, and virtues of all creatures are ordered and, by most absolute number, brought from Nothing to the Formality of their being and state.

We may both wind and draw ourselves into the inward and deep search and view of all Creatures' distinct virtues, natures, properties, and forms if we learn the properties of Numbers (as perfectly as the science permits.) And also, farther, arise, climb, ascend, and mount up (with Speculative wings) in spirit, to behold in the Mirror of Creation, the Form of Forms, the Exemplar Number of all things Numerable, both visible and invisible, mortal and immortal, Corporal and Spiritual.

Part of this profound and divine Science was explored by Joachim the Prophesier [Joachim of Fiore, ca. 1135-1202]. By using Formal, Natural and Rational Numbers he was able to predict and foretell particular important events long before they happened. His books are good proof of this. Besides that, the noble Joannes Pico Earl of Mirandola, [Pico della Mirandola,1463-1493] was a trustworthy witness that "Joachim, in his prophesies proceeded by no other way than by Formal Numbers."

This Earl himself, in Rome, posted 900 Conclusions regarding all kinds of Sciences so they might be debated openly. Among the rest of his Mathematical Conclusions (in his eleventh Conclusion), he writes this sentence, in Latin (which I have phrased in English):
"By numbers, a way is had, to the searching out, and understanding of everything able to be known. To verify this Conclusion, I promise to answer to the 74 Questions written below by using Numbers."

To avoid superfluous wordiness and because Pico's works are commonly available, I will not relate these Conclusions, but they should be read diligently and contemplated thoughtfully by earnest Observers. The constant law of numbers is planted in Natural and Supernatural things, and is prescribed to all Creatures, to be kept inviolably. To stay within my bounds, I will simply mention that there are other remarkable things in Pico's Conclusions which demonstrate wonderful mysteries that can be understood by way of numbers.

It is easy to gather that Number has a treble state: One, in the Creator. Another in every Creature (in respect of his complete constitution). And the third in Spiritual and Angelical minds, and in the Soul of man.

In the first and third state, Number is termed Number Numbering.
But in the second state (all Creatures), Number is termed Number Numbered. Number bears such a sway and has such an affinity in our soul, that some of the old Philosophers taught that Man's soul was a Number moving itself. And indeed, it does seem as though we are the result of a Fortunate Accident. However, the Fortunate Accident is that the Creator was a perfect and eternal being long before all Creatures were made.

Therefore, Number Numbering is the discretion, discernment, and distinction of things. In the beginning, God the Creator produced all things orderly and distinctly, according to his discretion. His Numbering was his Creating of all things. And his Continual Numbering of all things is why they are Conserved in being. Where and when he will lack a Unit, there and then, that particular thing shall be Dis-created. (But I won't dwell on this subject)

Man's dividing, distincting, and Numbering creates nothing. But with regards to the whole multitude of Number, it makes certain and distinct determinations. And even though these things be weighty, and truths of great importance (by the infinite goodness of the Almighty Ternarie), there are Artificial methods and easy ways by which the zealous Philosopher may approach this Riverish [abounding in rivers] Ida, this Mountain of Contemplation, and then even more Contemplation.

Number is a thing so Immaterial, so divine, and so eternal, but by degrees, little by little, stretching forth and applying some likeness of itself, it can become Material. It starts, as a Spiritual thing. Then it can be brought lower, to things perceived by the senses, like an echo. Then even lower, to things that may be seen and are numerable. And finally (most grossly) to a multitude of corporal things that can be seen and felt. Of these gross and sensible things, we are trained to learn a certain Image or likeness of numbers, and to use them skillfully for our pleasure and profit. As mortals, our spiritual selves are so coarse, and our understanding is so dull, that our Senses rule the commonwealth of our little world.

Thus we say, Three Lions are three, or a Ternarie. Three Eagles are three, or a Ternarie. Each of these Ternaries is the Union, knot and Uniformity of three discrete and distinct Units. That is, in each Ternarie, we can point out or show three separate parts: One, One, and One. But in Numbering, we say One, Two, Three. How far these visible Ones differ from our Indivisible Units (of pure Arithmetic) no man is ignorant.

From these gross and material things we may also be led back upwards, degree by degrees, directing our rude Imagination towards the conceiving of Numbers absolutely (now, not using created things to represent those imagined Numbers). Finally, at great length, we may be able to find the number of our own earthly name, gloriously exemplified and registered in the book of the most blessed and eternal Trinity.
[the various kinds of Common Arithmetic]
Understand that vulgar Practicers have extended their definition of Numbers, in various ways, past what we call Numbers, whose smallest part is a Unit. The common Logician, Reckonmaster, or Arithmetician, in his using of Numbers, imagines parts smaller than a Unit and calls them Fractions. For example, he will divide a Unit in two, and call it "a half." He can find an infinitely different number of ways to divide the Unit. Even further, he finds Fractions of Fractions.

Addition, Subtraction, Multiplication, Division, and Extraction of Roots are the chief
parts of Arithmetic, the Science that demonstrates the properties of Numbers and all operations to be performed in numbers.

## [Arithmetic of Whole Numbers and Arithmetic of Fractions]

These five sorts of operations work differently with fractions than they do with whole numbers. Operations involving Fractions are so a distinctly different that we give them a specific name. The doctrine of working in whole numbers only, where a Unit is the smallest part allowed, is simply called Arithmetic. Using using smaller parts is called Arithmetic of Fractions.

## [Arithmetic of Proportion]

Similarly, the necessary, wonderful and Secret doctrine of proportionality also works in its own special way so we call it the Arithmetic of Proportion.

## [Circular Arithmetic]

## A.Arithmetic. .Note.

For speed and greater ease of calculation, the Astronomers, (who deal with circular motions), have devised a special manner of ordering numbers, involving Sexagones [multiples of sixty], and Sexagesines [fractions of sixty]. The use of Signs, Degrees, Minutes and Seconds is called the Arithmetic of Astronomical Fractions or the Arithmetic of Physical Fractions. I have shortened the name to Circular Arithmetic because it is also used in circles that are not Astronomical.

## [Arithmetic of Radical (Root) Numbers]

Another special area of Numbers deals with which is Incommensurability and Irrationality, a characteristic that can be seen in the study of Magnitude. Remember, in pure Arithmetic, a Unit is the common Measure of all Numbers. But here, Numbers are like measurements found in Lines, Planes and Solids. Sometimes they are Rational, and sometimes Irrational. These are used in the 5 operations of Arithmetic mentioned above and have many types, like: $\sqrt{ }$ Square Root, $\sqrt[3]{ }$ Cubic Root, and other roots. So this is also considered to be a another different kind of Arithmetic.
[Dee actually uses $\sqrt{ } \boldsymbol{z}$ for the square root symbol and $\sqrt{ }$ e for the cube root symbol.]


The variety of combinations is infinite. Some of these examples involve fractions, so this operation in Arithmetic greatly enlarged by various mixings with the other operations.

To steer clear of objections and to keep it understandable for students, I call this operation the Art of Radical [Root] Numbers. As you can learn in Euclid's Tenth Book, it is incorrect to think that all roots are Irrational Numbers (Surds). Calling them Radical Numbers and prefixing them with a special sign $(\sqrt{ })$ distinguishes them from other Numbers.

## [Arithmetic of Cossick Numbers (involving an unknown); the great Art of Algebra]

Aside from this, consider the incredible power of man's Search and Capacity, his infinite desire for knowledge. By mixing theory and practice he has gone ever further and discovered one of the most Practical uses for Number: the great Arithmetical Art of Equation,commonly called the Rule of Cossick or the Rule of Algebra. The Latins called it Reglam Rei \& Census or the Rule of a Thing and its Value. This name is appropriate because it includes the first and last points of this work [both sides of the equation]. Some of its names in Italian, French, and Spanish include the Latin word Res, but usually it's simply called Algebra. However, there are two ways using this word can be misleading.

One has to do with the idea that Geber invented it [Abu Musa Jabir (Geber) ibn Hayyan, ca.721- ca. 815]. The other has to do with the spelling of the word Algebra.

Geber had great skill in Numbers, Geometry, Astronomy, and other marvellous arts and was
*In the Year 1550 Mathematician named Diophantus wrote 13 books on the subject (of which six are still extant). I was able to borrow them* from the famous Mathematician and my great friend, Petrus Montaureus.

And secondly, the true name is Algiebar, and not Algebra. This can be proven by the title of a work by the Arabian Avicenna, which was translated (with precision) into Latin by Andreas Alpagus (an expert in the Arabic language):
"Scientia faciendi Algiebar \& Almachabel i. Scientia inveniendi numerum ignotum, per additionem Numeri, \& divsionnem \& aequationnem."

Which translated means,"The Science of working Algiebar and Almachabel, that is, the Science of finding an unknown number, by Adding of a Number, \& Division \& equation."

This title includes the name and it also touches on the the principal parts of the Rule. Calling
5. it the Rule of Equation or the Art of Equation clarifies the State of the Rule and highlights its middle part [which is the equals sign, between the first part and the last part].

This Rule has a peculiar Character that makes it different from the other Arithmetical operations. It involves all the kinds of Numbers, Simple, Compound, Mixed, as well as Fractions. Because it contains the whole power of Numbers' practical Application, this Rule and the Arithmetic of Algiebar are profound subjects for Man's intellect to deal with. In human Studies, affairs, and exercises nothing involving number is more profitable or more suited to the divine force of the Soul.

## [practical uses for Arithmetic]

Perhaps you have been looking for proof or evidence of the use, profit, and Commodity of vulgar Arithmetic in the Common life and trade of men. I will now demonstrate how useful Atithmetic can be. I must be careful not to bore you with too many proofs, yet show you enough so that you understand the process. First, I will demonstrate a proof, then give four, five, or six examples. This should be enough to persuade any reasonable man to love, honor, learn, and practice the excellent science of Arithmetic.

Who is a better recipient of the fruits of Arithmetic than Merchants (of all kinds)? Some Merchants don't use Arithmetic, and feel they don't even need it.
How could they possibly refuse the assistance of the Golden Rule (whether using it in a simple or compound instance) either forward or backward?
[In mathematics, the Golden Rule is the "Rule of Proportionality" or the "Rule of Three." When 3 numbers in a proportional equation are given, it teaches how to figure out what the fourth one is. For example, $(2$ to $3=9$ to X$)$ is "forward"; (2 to $3=\mathrm{X}$ to 12) is "backward"]

In the Rules of Fellowship (either with or without regard to time) how can they not be assisted by Arithmetic [Merchants in a company each profit in proportion to the percentage of stock they own]. Arithmetic is necessary even if it's just between a Merchant and his Factor [trading partner]. Wouldn't a Merchant find Arithmetic essential when Bartering wares, or when the exchange was partially goods and partially money?

How could Merchant Adventurers and Sea Travelers order their affairs properly (and without loss) unless certain Rules for the Exchange of money (or Rechange) were devised for their uses?

In many instances, the Rule of Alligation demonstrates truth. In how many instances has the Rule of Alligation been useed to determine a truth so precise that it could not be determined by natural wits, regardless of experience? [Alligation means "a linking or mixing." If two differently priced grains are mixed, what is the price of the mixture? This rule is used in mixing medicines, or metals, or (shamefully) in the dilution of wine.]

And how ample and wonderful is the Rule of False Positions, especially as it has been explained by two excellent Mathematicians (who were acquaintances of mine in their lifetime). I am referring to Gemma Frisius and Simon Jacob. [This rule involves guessing an answer for an unknown in an equation, then making an adjustment upon seeing the result]

Who can briefly summarize the Rules of Capital without Arithmetic? [How much capital or money is needed to get a business or enterprise started.] Who can Imagine the Myriad of various cases and examples (in Act and earnest) that are determined by all these Rules?

I will leave it to the Merchants to explain all the other ways they commonly use Arithmetical Practices.

## The Art of Graduation

Mintmasters and Goldsmiths mix Metals of various kinds and values. They are properly directed and marvelously pleasured Using Arithmetic as their guide. The honorable Physicians will acknowledge that they use the Science of Arithmetic in various ways. One of the main uses is to make compounds of Medicine using the Art of Graduation.

Galen, Aurerois, Arnold of Villanova, and Ramon Lull have each published Rules for determining the new Form Resulting from adding various Degrees above Temperament. But about 200 years ago, a Method was invented by a Countryman of ours that is easier, more precise, and more commodious. (I am uncertain who owns a copy of this little Latin treatise, or when it might be republished.)
R.B. [Roger Bacon]

Both to demonstrate my love of Country and to prove the usefulness of numbers (in this most subtle and fruitful philosophical conclusion), I will briefly explain the essentials.

First draw a circle with a diameter of one inch. Divide the Circumference into four equal parts. Extend four lines from the center outwards through the four points. Make each line $41 / 2$ inches long. (Thus they will be 4 inches long outside the circle.)

Indicate every inch with clear, accurate markings. If you wish, you can subdivide the inches again into 10 or 12 equal, smaller parts. At the ends of the lines write the 4 principal elemental Qualities Hot and Cold (opposing each other) and Moist and Dry (opposing each other.) In the Circle write the word Temperate. This word has a wide range of meanings. For example, it is used in determining the Complexion of Man [the 4 Humours or 4 Temperments in man are choleric, sanguine, melancholic, and phlegmatic.]

*Take Raymond Lull's
council in his book de Quinta Essentia [Fifth Essence]
*Note.

Given two (mixable) things of known* Degrees, their Quantities (or Weights) are either the same or different.

Regardless of whether the two things are equal or different, or if they are of the same or different Qualities [like Hot and Cold], the following rule applies:"The form resulting from their Mixture is in the Middle, between the degrees of the forms that are mixed."

For example, let A be Moist in the first degree and B be Dry in the third degree. Adding 1 and 3 makes 4. The half or Middle of 4 is 2 . Thus, 2 is in the middle equally distant from A and B. Starting at B and counting 2 degrees towards A, the answer is Dry in the first degree. (*Note that the Temperament is not counted. If, at any time, it's involved in the Mixture, simply use a Cipher [zero].)

Here's another example involving C and D on the chart. Suppose C is Hot in the fourth degree and D is even Temperament (or Zero). Adding 4 plus 0 makes 4. The middle, or half, of 4 is 2 . Thus the Form Resulting from mixing C and D is Hot in the second degree.

Here's a third example. I have a liquid Medicine whose Quality of heat is exalted to the fourth Note. degree (like C in the previous example). I have another liquid Medicine whose Quality (namely, E ) is heat in the first degree. (Also let's suppose the quantities of each of these is the same.) Simply subtract the lesser from the greater and divide what remains into two equal parts.

So, subtracting 1 from 4 leaves 3 . And half of 3 is $1 \frac{1}{2}$. Add this to 1 and it results in $2 \frac{1}{2}$. (Or you could have subtracted $11 / 2$ from 4 to also arrive at $21 / 2$.)

If the Temperament Qualities of two things are different and their Quantities are also different, this Second Rule Applies. The proportion of the "lesser quantity" to the "greater quantity" is equal to the proportion of the "greater quantity minus the unknown result" to the "unknown result minus the lesser quantity."

This is easier to see by example. Suppose you had 2 pounds of liquid hot in the fourth degree and only 1 pound of Liquid hot in the third degree. To determine the Form Resulting from the Mixture of these two Liquids
 make a chart like this:

I have devised an easy, brief and general manner of solving this problem using Algiebar. Let's call the Middle form that we are searching for 1 y.
[This is Dee's symbol for "the unknown." His putting a 1 in front of it does not affect it at all. In modern math, "the unknown" is usually the letter X. This tradition derives from Geber's Arabic word for "thing" which in Old Spanish was written XEI. However to avoid confusion with the multiplication sign "X," here I will use the letter Z, which somewhat resembles Dee's symbol.]

So applying the Second Rule, the proportion of the weights (" 1 " is to " 2 ") is the same proportion that "the heavier (4) minus Z " is to " Z minus the lighter (3)."

In short, as 1 is to 2 , so $4-\mathrm{Z}$ is to $\mathrm{Z}-3$. In a proportion which involves 4 numbers, the first times the fourth always equals the second times the third.

Doing that multiplication results in $(2-3)=(8-2 Z)$.
Using the Art of Algebra we add 3 to each side of the Equation, resulting in $Z=11-2 Z$.
To reduce it further, we can add 2 Z to each side. This results is $3 \mathrm{Z}=11$.
Dividing 11 by 3, the Quotient is $32 / 3$. This is the value of the 1 , the Coss or the Thing that we were looking for. So the Form Resulting is Heat in $32 / 3$ degrees.


To check or prove this is easy. Subtracting 3 from $32 / 3$ leaves $2 / 3$. Subtracting $32 / 3$ from 4 leaves $1 / 3$. And the proportion of $2 / 3$ to $1 / 3$ equals the proportion 2 to 1 , which is what was originally given. (Alternatively we could have added 2 Z to each side, prior to subtracting 3 from each side. This reduces to $3 Z-3=8$ which is $3 Z=11$, and the answer is the same.)

Though this example only involves Mixing two things, more commonly three, four, five, six or more things are combined into one Compound. Apply these same rules to determine the Form Resulting from the mixture. The easiest procedure is to determine the Form Resulting from the first two things, then combine that result with the third thing. Continue this way and the final result is the Form Resulting from the mixture of them all.

I don't need to speak much about what the Mixture is. Common Philosophy defines it this way: Mixtio est miscibilium, alteratorum, per minima conjunctorum, Unio. ['Combination' is the unification of the 'combinables' resulting from their 'alteration.' From Debus, Alchemy and Early Modern Chemistry, p. 175]

Every word in this definition is of great importance.
I also don't need to spend time showing how the other manner of distributing degrees also agrees with these Rules. Neither do I need to mention further uses of the Cross of Graduation.

Nor will I give any more examples of the kinds of ways the two aforementioned general Rules can be used. There is enough information here for the quick witted and the Studious. Some may not understand what I mean without a more lively teaching, but this is not the proper place to discuss it in full. It is possible that others, with a proud sniff, might disdain what little I have discussed here and would be ungrateful even if I did elaborate.

To conclude, those with modest and earnest Philosophical minds will praise God highly for this. They will Marvel that the profoundest and subtlest point about the Mixture of forms and Natural qualities: It is matched and married so wonderfully with the simple, easy, and short way of the noble Rule of Algiebar.

Who cannot love, praise, and honor the excellent Science of Arithmetic? For here you can see that the little finger of Arithmetic is mightier and more ingenious than the intellect of 100,000 average men.

## [even more practical uses for Arithmetic]

Next, we will discuss how the wise and valiant Captain can authoritatively be helped by the Rules of Arithmetic in what the Greeks called Taxtixou [Tactics] or the Skill of Arranging Soldiers for Battle.

In his work dedicated to Emperor Hadrian, Aelianus writes about the importance of Numbers and Mathematics in Tactics. He felt that his book was more comprehensive than all previous books written on this Art.

Many worthy Captains, Philosophers and Princes of Immortal fame and memory have praised Aelianus' work, including Aeneas, Cyneas of Thessaly, Pyrrhus Epirota (and his son Alexander), Clearchus, Pausanias, Euangelus, Polybius (a close friend of Scipio), Eupolemus, Iphicrates, and Passidonius. His work discusses the use of Geometrical figures, but the fairest flower in their garland of Tactics, that which helps the Captain the most, is Arithmetic and an understanding of Geometric figures.

There are many ways Arithmetic stands the Captain in great stead. For example, one way is in determining how provisions should be distributed, whether the Army is of a constant size or if the number of soldiers were to suddenly increase. The good Art of Arithmetic might also be used if the number of soldiers were to suddenly decrease, in order to apportion provisions so they will last for a longer time.

The wise, expert, and thoughtful Captain will agree that for other Reckonings, Measurings, and Apportionings, the Science of Arithmetic is one of his chief counselors, directors, and assistants. This was made evident by the Noble, Courageous, loyal and Courteous John, the late Earl of Warwick. Though few knew this young Gentleman personally, his character traits (his lusty bravery, force, and skill in Chivalrous feats, his humbleness, and friendliness to all men) were seen openly by the whole world.

What virtue he had fastened to his breast. What Rules of godly and honorable life he had framed to himself. What notable vices he took great care to eschew. What manly virtues in other noblemen (flourishing before his eyes) he aspired after. What prowess he tried and was determined to achieve. What feats and Arts he began to furnish and fraught himself [acquired] in order to serve his King and Country, both in peace and war.

No one can attest to his Heroical Meditations, forecastings, and determinations better than I. With firm Conscience and to the honor of virtue, I recommend his name be put in the Register of Immortal Fame.

By one act in particular (there were many more that I noted, both in England and France) this John revealed his hearty love of the virtuous Sciences and his noble intent to excel in martial prowess.

He requested of me the best Rules for the ordering of all Companies, sums, and numbers of men (either from Greek or Roman times or from new Strategies devised in our times). It was taken into account whether a soldier had one weapon (or more), whether they had Artillery (or not), and whether they were on horseback or on foot. It was considered whether he was trying to make a few men seem like a large force, or if many men were to appear as only a few. Or if the soldiers should march as a large group into the Battlefield, or engage in several minor skirmishes, or even to arrange an Ambush. He wrote the pertinent Arithmetical Rules on a vellum parchment which he kept in a Gold Case worn around his neck. It was his most precious Jewell, his most trusted Counselor. Thus, he enshrined Arithmetic in gold. Of Number's results he had good hope.

I hardly need to provide testimony as to how needful, fruitful, and skillful Arithmetic is for Schoolmasters of Justice. By this I mean all types of Lawyers. Even Civilians can attest to the idea that the Art of Numbers is needed to perceive ancient Roman Laws or how an infinite number of cases of Justice are able to be settled. Papinianus instituted a just law of partition and allowance between a man and his wife after a divorce by using the great Art of Arithmetic. Accursius, Baldus, Bartolus, Jason, Alexander and finally Alciatus used Arithmetic to detect, convince, and make the truth shine clearly instead of jumbling, guessing and erring about the equity and Intent of the lawmaker. Good Bartolus, using Accursius' thorough Glosse, wrote about apportionings:
"Nulla est in toto libro: hac glossa difficilior: Cuius computationem nec Scholastici nec Doctores intelligunt ..."

That is, " In the whole book, there is no Gloss harder than this, Whose account or reckoning, neither the Scholars, nor the Doctors understand ..."

What can they say of Julian's law (Si ita Scriptum ...etc.) regarding the just distribution of a deceased man's estate among the wife, Son, and daughter? How can they perceive the Arithmetical Reckoning of Africanus where he discusses Lex Falcidia. How can they defend him from his Reprovers or even understand his supporters like Johannes, Accursius Hypolitus and Alciatus? How can they even perceive how skillfully Africanus' reckoning was made?

He proportioned the Sums bequeathed to the legitimate heirs in this way: Upon death, the heirs received $171 / 7$ [percent] of the estate. After 10 months another $126 / 7$ [percent] of the estate was distributed. This makes a total of 30 [percent]. The proportion of $171 / 7$ to $126 / 7$ is the same proportion that 100 has to 75 , that is, the Sesquitertia, or 4 to 3, which makes 7 .

This noble Earl died in the Year 1554 scarcely 24 yaers old having no children with his wife, the Daughter of the Duke of Somerset

In many areas of Civil Law, an expert Arithmetician is required in order to understand the deep Judgement and Just determination of the Ancient Roman Lawmakers. One must be even more of an expert to equitably decide the wide the variety of Cases in Civil Law. Thus, you can conjecture that in Canon Law and in the laws of the Realm (which bear chief authority with us), Justice and equity would be executed more skillfully with knowledge of Arithmetic and Proportions.

Many worthy Philosophers and prudent lawmakers, who have written many books $D e$ Republica [Concerning the Republic] (on the ways to procure and maintain the best state of Commonwealths) have already determined the Rules of Justice.

Justice is not only the Base and foundation of Commonwealths, but also the total perfection of all our works, words and thoughts. It is a virtue that pertains to everyone. God challenges this at our hands. To be honored as God. To be loved as a father. To be feared as a Lord and master. Our neighbor's proportion is also prescribed by the Almighty lawmaker. That is, do unto others as we wish others would do unto us. These proportions are necessary in Justice, commendable in duty, and are essential to the life, strength, maintenance and flourishing of Commonwealths.

Aristotle in his book Ethics (to fetch the seed of Justice and use it as a beacon) was reluctant to use the perfection and power of Arithmetical and Geometrical proportions of Number.

Plato's purpose in his book called Epinomis (the Treasury of all his doctrine) is to seek a Science, which, when a man had it perfectly, he might seem (and indeed so be) Wise.

Briefly discussing other Sciences, he finds them inadequate. But of the Science of Numbers, he says, "Illa, qua numerum mortalium generi dedit, id profecto efficient.. Deum autem aliquem, magis quam fortunam, ad salutem nostrum, hoc munus nobit arbitror contuliffe ...Nam ipsum bonorum omnium Authorem, cur non maximi boni Prudentia dico, causam arbitramur."

This translates as: "That Science, verily, which has taught mankind numbers, shall be able to bring it to pass." And, I think, a certain God (rather than fortune) gave us this gift for our bliss.

For why should we not Judge he who is the Author of all good things to also be the cause of the greatest good thing, namely Wisdom? Then, at length, he proves that Wisdom can be attained by good Skill of Numbers. With which great Testimony and the manifold proof and reasons, (expressed earlier), you may be sufficiently and fully persuaded (by the perfect Science of Arithmetic) to agree with Plato.

Of all Sciences besides Thoelogy, Arithmetic is most divine, most pure, most ample, most profound, most subtle, most commodious and most necessary. Its close Sister is the Absolute Science of Magnitudes, of which I now intend to write (by the Direction and Aid of him, whose Magnitude is Infinite, and to us, Incomprehensible).

Both with the Multitude and also with the Magnitude of Marvelous and fruitful truths, you (my friends and Countrymen) may be stirred up, and awakened, to behold what certain Arts and Sciences (to our unspeakable behalf) our heavenly father, has prepared for us and which have been revealed to us by various Philosophers and Mathematicians.

## [Geometry (Megethologia) or Science of Magnitudes]

Of Number, a Unit, and of Magnitude, a Point, do seem to be much like original causes. Nevertheless, there is a great difference between the two. We defined a Unit, to be an indivisible Mathematical thing. A Point, likewise, we said to be an indivisible Mathematical thing.

Furthermore, a Point may have a certain determined Situation. We may assign or prescribe a Point to be here, there, yonder, etc. However our Unit is free and can abide no bondage, nor be tied to any place or seat, (whether divisible or indivisible).

## A Point may have a Situation limited to him, a certain motion, to a place, and from a place.

 But, a Unit cannot be thought of as having any motion.A Point, by its motion, Mathematically produces a line (as we said before) which is the first and most simple kind of Magnitude. But, a unit cannot produce a number. Even though it is produced by a Point being moved, a line does not consist of points.

Contrarily, even though it is not made by a unit, Number consists of units, as a material cause.
Formally, Number is the Union or Unity of Units.
This uniting or knitting is the workmanship of our mind. From these distinct and discrete units our mind makes a Number, which by uniformity, results in the formation of a certain multitude of units. Thus, every number has the Unit as its least part.

But Magnitudes (like a line) do not have a least part as they are infinitely divisible. All Magnitude is either a Line, a Plane, or a Solid. A Line, Plane, or Solid can not be perceived by any sense, nor can they be exactly represented in any way, nor produced by Nature, the way Number (by degrees) is able to be perceived. However, we can use visible forms to imagine what our Mathematical Line is or what our Point is. So precise are our Magnitudes, that one Line is no broader than another, for they have no breadth. Nor do our Planes have any thickness. Nor do our Bodies have any weight regardless of how large their dimensions are.

Our Bodies are both Smaller than either Art or Nature can produce yet also Greater than all the world can comprehend. Our least Magnitudes can be divided into as many parts as the greatest. An inch-long Line may be divided into as many parts as may the diameter of the whole world (whether that diameter is extended from East to West or in any other direction.)

What privileges our two Mathematical Sciences exhibit over all manual Art and Nature. They deal with things of such power, liberty, simplicity, purity, and perfection. They proceed so certainly, so orderly, so precisely. The Mechanical Workman who can best represent Mathematical works is judged as the most excellent. Our two Sciences are pure in their own ways and in their own Matters. They each can be Demonstrated in ways that are plain, certain, universal and eternally true. All Philosophers, from the beginning to now, have called the Science of Magnitude (its properties The ever ple conditions and appurtenances) by the name Geometry. But truthfully, this term is too base and scant for Geometry a Science of such dignity and fullness.

Possibly that name has been used by all wise men throughout history so that it might carry in perpetual memory the first and most notable benefit which this science showed to common people. In other words, how Common land might be divided into parts using boundaries. Sometimes boundary lines got lost or confused, as in Egypt when the Nile River (the greatest and longest river in the world) overflowed every year. Sometimes land was bequeathed, assigned, or sold and needed to be properly divided.

Through ignorance, negligence, fraud, or violence often one man might wrongfully limit, measure, encroach or challenge the lands of another, causing great loss, disquiet, murder, or even war. Finally, by God's mercy and by man's Industry, the perfect Science of Lines, Planes, and Solids (like a divine Judge) allowed every man to have his own. Pleased by this art, and greatly relieved by the just measuring, the Philosophers who wrote the rules for land measuring named it Geometria, that is, (according to the very etymology of the word) "Land Measuring". The people knew no further use for Magnitude other than in Planes.

And the early Philosophers and Scholars did not disclose to these people anything other than flat, plane Geometry. But Philosophers like Plato and Pythagoras, (even thiugh they understand the etymology of the word Geometria) all used the term. Plato defines it as, "Studium quod circa planum versantur" [The study of flat planes]

Euclid, in the Elements of Geometry, never mentions Land Measurement, but clearly demonstrates how Geometry is useful for more than measuring Plane surfaces. Thus, we need a better " name for our Mathematical Science of Magnitudes, which regards neither clod nor turf, neither hill " nor dale, neither earth nor heaven. It is absolute Megethologia, not walking the ground and dazzling
" the eye with pole, perch, rod, or line, but lifting the heart above the heavens by invisible lines and immortal beams, meeting with the reflections of incomprehensible light, and so procuring unspeakable Joy and perfection of what I prefer to call Megethica or Megethologia.

Divine Plato exercised good taste and judgement regarding the name Geometry by warning his Scholars about the name Geometry in the seventh Dialogue of the Commonwealth [in Republic, Book 7].

Here is a good translation from Plato's Greek into Latin: "Profecto, nobis hoc non negabunt, Quincuna vel paululum quid Geometria gustarunt quin hac Scientia, contra omnino se habeat, quam de ea loquuntur, qui in ipsa versantur."

In English, this reads: "Verily (says Plato), whosoever has tasted even the least amount of Geometry, will not deny this Science is of another condition quite contrary to that which they who are exercised in it speak of it."

And there it follows, regarding our Geometry,
"Quod quaeritur cognescendi illius gratia, quad simper est, non \& eius quod oritur quandog \& interit. Geometria, eius quod est semper, Cognitio est. Attollet igiture (o Generose vir) ad Veritatem, animum ata ita, ad Philosophandum preparabit cogitationem, ut ad supera convertamus, qua, nunc, contra quam decet, ad inferiora deycimus, \&c. Quam maxime igitur praecipiendum est, ut qui preclarissimam hanc habitat Civitatem, nullo modo, Geometriam spernant. Nam \& quae praeteripsius propositum, quodam modo esse videntur, haud exigua sunt \&c."
"That [Geometry] is learned, for the knowing of that which is forever, and not of that which, in time, is brought to an end. Geometry is the knowledge of that which is everlasting. It will lift up therefore (O Gentle Sir) our mind to the Truth, and by that means, it will prepare the Thought to the Philosophical love of wisdom, that we may turn or convert toward heavenly things (both mind and thought) which now, when it comes to us, we cast down on base or inferior things. ... Chiefly, therefore, it should be commanded, that those who inhabit this most honorable City, must in no way look down upon or disregard Geometry. There are many important things that seem to be outside the realm of Geometry, but they are not ..."

And besides the many uses of Geometry in matters pertaining to war, he adds that there is a second unpurposed result and commodity arising from Geometry saying:
"Scimus quin etiam, ad Disciplinas omnes facilius per descendas, interesse omnino, attigerit ne Geometriam aliquis, an non \&c. Hanc ergo Doctrinam, secondo loco descendam Juvenibus statuamus."
"But, also, we know, to learn all Arts more easily, it is very important that one have knowledge of Geometry. Let us therefore make an ordinance or decree that this Science shall be learned by all young men in the second place." [that is, following Arithmetic]

This was the Judgment of Divine Plato, both of the purposed, chief, and perfect use of Geometry and of its secondary, dependant, and derivative commodities. For us Christian men, a thousand thousand more occasions exist that require the assistance of Megethological Contemplations, which will train our Imaginations and Minds, little by little, to forsake and abandon the gross and corruptible objects of our outward senses, so we can apprehend Mathematical Things by sure demonstrative doctrine.

And by these *Megethological Contemplations readily we will be helped and conducted to conceive, discuss, and draw conclusions about Intellectual, Spiritual, and Eternal affairs. These things are related to our everlasting Bliss, which otherwise (without Special privilege of Illumination or Revelation from heaven), no mortal man's intellect (naturally) is able to reach or encompass.

And, verily, by my small Talent (from above), I am able to prove and testify that the literal text and order of our divine Law, Oracles, and Mysteries requires more skill in Numbers and Magnitudes than the expositors have usually uttered. They have only, at most, shown their own lack of knowledge. (To name any is needless, and this is not the occasion to note the places. But if I am duly asked, my answer is ready.)

And without the Literal, Grammatical, Mathematical or Natural truths of such places (perceived by good and certain Art), the Spiritual sense of those places (by Absolute Theology) cannot be comprehended. Therefore, no man can doubt that toward the attaining of incomparable knowledge and Heavenly Wisdom, Mathematical Speculations (both Numbers and Magnitudes) are means, aids, and guides - ready, certain, and necessary.

Henceforth, in this my Preface, I will frame my talk to the fugitive Scholars of Plato, or rather, to those who can (and also will) use their outward senses for the glory of God, for the benefit of their Country, and for their own secret contentment or honest preferment on this earthly Scaffold.

To them, in an orderly manner, I will recite. describe and declare a great Number of Arts derived from our two Mathematical fountains and seen in the fields of Nature. Because of these fountains, the Seeds and Roots that lie deeply hidden in the ground of Nature are refreshed, quickened, and provoked to grow, shoot up, flower, and bear infinite and incredible fruit.

These Arts depend more upon Magnitude's properties more than upon Number's properties. And there is good reason why we call them Arts or more specifically, the Derivative Mathematical Arts.

I define an Art to be a "complete Methodical Doctrine that deals with enough particular matter to give the Metaphysical Philosopher knowledge necessary to the human state." I define a Derivative Mathematical Art as that which orders and confirms its doctrine as perfectly as the subject matter will allow (by a Mathematically demonstrative Method in Numbers or Magnitudes).

I intend to use the name Mechanician differently than it has been used previously. Its's only appropriate (for distinction sake) that I give you also a brief description of what I mean by this. A Mechanician, or a Mechanical workman, is he who is skilled to work and finish any sensible work without knowledge of Mathematical demonstration which a principal or derivative Mathematician has demonstrated or can demonstrate.

I know full well that he who invents or makes these demonstrations is generally called A Speculative Mechanician or a Mechanical Mathematician. So in many instances, one man may have several different names, depending on the various arts in which he is skilled.

For example, a Logician, sometimes (in dealing with the same matter in different ways) may also be a Rhetoritician. I make mention of these trifles, (as now, in respect of my Preface) for the sake of subtle curious disputers. In other places, they may ask me to support my reasoning, but here I will not dwell on it.

## [measuring things at hand using Common Geometry]

From the purity, absoluteness, and Immateriality of Principal Geometry, another kind of Geometry is derived. What the vulgar call Geometry is the Art of Measuring the qualities and contents of sensible magnitudes.

I call this Mecometry [Mechanical Geometry]. It teaches how to measure things at hand, or things to be measured in the field. It teaches how to measure linear distance or circumference of Length, Plane, or Solid using a Compass, Rule, Square, Ell, Perch, Pole, Line, Gaging rod (or similar instrument).

Measuring the area of any plane Surface, whether it be Surveyed ground, measured Board, Glass, or something similar is named Embadometrie.

Measuring the Solidity or contents of any bodily thing like Timber, Stone, the content of Pits, Ponds, Wells, Vessels, small \& great, of all shapes for Wine, Oil, Beer, or Ale is commonly called Gaging. And the general name of these Solid measures is called Stereometry.
[measuring things at a distance using Common Geometry]
Also, this vulgar Geometry can teach the practiser how to measure things even if there is a good distance between him and the thing measured. This measuring of how far an observable thing (on land or water) is from the measurer is called Apomecometrie [Apo means out of + mechanical geometry]. Measuring the depth below or height above the level where the measurer is, whether seen on land or in water, is called Hypsometrie.

Measuring the width of anything in the measurers' view, whether situated on Land or Water is called Platometrie [Plat means flat]. Though here I'm discussing not only things measured on Land and Water, but also the height of clouds or the height and volume of blazing Stars and the Moon. I will touch more upon these kinds of measurement when discussing the Arts of Perspective and Astronomy.

## [Feats or Arts of Commom Geometry]

[Geodesy] [surveying]
From these Feats springs the Feat of Geodesy or Land Measuring, a way to cunningly measure and Survey far-off Land, Woods, and Waters. I say more cunningly, but God knows in these realms of England and Ireland great wrong and injury has (in my Time) been committed by untrue measuring and surveying of Land or Woods (whether through ignorance or fraud).

Note.
But of this I am certain, the difference between truthful and untruthful surveys might be determined by hiring an excellent Mathematical Reader from each of our two Universities for a mere 100 marks a year.

The French King employs two such Mathematical Readers from the famous University of Paris at the cost of 200 French Crowns. But let's return to our purpose and see how the skills of Geography, Chorography, Hydrography and Stratrithmetry have grown from this knowledge of Geometry.
[Geography] [topography of large areas]
Geography teaches the various ways (spherical, in plane, or other) to describe and design and represent (in commensurations analogous to Nature) the situations of Cities, Towns, Villages, Forts, Castles, Mountains, Woods, Havens, Rivers, Creeks and other such things upon the surface of the earthly Globe (either all of it or a principal part of it).

Daily and hourly, many men realize the great pleasure and many benefits of this Art. Some collect artifacts from battles fought, earthquakes, heavenly firings and similar occurrences mentioned in history books to beautify their Halls, Parlors, Chambers, Galleries, Studies or Libraries. They help us understand the geography of adjoining lands and lands quite distant from us.

Such maps might have come from that little morsel of ground in the heart of Christendom [Jerusalem], or from the large dominion of the Turks [Asia Minor], or from the wide Empire of the Muscovite [Moscow, or Russia] not to mention the rest of the world. Some use the maps to guide them on their journeys to far lands, and others use them to understand the travails of other men.To properly explain the various reasons men like, love, obtain, and use Maps, Charts and Geographical Globes would require a whole book.
[Chorography] [local topography]
Chorography seems like an underling or branch of Geography, but it has many practical uses. Some call it Topography. [In Greek Xora and Topo both mean place.]

It teaches how to analogically describe the contents of a small circuit of ground while disregarding the surrounding parcels. In the territory or parcel of ground it describes, it leaves out no notable or odd thing that is visible above ground. Sometimes it even gives a peculiar mark or warning about underground things, like Metal mines, Coal pits, Stone quarries or the like.

Thus, a Dukedom, a Shire, a Lordship (or even less) can be accurately depicted. It is marvelously pleasant and profitable to view the plot of a City, Town, Fort, or Palace in true Symmetry without having to actually be there. Out of Gunshot, an Architect can study the topography of Hills, Rivers, Havens and Woods.
[Hydrography] [oceans]
Hydrography provides us with a perfect analogical description of the Ocean seacoasts in the principal parts of the world on either a flat plane or a round Globe. It depicts not just the Seacoasts but also the Islands and places of danger like Quicksands, Banks, Pits, Rocks, Countertides and Whirlpools.

As Geography deals principally with the Earth's description, Hydrography deals chiefly with Water. But it also incorporates certain dangerous Landmarks visible form the sea, with regards to their compass direction, location, shape, and size.

And along all the coasts, a Hydrographer should record what Moon makes a full Sea and how the Tides and Ebbs come and go. The Hydrographer should know by soundings about the depths and ways of Channels (at high and low tide) through observation and diligent Measuring.

There are many other aspects of Hydrography (or how to make a Rudder) that I could write about, like the 32 points of a Compass or how to describe the location of a place on the Globe. (Only four people in all of England know that a Sphere in plane has neither straight lines nor circles.)

I could write about matters like the Variation of the Compass from true North (of great importance to all), but I will stop as I've already enlarged the bounds and dutys of a Hydrographer more than any man to this day. However I am quite able to prove that all these things pertain to the Hydrographer. Ultimately the chief purpose of this Art is in the Art of Navigation, but it has other uses and can be enjoyed by those that never go to sea.

## [Stratarithmetry] [battle arrays]

Stratarithmetry is the skill (pertaining to war) by which a man can depict using Geometrical figures a certain grouping of Soldiers. (This is because there is a regularity in the space between soldiers. You can't take a fraction of a man, but any overplus of men can be added to the next troop.) Thus, any army or company of men (standing orderly, in a shape

* Note.

The dif-" ference " between " Stratarith-" mike and Tacticie known dimension) can easily be counted*.

This is a sufficient description of Stratarithmetry for now. It differs from Tacticall De aciebus istruendis ["Tactics, the plannning of a battle array"] because it involves the wisdom, foresight and skillful ability to arrange and purpose a company of men.

By figure, I mean either a Perfect Square, Triangle, Circle, Oval, long Square (the Greeks called this Eteromekes), Rhombus, Rhomboid, Lunular, Ring, Serpentine and Other Geometrical figures used in past and future wars for commodiousness, necessity and advantage. Stratarithmetry is also useful in making a true report or estimate of the number of Enemy foot soldiers and horsemen who might still be far off.

Even to provide a "not more than" or "not less than" figure is not an easy thing, even for those so bold enough to take on that challenge. In various instances, a Captain can use Geometrical Figures in taking advantage of the three kinds of usual spaces between footmen and horsemen. If he has many men, they can be arranged to make the greatest show. If he has few men, he can use Figure and space to make it seem as though he has many.

But by Chorography you can better determine if the Known Figures are regular (in sides and angles). You can determine when the use of a Triangular arrangement is beneficial. You might find it strange dealing with Arithmetical figures in forming an arrangement for Battle, as their contents differ so much from those of Geometrical Figures.

The Herald, Pursuivant, Sergeant Royal, Captain (or whoever) can improve the judgement of his eye or his skill in Tactical Ordering by using Geometrical instruments, the Astronomer's Ring, and the Astronomical Staff (which is conveniently constructed to be portable). He may wondrously help himself by using a perspective Glass [early version of a telescope] which (I trust) in the future will be more refined than they are these days.

I have briefly reviewed a few of the Artificial Feats that use vulgar Geometry, but there are many Methodical Arts that are of great usefulness even though they lack the purity, simplicity, and Immateriality of our Principal Science of Magnitude.
J.D.

Friend, you may find it hard to perform my description of this Feat, as battlefields are not always regular shapes. Try breaking them down into triangles. Indeed, it does seem strange to mix battlfields and geometrical figures.

## [Arts that are Derived from Arithmetic and Geometry]

Here are the proper names of the Methodical Arts that derive from Geometry (and which are interrelated as well). Perspective, Astronomy, Music, Cosmography, Astrology, Statike, Anthropography, Trochilike, Helioscophy, Pneumatithmy, Menadry, Hypogeiody, Hydrogogy, Horometry, Zography, Architecture, Navigation, Thaumaturgike and Archemastry. It is essential I specifically describe each of these and explain their benefits in order to make this Preface a sweet, pleasant Nosegay [bouquet] for you, to comfort your spirits.

You may be almost out of courage and in despair (through brutish brute) supposing that Geometry is only useful for building a house, a curious bridge, the roof of Westminster Hall, or some witty, pretty device, or engine [mechanical device] and is only useful to a Carpenter or a Joiner or the like. By word and work, I will prove that the situation is far different than most people in the world commonly think.

Among these Arts, Perspective should be learned before perfect knowledge of Astronomical Appearances can be attained, and for good reasons. Light is the first of God's Creatures. The eye, the light of our bodies is its most mighty Sense and its most Artful and Geometrical organ. Therefore, we will begin with Perspective.

## [The Art of Perspective] [optics]

Perspective is the Mathematical Art which demonstrates the manner and properties of all Radiations-Direct, Refracted, and Reflected. This Description or Notation is brief, but it reaches as far as the world is wide. It concerns all Creatures, all Actions, and passions, and is performed by the Emanation of beams.

By Beams or natural lines I mean not only of light or of color (though they give show, witness and proof that the Art is grounded on), but also the certain and determined active Radial emanations of other Forms, both Substantial and Incidental.

By this Art (not including its highest points) we may use our eyes and light with greater pleasure and more perfect Judgement both in things seen in light and of other things which work and produce their effects similarly to the Radiation of Light.

We should be ashamed to be ignorant of the reasons why our eye is deceived and abused in various ways, like the way the eye perceives a far off Globe or Sphere to be a flat Circle on a plane, or the way a Square on a plane might appear to be round. Or the way distant parallel walls appear unparallel, or a flat roof appears to bend downwards or a flat floor appears to bend upwards. Or the way things moving swiftly appear to be moving faster when they are near and slower when they are distant. Or of when one thing is moving slightly slower than another, the slower thing appears to be standing still. These are all errors of the eye.

One should learn the reasons for the order of the Colors of the Rainbow, its size, location and height. It is pleasant, necessary and commodious for man to understand why two or three suns might appear at the same time, to know the cause of Blazing Stars and similar things caused quite naturally (yet signifying further matters).

Yea, isn't it greatly against the Sovereignty of Man's nature to be amazed and confounded right in front of his very eyes, like a Peacock's tail or the neck of a Dove, or a whole oar that seems to be broken when seen through water.
[The Greek Atomist Lucretius mentions all three of these examples (peacock tail, dove's neck and bent oar) in Book 2 of his work De Rerum Natura, On the Nature of Things]

A marvelous Glass [Mirror]
S.W.P.
[Sir
William
Picker-

Far off things can appear near. Near things can appear far off. Small things can seem large. Large things can seem small. One man can seem like an Army. If he doesn't understand perspective, a man might even be cursedly afraid of his own shadow.

Yea, looking into a certain mirror [concave] and drawing a dagger or sword towards the mirror you might suddenly stand aback in surprise at the image that appears in the air between you and the mirror. A hand, with sword and dagger will be stabbing back and do whatever you do in the mirror. This may sound Strange, but it's more amazing than words can describe.

Nonetheless, the reason for this effect can be explained by Optical principles. I won't get into the explanation here, but for those of noble courage who long ardently for the wisdom of Natural Causes, let him understand that he may find proof of this even here in London. A certain English gentleman (who is an Odd man in this land, but his skill in the Mathematical sciences and languages, and good service to his Country make him an honorable man) is able and (I am sure) willing to let this mirror be seen, thus proving my assertion. For the benefit of the honorable and to repress the arrogance of the ignorant with their malicious mouths, I here request him to let his Mirror and proof to be seen. Then you will better understand what I have described.

This Art of Perspective is excellent but no man would easily believe it without Actual proof. Without Perspective, Natural Philosophy cannot be fully understood. Without Perspective, Astronomy cannot be well grounded, nor can Astrology be verified and avouched for.

The part of Perspective which deals with Mirrors is called Catoptrics. It has too many marvelous and profitable uses to explain here, but the principal conclusions are already well known.

But before you have learned enough about the power of Nature and Art, you might not fully comprehend some parts of Perspective and slip into light Judgement of them, so I shall refrain from explaining them all here.
[Dee uses this expression, "the Power of Nature and Art" in the "Thus the World was Created " chart of the Monas Hieroglyphica]

## [The Art of Astronomy]

Astronomy is a Mathematical Art which demonstrates the distance, magnitudes, and all natural motions, appearances, and passions of the Planets and fixed Stars, for any time (past, present or to come) in respect to a certain Horizon or without respect to any Horizon. By this Art we can ascertain the distance from the center of the Earth to the Starry sky and each of the Planets, or how large any visible fixed star or Planet is compared to the size of the Earth.

By this Art we can ascertain that the Solidity, Mass, and Body of the Sun is $1617 / 8$ times the size of the Earth. And that the Body of the early globe and Sea is $427 / 8$ times larger than the Moon. Thus, the Sun is $694025 / 64$ times larger than the Moon. Yet the unskillful man would judge them to be the same size. Therefore, by Necessity one is much farther from us than the other.

The Sun, when he is farthest from the earth (which now, in our age is in the $8^{\text {th }}$ degree of Cancer) is 1179 earth radii from the Earth. And the Moon, when she is farthest from the earth is $681 / 3$ earth radii from the Earth. The nearest the Moon comes to Earth is $521 / 4$ earth radii.

The starry sky is $20081 / 2$ earth radii from Earth. Subtract the Moon's nearest distance from this and it makes $200291 / 4$ earth radii.

The heavenly Palace is so thick that the Planets have all their exercise in, and marvelously perform the Commandment and Charge given to them by the Majesty of the King of Kings in the realm Genesis calls Ha Rakia [Hebrew for "the Expanse"]. Consider it well.

The radius of the Earth is $34364 / 11$ miles. Its circumference is about 21600 miles. This makes each of the 360 degrees of a circle 60 miles.

If you contemplate this little parcel of Astronomical fruit regarding the size and distances of the Sun, Moon, Starry Sky and the huge mass of the Ha Rakia you will find your conscience moved and sing the confession of God's Glory and say:

The Heavens declare the glory of God, and the Firmament (Ha Rakia) showeth forth the works of his hands. And so forth, for the first five staves of that Kingly Psalm.

Well, well, it is time for some to lay hold on Wisdom and to Judge the truth of things. We ought not to simply expound the Holy word through Allegories and Neglect the wisdom, power and Goodness in God which can be seen and learned from his Creatures and from Creation. Holy Scripture declares to us very many Mysteries of the nature and properties of Creation by parables and Analogies.

To us, the Frame of God's Creatures is a bright mirror. By reflection it Rebounds our knowledge and perception, Beams, and Radiations of the Image of his Infinite goodness, omnipotence, and wisdom. Thus we are taught, persuaded, and thankful to Glorify our Creator as God.

Could the Heathenists find use for these most pure, beautiful and Mighty Corporeal Creatures? Can we find these uses after the true Sun of righteousness has risen above the Horizon of our temporal Hemisphere? It has so abundantly streamed into our hearts. Its goodness, mercy and grace has heat which All Creatures feel, heat which is both spiritual and Corporeal, Visible and Invisible. Shall we look upon the Heavens, Stars and Planets like the Ox or the Ass does, not wondering what they are or how they were created?

If we are to better understand why All Creatures were created chiefly to glorify the Almighty
Creator by all means possible, we should (as Plato says in Epinomis):
"Nolite igonare Astronomiam, Sapientissmus Quiddam esse"
"Do not be ignorant that Astronomy is a thing of excellent wisdom."
From the beginning, Astronomy was commended, and in a way commanded, by God himself, as he made the Sun, Moon, and Stars for us as Signs, knowledge of the Seasons, and for the Distinction of Days and Years.

Men should take particular note of this word "Signs." Consider it along with the tenth Chapter of Jeremiah. Some may think they have found a rod. But let modest reason be the indifferent Judge of who should be beaten with the rod if they don't study Astronomy.

Leaving that, I pray you understand this: The Distinction of the Seasons, years, and New Moons cannot be understood without diligent Observation, examination, and calculation of the periods and courses of celestial bodies.

Knowledge of the Art of Astronomy is required for Understanding the Courses of Times, days, Years, and Ages as well as for the Considerations of Sacred Prophesies foretold in High Mystical Solemnities which will be accomplished in due time.

It is required for an understanding of other human affairs, like covenants between man and man, and many other great uses.

There would be great uncertainty, Confusion, untruth, and brutish Barbarity without the wonderful diligence and skill of this Art.

An Astronomical Staff is more useful than simple belief in learning and determining Times and periods of Time that are written about in the Records of the heavenly book.

## [The Art of Music]

The Original cause of Music is Motion. Having spoken about the motions (both swift and Slow) which are performed in the Firmament of Nature in the Art of Astronomy, I will now speak of another king of Motion, that which produces an audible Sound, and which (when made by Man) comes in numerous varieties. What I call the Science of Music, the Greeks called Harmony. (I will not meddle in the Controversy between the ancient Harmonists and Canonists.)

Music is a Mathematical Science which teaches (by sense and reason) how to perfectly judge and order the diversity of sounds, high and low.

As Plato says, Astronomy and Music are Sisters. Just as Astronomy was made for the eyes, the ears were made for Harmonious Motion. Astronomy has a more divine Contemplation (and commodity) than the mortal eye can perceive.

Music might also be considered more preferred to the *Mind than the ear. And from audible sound we ought to ascend to the examination of which numbers are Harmonious and which are not and why some are and some are not. Pythagoras' Harp with eight strings.
4. 3 .
5.
6.


7.
8.

Also, same might be said of Mercury's* two Harps, each of four Elemental Strings.
And a very strange matter might be alleged of the Harmony appropriate to our Spiritual part as Ptolemy wrote about in his third book* (Chapters 4 and 6).
*And what is the cause of the apt bond or friendly fellowship between our Intellectual and Mental part and our gross and corruptible part? It is a certain Mean or Harmonious Spirituality which results from the participation of both of them.

There is a Harmony in the the *Tune of a Man's voice.
And certainly there is Harmony in the *Sound of an Instrument.

The average Musician would hardly believe what might be said about Harmony. It is a Mixture (as I might call it) collation, or Application of these Harmonies, as of 3, 4, 5 or more.

Marvelous effects of these proportional considerations have been found and more may yet be found. These wondrous effects are useful to the State.

Democritus and Theophrastus write that griefs and diseases of the Mind might be diagnosed and cured by Music. Harmonic Consonance has accomplished marvelous things according to the Works of Terpander, Arion, Ismenias, Orpheus, Amphion, David, Pythagora, Empedocles, Ascelepiades, and Timotheus. But I won't discuss them further here.

Commonly heard Music is so commodious and pleasant that I might make this claim: If it wasn't, more Musicians and Listeners would object to my definition of Music than would agree with it. The worthiness of this art is self evident (I wish other arts were as obvious), so I will spare you more explanation, and proceed.

## [The Art of Cosmography]

Of Cosmography I will give you some brief information. Cosmography is the whole, perfect description of both the heavenly and elemental parts of the world, their essential homologous application and mutual collation. This art involves Astronomy, Geography, Hydrogaphy and Music. It is not the small, simple Art that many consider it to be. It matches Heaven and Earth in one frame and appropriately corresponds them. Thus, the Heavenly Globe might (practically speaking) might be described on the Geographical and Hydrographical Globe.

We should consider the Equinoctial Circle, the plane of the Ecliptic, Colures, Poles, Stars in their true Longitudes, Latitudes, Declinations and Verticality. [Colures are two great circles that intersect each other at right angles at the poles]

Also consider Climates and Parallels and (with a Horizon annexed) the revolution of the earthly Globe (as the Heaven is carried by the Primovant [Prime Motion] in about 24 equal hours).

Much has been written about these matters by Virgil in his Georgikes, by Hesiod, by Hippocrates in his Medicinal Sphere (written to Perdicca, King of the Macedonians) by Diocles (writing to King Antigona), and by other famous Philosophers.

Cosmography is essential for the timely manuring of the earth, for Navigation, for the Alteration of man's body whether he is healthy, sick, wounded, or bruised. It is essential to understand the Revolution or motions of the Cosmographical Globe, the Rising and Setting of the Sun, the Length of days and nights, the Hours and times (both day and night) and many other pleasant and necessary uses.

Many uses are known, but some remain to be discovered by someone clever enough to turn a small spark of a true fire into a wonderful bonfire.

## [The Art of Astrology]

I make Astrology a separate Art from Astronomy, not by my own whim, but by good reason and authority. For Astrology is a Mathematical Art that reasonably demonstrates the operations and natural beams of light and the secret influence of the Stars and Planets in every element and elemental body, at all times and from any given Horizon.

This Art is informed by many other great Arts and experiences like perfect Perspective, Astronomy, Cosmography, the Natural Philosophy of 4 Elements, the Art of Graduation, a good understanding in Music, and moreover, another great Art, hereafter following, though I set this before for some considerations moving me. You see, these Arts furnish stuff to help make this rare and secret Art, but it is worthy enough on its own that deductive, logical conclusions can be drawn from it. The many and continuous travails of the most ancient and wise Philosophers in the practice of this Art and the examples of effects which confirm their works has provided sufficient proof and evidence, which we also may perceive everyday.

A man's body and all other Elemental bodies are altered, disposed, ordered, pleased and displeased by the Influential working of the Sun, Moon, and other Stars and Planets.

Thus, Aristotle writes in Chapter Two of his Meteorological books:
"Est autem necessario Mundus iste, supernis lationibus fere coninuus. Ut, inde, viseius universa regatur. Ea siquidem Causa prima putanda omnibut est, unde motue principium existit., "
"Because this Elemental World is, by necessity, adjoining or next to that of the heavenly motions, these motions govern all its virtue and strength. The heavenly motions are the First Cause of Everything and thus the beginning of all motion."

Aristotle also writes in Chapter Ten: "Oportet igitur \& horum principia sumamus, \& causas omnium similiter. Principium igitur ut movens, pracipuuma \& omnium primum, Circulus ille est, in quo manifeste Solis latio."
["It is necessary, therefore, that we take up both the beginnings and and the causes of all these things. Therefore, the special and first moving principle is the Circle, which is the way the Sun conducts himself."]

His Meteorological books are full of arguments and demonstrations of the effect, virtue, operation, and power of the heavenly bodies have on the four Elements and other bodies which are made from the Elements, either perfectly or imperfectly.

And in Book Two, Chapter Ten of De Generation \& Corruptione ["On Generation and Corruption" or "On Creation and Destruction"]:
"Quocirca \& prima latio, Ortus \& Interitus causa non est: Sed obliqui Circuli latio: ea nama \& continua est, \& duobus motibut fit."

In English this means: "The uppermost motion is not the cause of Generation and Corruption. The motion of the Zodiac is, because it is both continuous and is caused by two motions."

And in Book Two, Chapter Two of his Physics: "Homa nama, generat hominem, ata Sol."
He says: "For Man and the Sun are the cause of man's generation."
Numerous authorities can be cited from Antiquity (1000, 2000, and even 3000 years ago). These great Philosophers, Expert, Wise and godly men have come to the same conclusion which, daily and hourly we men may discern and perceive by sense and reason.

According to Aristotle, all Beasts feel and demonstrate (by their actions and passions, both outwardly and inwardly), and all Plants, Herbs, Trees, Flowers, Fruits, and all things composed of the Elements give Testimony that: Whole Dispositions, virtues, and natural motions depend on the Activity of the heavenly motions and Influences.

The perfect and cautiously observant Astrologer has to conclude that the heavenly Impression is responsible for the specific order and form of every seed and the Individual Matrix of things produced in Nature.

In the end, this conclusion can be drawn not only using reason, but by Natural and Mathematical demonstration.

I have here expressed which Sciences are requisite (without exception) to the Art of Astrology. In my Propaedeumata Aphoristica (among other matters disclosed there) I have provided Mathematical demonstration of the whole Method. I have not seen or heard of it so carefully explained by anyone before.

Twenty-one years ago I was provoked by certain earnest disputations of the Learned Gerard Mercator and Antonius Gogava (and others) to make my own diligent observations of Heavenly Influences down to the precise Minute of time (driven by my own constant and invincible zeal for the truth).

Directed chiefly by the Supernatural influence of the Star of Jacob, [metaphor for Jesus; referring to the star that guided the 3 Wise Men] any Modest and Sober Student also carefully and diligently seeking the Truth will both find and confess there is Verity in my words. He might also become a Reasonable Reformer to help three sorts of People from greatly erring from the truth about these Influential Operations.

The first are the Light Believers, the second are the Light Despisers and the third are the

## Light Practicers.

The first and most common Sort think that the Stars in Heaven can answer any question or fulfill any desire.

The Second sort deny that Influential virtue from heavenly bodies can bear any sway in Generation and Corruption in this Elemental world. Because the Sun, Moon and Stars (being so plentiful, so bright, so wonderfully large, so distant, having so many motions, being so constant in their periods; etc.) they assign them one or two simple characteristics and use the Sun, Moon, or the seven Stars as signs for their businesses here in London or for other such gross purposes of worldly affairs. They do not understand (or will not understand) the other workings and virtues of the Heavenly Sun, Moon and Stars.

They don't understand these virtues the way a Mariner or a Farmer does. They don't even understand them the way an Elephant does, or as a Cynephalus does, [a mythical creature with the head of a dog and the body of a human] or even the way a Porcupine does.

They don't acknowledge that these perfect and incorruptible mighty bodies even has the Radiation and Force of a little magnet, (because these bodies are so distant.)

They think the Sea and Tidal Rivers (like the Thames) just ebb and flow, run in and out by themselves at their own fancy. God help, God help. These men fall short of understanding because they are either too dull, too willfully blind, and in some instances too busy being malicious.

The third Sort is the common, vulgar Astrologer or Light Practicer. Not being skillful or knowledgeable enough, either for vainglory or for personal gain, like a simple dolt or blind Horse (both in matter and in manner) purposefully errs. This sort brings discredit to the Cautious and modest Astrologer, robbing those most noble corporeal Creatures of the Heavens of their Natural Virtue.

These noble Creatures are the most Harmonious in their Monarchy. They are the most mighty and the most beneficial to all elemental Generation, Corruption, and their subsidiary effects.

Properly understood and modestly used, we might highly and continually glorify God and his princely Prophet saying:

The Heavens declare the Glory of God who, in his wisdom, made the Heavens. He made the Sun to have dominion of the day. He made the Moon and Stars to have dominion of the night. Day-to-day he utters talk and night-to-night he declares his knowledge. Praise him. Praise all the Stars. Praise Light. Amen.

## In the

Years
1548 and
1549 in
the Lou-
vain.

Note.
1.
2.
3.

## [The Art of Statike] [weighing things]

Next in order is Statike [Statics or the Science of Weighing things]. I will explain what it means and the commodities that are dependant upon this Art.

Statike is a Mathematical Art which demonstrates the reason for the heaviness and lightness of things, and of motions and properties related to heaviness and lightness.

Because the Balance is the chief instrument used, we call this Art Statike or the Experiments of the Balance. Oh, if a man became an able examiner and diligent practicer of this Art he would profit in many ways.

O God, who has made weight and Balance by thy Judgement, who has created all things in Number, Weight, and Measure, who has weighed the mountains and hills in a Balance, who has measured both Heaven and Earth in their hand, only you know all things precisely. Thus, we who have been informed by the sacred word to consider thy Creatures, might catch a glimpse or perceive but a shadow of the fact that you have revealed in these Creatures your wisdom, might, and infinite goodness.

We should be aware that in your merciful goodness you have used three principal ways in the Creation of all your Creatures, namely Number, Weight, and Measure.

As the two Arts of Number and Measure (the most famous, ancient and most essential to human use) are already well known, we beseech you (through your accustomed goodness) that we may obtain sufficient knowledge of this third key, Weight. You have purposely used these three as Servants of your workmanship.

To glorify your name we should demonstrate (to the weaklings in faith) your wondrous wisdom and Goodness. Amen.

To you my goodly friend, you Gentle and zealous Student, do not marvel at my devoted enthusiasm. Perhaps someday you will perceive what has caused me to feel this way. Now I will give you some ground and show specific benefits of using this Art. Because this Art is rare and my words seem dark and obscure, I will hold a light before the matter by showing you a few principal Conclusions demonstrated by Archimedes:

Conclusion 1.
At rest, the surface of all Liquid is spherical.
All liquid surfaces have the same center - the center of the Earth.
Conclusion 2.
If a solid shape is placed in a quantity of Liquid that is of the same size and weight, it will settle downwards so none of it will be above the surface of the Liquid, but it will still float within the Liquid.

Conclusion 3.
A solid shape, which is lighter than the Liquid, it will only partially sink in the Liquid.
The weight of the Liquid it displaces is equal to the weight of the Solid shape.

## Conclusion 4.

If this (Lighter than the Liquid) solid shape is forced down into the Liquid, it will try to move upwards with a force proportional to that difference in weight.

Conclusion 5.
If a solid shape is heavier than a liquid it will fully sink and
displace an equivalent weight of the Liquid.
Conclusion 6.
If a Solid shape is lighter than a Liquid, it displaces only the amount of Liquid equal to its weight. The amount it sinks is proportional to the difference in weight.

Great errors in the judgment of the Natural Motions of Light things and Heavy things can be corrected by using these Truths. These errors are common among men who are too trusting of false Authority and misguided suppositions, for example: Given two bodies, the heavier moves downward faster than the lighter.

This error was first noticed not by me, but by Giovanni Battista Benedetti [Italian physicist, 1530-1590]. Though it seems like a paradox, this is one of his main propositions: Two bodies of the same shape will move at the same rate whether they are equal or equal in weight. This holds true if both are in air, both are in water, or both are in something similar.

Good discourses written on the feat of Gunning [trajectory of cannonballs] explore this principle, but due somewhat to the imperfection of Nature, it is challenging to demonstrate. These principles are widely used to determine the natural weights (of parts or of the whole) of Air, Water, Earth and Fire. The same principles also apply to Compounds of those Elements. They also apply to the proportions of the Humors in Man, their weights and the weight of man's bones, flesh, and etc. They can be used in many ways to determine the Force or strength of man.

You may also use these principles to determine how much a ship weighs or how much water it draws, in either the sea or in fresh water. And (lifting your head aloft) you can measure the Diameters of the Sun and Moon by weight as precisely as by using any instrument.

Friend, I pray you, weigh those things with the just Balance of Reason and you will find Marvels upon Marvels. One Drop of Truth in Natural Philosophy is worth more than a whole library of Opinions, which can neither be demonstrated nor do they answer to Natures Law or your own experience

This can also be used to find weight proportions of nonrectilinear shapes, like spheres.

Others have noted this Common Error

A paradox
N.T.
[Nicolo
Tartaglia]
The won-
derful use of these propositions.

## [the Mathematics of weight, using a balance scale]

To learn the proportion between a Cube and Sphere using the practice of Statics.
J.D.

Thus you
have 256
perts of a
grain.

* the proportion of a Squaare to a Circle inscribed within it.


## * The squar-

 ing of the Circle, Mechanically* To generate a Circle equal to any given Square.

To complete this chapter on Statics, I will provide you with two or three practical applications. First we'll study the Mathematics of weight, using a Mechanician's instrument.

With the same Uniform substance, make a Cube and a Sphere. Make the side of the Cube equal to the Diameter of the Sphere. You can make them out of Wood, Copper, Tin, Lead or Silver as long as the stuff is consistently heavy. For the Balance Scale prepare a large number of small weights. So you can accurately measure up to six, eight, or twelve pounds objects. Know how many of your smallest weights it takes to counter balance these objects on the Balance Scale.

If you can't make the weights with precision, you may use clean sand. By continuously halving the sand, you will arrive at your smallest weight. (If you are using a pinch of sand as your first measurement, be sure to test your method). The Venetians use a method of halving 256 parts eight times [128, 64, 32, 16, 8, 4, 2, 1].

You will find that the cube and sphere are not of equal weight. Weigh the Cube and the Sphere separately using your small weights. You will find them to be in the proportion of 21:11. This you can see how the Mechanician or Experimenter can understand the proportion of the Cube to the Sphere without any knowledge of Geometry (which I demonstrate at the end of the twelfth book of Euclid).

After repeating your tests for confirmation, change the sizes of the Cube and Sphere until you have made a perfect universal Experience of the proportion. It's possible that you can find a ratio even more precise than 21:11.

Once you have found this Drop of Natural verity, test it with other shapes. For example, make a solid Cylinder whose height and base diameter of a Solid Sphere. The ratio of the volumes of the Cylinder to Sphere is Sesqualiter or the ration of 3 to 2. Add to the Sphere another half of its weight and you will have the weight of the Cylinder.

As they are both in specific proportions to the Sphere, we can now compare the volumes of the Cylinder and the Cube. The Base of the Cylinder is a circle inscribed in the square base of the Cube. As the Cube and Cylinder are the same height, their volumes are in the same proportion that the square base is to the circular base. Now we can use Archimedes's great secret, which he deduced through practical Experimentation and great labor of mind.

Given any Circle, you can find a Square of equal size. Conversely, given any square, you can find an equal-sized Circle. This principle is the Squaring of the Circle.

I have provided an in-depth explanation in my Annotation to the Twelfth Book of Euclid. Through diligence you will find the proportion of a square to the circle inscribed within it to be 14:11.

Using this proportion you can now determine the ratio of the Cube to the Sphere.
We can also demonstrate this mechanically. Make a square of Gold or Silver plate and weigh it. Inscribe a circle in the square, then cut it out, filing the edges to precision. You will find ratio of the weight of the Square to the weight of the Circle to be $14: 11$.

As you can see, we can Square the Circle without even knowing the proportion of the Circumference to the Diameter [which is pi, 3.1416]. (Many have encumbered themselves superfluously be approaching that problem first which is not only intricate, but quite unnecessary).

There are many ways you can easily determine the Circumference once a circle's Quantity is known. I leave you to study this independently so we can move on to another Magistral Problem, which to this day has never been presented better than this:

## The Mechanical Doubling of the Cube, by conerting the solid cube's weight itno a liquid (water)

Make a 4-sided pyramid out of 4 equal isosceles triangles made from copper or tin. Make it as geometrically perfect as you can, and leave the base open. A cone might also be used instead of a pyramid .


Inscribe marks dividing the height of the pyramid using different increments. Divide one internal face into 12 equal parts, another into 24 parts, another into 60 parts and the last into 100 parts.

With its vertex pointing exactly downward, build a frame to steady the pyramid.
Now we will see how to calculate double the volume of a given Cube. Make a perfect Cube out of Copper, Silver, Lead, Tin, Wood, Stone, or Bone. (Make it small enough so that 3 or 4 of them can fit inside the hollow pyramid).

Put the cube on a scale and balance it with an equal weight of water. Then pour that water into the hollow Pyramid. Note the measurement of the surface of the water. Repeat the process make note of the new level of the water.

Next divide the side of the cube into as many equal parts as you can. Now we can mathematically double the cube.

The ratio of the first water level mark to the second water level mark is equivalent to the ratio of the cube to a cube double of its size. To the ratio of the side of the original cube to the side of a cube double its size in volume. (This is proven by Proposition Twelve, Book Six of Euclid).

To Double the Cube by Mechanical Art and with Mathematical Demonstration
J.D.

The sides of this Pyramid must be 4 equal Isosceles Triangles.

## Note

Squaring the Circle without even knowing the proportion between a Circumference and a Diameter.
J.D.

Remember, in for some measurements you must empty the water from the Pyramid first.

Vitruvius, Book Nine, Chapter Three

God be thanked for this Invention and the ensuing fruits.

Note concerning the spherical surface of "، water. '"

Now that we know the length of the side of that double cube, we can find its volume by cubing that length. Thus, I exclaim with joy, "EUREKA, EUREKA, EUREKA." I have have an even greater reason to thank the holy and glorious Trinity than Archimedes had after discovering the fraud in King Heiron's Crown of Gold.

To perform this same test without using a balance scale and weight, make your cube hollow (but water tight). Fill it with water and pour that into the hollow pyramid. Repeat that process. Then use the mathematics just shown to find the volume of the double cube.

Meanwhile, I have not forgotten my first Proposition in the Art of Statistics, that the surface of water is Spherical. To account for this, add a hair's width more to your measurement of the top surface of the water.

To be extremely accurate you could mathematically calculate the swelling of the water above level by finding the distance between the top of the water and the center of the earth. Knowing the width of the swell, you can use mathematics [The Pythagorean Theorem] to determine the height of the swell. Though the swelling is very real, its effect on your calculations will be insignificant. To further lessen the effect of swelling, moisten (with a sponge) the interior sides of the hollow Pyramid before conducting your tests. Experience will guide.

Using this process, you can double the Cube Mechanically, or even triple it (or more).

Now I will lessen your pain, cost, and care by showing you a simple method that does not involve using a Fundamental Cube as a unit of measurement. (That method served as a good demonstration, but it was not the shortest route.)

Take any amount of water (that will fit in the device with plenty of room to spare) and precisely weigh it.Then pour it into the inverted pyramid and make a note if its level.

Repeat that process with the exact same amount of water and make a note of the new level.

These two marks give you the proportion between the sides of two cubes, one of which is twice the volume of the other. (*Thus we can have doubled the the volume of any cube without having to use a given, Fundamental Cube)

Proceeding with our drop of Natural truth, we can now find the proportion of the volumes of two differently sized cubes, whether that proportion is Rational or Irrational.

## 31 (c.iij.)

Make a tall Parallelipipedon [paral-
lelepipeded, essentially a rectangular box] out of Copper or Tin, again with an open top. Make a scale of equal increments dividing the height of the interior of the box.


For Cubes
in any
proportion,
Rational or
Irrational.
" given cubes.

Pour water into the metal box up to the first mark. Then transfer that water to the hollow Pyramid (from the first experiment). Make note of the height, but this time, we empty* the water.

Pour water into the metal box up to the height of the second mark, and again transfer this water into the hollow Pyramid.

Now, in the hollow Pyramid, the ratio of the first level to the second level is the proportion of the sides of any two cubes, which have volume of the original given proportion, whether it was Rational or Irrational.

Thus, there are various ways to provide much-needed information. Even though it is done Mechanically, it can be proven Mathematically.

For example, let's take as a given, two cones whose heights are proportional to each other. As the volume of a cone is 3 times the area of a base times its height, the volumes of the 2 cones are in the same proportion to each other that their sides are.

Returning to the hollow Pyramid in the previous experiment, recall the two watermarks that showed the proportion of the volumes of two Cubes. From water level 2, draw a third line in the hollow pyramid in the same proportion that water level 1 is from water level 2 . Then draw a fourth line that is in the same proportion from the third line.

Because these various depths are in a continuous progression, the various volumes will be in proportion as well*.
*By Proposition 33, Book II of Euclid.
*Note this
Corollary.
*The great Commodity of these new Inventions
*This same proportioning that applies that applies to two cones can als be applied to two square-based pyramids, or even to two parallelipedons [like the tall rectangular containers of the previous experiment].

Furthermore, this demonstration applies to a certain shapes besides square-based Pyramids or Cones. Consider this well.
[Dee might be implying a 5 -sided pyramid or a 6 -sided pyramid, (etc.), but its more likely he's hinting at a 3-sided pyramid (plus base), in other words a tetrahedron. As a cuboctahedron is made out of tetrahedra and square-based pyramids, this same proportioning method works with variously sized cuboctahedra].

I have been very long in words both Mathematically and Mechanically, but I trust it was not too tedious to those who find this information relevant to their work. To avoid prolixity I have omitted various things which could be easily explored which to the Mathmetician would be a great Treasure and to the Mechanician of great commodity.
*You have now learned how to find two middle proportionals between two given lines in a hollow Parallelipedon, a hollow Pyramid or a hollow Cone.

In a rectangular Parallelipipedon, each corner is formed from 3 perpendicular edges or lines. Given a specific proportion of those 3 lines, similarly proportional rectangular Parallelipipedons can be found. (I have elaborated on this following Proposition 36 in Book II in Euclid).

Now, we can easily perform all those things that Vitruvius claims in his On Architecture can be done, like doubling the Cube or finding the two middle proportional lines between two given lines.

Now, that Problem which I explain in my Addition to Proposition 34 of Book II of Euclid is proven to be possible: Any regular body can be Transformed into another.

Now, any sphere or any Mixed Solid or any Irregular Solid may be made in any given proportion to a first, given body.

Thus, from a Mannequin (as the Dutch Painters call it) a Giant can be made having the same symmetry. The Mannequin can have any gesture and the Giant will have the same gesture (and viceversa).

Now, from any Mold or Model of a Ship, you can make a similar mold in any give proportion either larger or smaller.

Now from any *Gun or small piece of ordinance you can make another (with the same symmetry in all points) as large or as small as you want. Think about how useful this can be.

There are an infinite number of ways you can apply this principle which has been sought for so long, so simply presented, and so willingly and frankly communicated to those who faithfully deal with virtuous studies.

Thus the Mathematical mind can deal Speculatively in its own Art (and by good means) mount above the clouds and stars. Also, it can Descend to frame Natural things to wonderful uses. Whenever he wishes, man can return home to his own Center and there prepare more Means with which to Ascend or Descend (all to the glory of God and our honest enjoyment here on earth).

Though the Printer has been asking for the Preface for a day or two, I could not bring my pen from the paper before I had given you a brief compilation of some of the commodities that are able to be reaped using the Art of Statike.

For the remaining Arts, therefore, I will be brief. The next Art is an endless Treasure. I could write about it fruitfully for a whole year, however I will glance over it with but a few words.

## [The Art of Anthropography] [Man]

This is a restored Art, quite worthy of my commendation, which I call Anthropography. I pray you, think of it as one of the chief points of Human Knowledge. Though my name for it is new, the subject has been examined by all perfect Philosophers from the beginning.

Anthropography is the description of the Number, Measure, Weight, Figure, Location and Color of the many varied things contained in the perfect body of a MAN. It incorporates the certain knowledge of the symmetry, figure, weight, Character, and due local motion of any part of the given body and of the Numbers that pertain to these parts.

The final phrase in this Definition helps explain why it is considered a Mathematical Art. The description of the heavenly part of the world is called Astronomy. The description of the earthly Globe is called Geography.

The matching of both is called Cosmography, (the description of the whole and universal frame of the world). So why shouldn't the description of he who is in the Microcosmos or the Lesser World, (for whose sake and service all other bodily creatures were created, who participates with Spirits and Angels, and is made to the Image and similitude of God) have its own special Art? Instead of going unnamed or given a base and improper name like Microcosmology, it should be honored as the Art of Arts.

Depending on your profession you may wish to examine particular parts of this Art, as God, Nature, Reason and Experience shall guide your interests. The Anatomists will teach you part of this Art. Physiognomists [those who judge character from features of the face] will teach you another part.
Chyromantics [those who read palms] will teach another. Metaposcopists [those who find a dominant quality of various bodies, quick as a dog, slow like the pig, forceful like a lion, etc.] will teach yet another part.

The excellent Albrecht Dürer helps explain much about the Eye, which is a substantial part of the Art of Perspective. Pythagoras, Hippocrates, Plato, Galen, Meletius and many others contribute to our understanding of other parts. To study what's left, the Heaven, Earth and all other Creatures offer their Harmonious service. Using your own Experience, perhaps you can Methodically explore the whole, for the sake of posterity.

There is good proof of our Harmonious and Microcosmical constitution. The Art of Zography (Painting and Sculpture) gives view of its outward Image.

To build man's Churches, Houses, Forts and Ships, the Art of Architecture is most necessary and profitable. Anthropology is the chief base and foundation of these Architectural structures

If you don't believe me, simply look at of *Vitruvius
[Chapter 1, Book 3 is entitled On Symmetry: In Temples and in the Human Body].
Look at Albrect Dürer's On the Symmetry of the Human Body.
Look in the 27th and 28th Chapters of Book Two of Agrippa's On Occult Philosophy
[entitled Of the Proportion, Measure and Harmony of Man's Body; and of the Composition and Harmony of the Human Soul].

Consider Noah's Ark.
And go even further. Remember the Delphic Oracle NOSCE TEIPSUM (Know Thyself) pronounced so long ago and so often repeated by many a Philosopher, and strived at by the Wisest.

Now you may perceive that these voices from so long ago are calling to you the School where this Art might be learned.

MAN
is the
Lesser
World
[the
Micro-
cosm]

I am not afraid of the distain of those who believe there are only Seven Arts and Sciences. Some, with enough ignorance and shame don't even say there are seven. Nobody can really say there are a certain number of Arts. And within each Art there are no limits to God, Nature, and Man's Inventiveness.

Every day New Arts are born. All the Arts of the world will never be known to one man, or in one land or even in one age. Let us embrace the gifts of God and the paths to wisdom in this time of grace from above which is continually bestowed on those who thankfully receive them. All goodness overflows with more goodness.

## [The Art of Trochilike] [circular motion]

Trochilike, is that Mathematical Art which demonstrates the properties of all Circular motions, both Simple and Compound. Because the most basic functional use of circular motion is the wheel, it is called Trochilike, or as one might say, Wheel Art. In this Art a given Wheel can move others in many different ways. Two wheels can turn at the same rate, or in any given proportion.

A Wheel can describe a straight line. Also, it can describe a spiral line, an ellipse of a Conical Section, and many other Irregular kinds of lines. These geometric principles are utilized in many pleasant and profitable Mechanical works.

I have seen Mills in Germany that saw extremely long boards with no manpower involved. In the City of Prague, in the Kingdom of Bohemia I have seen Mills for making coins and Mills for grinding corn. Mills and Wheelworks can be powered in many ways, by Wind, Smoke, Water, Weight, Spring, or by Man or Beast.

Read Georg Agricola's book, On the Nature of Metals, and you will see how essential Wheelwork is in Mining operations. Strange works have already been made using Wheels, and even more incredible inventions will be made in the future. One wonderful current-day example that will certainly be elaborated on is a clock which the Inventor [William Zenlander, in the 1300's] sold for a mere 20 Talents of Gold. It was accidentally broken, but was repaired by Janellus of Cremona [in the 1500 's] and presented to Emperor Charles V. Geralmo Cardano testifies that one of its gears moved at such a slow rate it would take 7000 years to make a circuit - an almost unbelievable thing.

Many men, some still living, could testify that what I speak of is not that unusual.

## [The Art of Heliocosophy] [spirals]

Helicosophy is a close sister to Trochilike. It is a Mathematical Art which demonstrates the designing of all Spiral lines on a Plane, Cylinder, Cone, Sphere, Conoid, or Spheroid, and all the properties pertaining to them. This art is most useful in Architecture and in the design of various Instruments and Machines. In many instances, a Screw does what nothing else can do.

Athenaeus writes in Chapter 8, Book 5 [of Diephosophists, or Banquet of the Learned, around 225 $\mathrm{AD}]$, that all the manpower in the city of Syracuse could not move a huge Ship that was grounded, but Archimedes set up his Screw machine and King Hieron was able to operate it and remove the boat with ease. According to Proclus (page 18), the king was so struck by the wonder of it all he declared, "From this day forward, whatever Archimedes says is to be believed."

## [The Art of Pneumatithmy] [air or water pressure]

Pneumatithmy demonstrates by using enclosed hollow Geometrical shapes (either regular or irregular) the strange properties (either in motions or at rest) of Water, Air, Smoke and Fire (either separately or together).

The Natural Philospher can use this art to prove that there is no Emptiness in this world. Nature abhors a vacuum so much that, contrary to ordinary laws, Elements can be caused to move (or to stand still) [as in a straw]. If there is more space than there is air to fill it, water can be caused to ascend. Similarly, water can be caused to hang, and not descend, rather than leave behind emptiness. The same is true of Fire and Air. They will descend either when their Continuity has been dissolved or when they are forced by another Element. They cannot be extended to discontinuity nor can they be compressed or pent up in a space insufficient to hold their bodily substance, even using the force of man. They will use great force and violence to enjoy their natural right and liberty.

As a practical example, by keeping air in an inverted Cauldron, several men can descend to the bottom of the Sea and remain there for a while. Note that a thicker Element (like the Water) will relinquish its place to a thinner Element (like the Air) when it receives its violent force.

Pumps, all kinds of Bellows, and many other strange devices are based upon this Art. Many goodly works in Greek and Latin describe Hydraulic Organs that operated by water, a science commonly called Pneumatica [pneumo means "wind"].

What I call Pneumatithmy, the old and learned Scholars called Scientia de Pleno \& Vacuo [the Science of Matter and Void].

## [The Art of Menadry] [multiplying of a force]

Menadry is a Mathematical Art, which demonstrates how a Virtue or force can be multiplied so it can push, pull, lift or cast off a virtue weight or force, which is not naturally directable or moveable. [Menadrie is a term apparently coined by Dee]

Often this art is used in conjunction with other Arts like Perspective, Static, Trochilike, Heliocosophy, and Pnematithmy. Cranes, Gibbets and Machines use this Art to lift or force things in a variety of ways. The cause of this force is well-known.

The Dutch Rack uses this force allowing one man to upright a large, full wagon lying on its side. A Crossbow uses this force. It is the reason why one man with a lever can lift what six men couldn't lift using their hands. We have Cranes right here in London that can lift 2000 pounds of weight, with the help of two pulleys (properly arranged). It is estimated that a large enough crane can lift up to 200,000 pounds of weight.

Archimedes knew this Art so well that several times, single handedly, with his devices and machines, ravaged and utterly defeated an entire battle array of the Roman Army (led by the Supreme Roman Consul Marcus Marcellus), which had been besieging Syracuse. With his machines he rained so many huge stones on them that they were driven far away from the city. And likewise he hurled mighty stones at the ships that had come up to the walls of Syracuse, utterly confounding the Roman Navy. He was able to project 18 foot pikes almost a quarter of a mile*.

To go to the bottom of the Sea without danger.
*These things are written about in Plutarch's Marco Marcello, Synesius' Epistolis Polybius, as well as in Pliny, Quintilian, Titus Livius, and Athenaus

He devised a way to catch hold of the ships, hoist them above the water and suddenly
*Galen and Anthemius write about this. drop them into the Sea again. He used *Burning Glasses to set fire to distant Ships. For months the Romans were repelled from Syracuse. All their force, courage, and tactics couldn't contend with his devices and engines. The Romans gave Archimedesthe name Briareus or Centimanus [, the Greek and Latin terms (respectively) for a mythological giant having 100 arms].

Zonaras says that Proclus understood Archimedes'Art of Menadry so well that he devised large Burning Glasses. Placing them on the walls of Constantinople, he multiplied the heat of the Sun and directed the beams against the enemy Navy with such force that he set them ablaze (like lightening) destroying the ships and all the men.

Dion writes about a Geometer from Constantinople named Priscus who invented and uses a variety of machines using multiplied Force. Even though Emperor Severus conquered the city, he pardoned Priscus because he honored his Art, cleverness and skill.

Just as important as these machines of Force was the invention of the Gun. Though first " invented in another land, an Englishman refined its design. He who has studied the history of
Guns " Guns is amazed how such a small, common thing (devised by wise men and handled by indus-
" trious men) could have such incredible force.

## [The Art of Hypogeiody] [tunnels]

Hypogeiody [hypo means under, geo means earth] is a Mathematical Art that demonstrates how tunnels can be planned and dug under the Spherical Surface of the Earth (at any depth) to end up under a specific remote location (if the distance and compass direction is known). This Art explains how a tunnel direction can follow a given track beneath the surface of the earth. And conversely, how an existing tunnel (straight or crooked) can be tracked from on the earth's surface.

This Art is very profitable to the Commonwealth in various ways. I invented this Art at the request of two Gentlemen. They both owned mines near the border of their lands. Because the tunnels were crooked and at various depths, they couldn't determine on whose property the tunnels were actually located. Upon settling their dispute I published a book entitled, De Itinere Subterraneo [On Travel Underground].

The rest is at God's Will. For foot soldiers who dig trenches, for miners digging for Metal, Stone, or Coal, for those digging for secret underground passages from place to place (and our country has many) and for other purposes, anyone can easily see the benefit of this Art. One can also see how much knowledge of Geometry helps in this Art of Hypogeidy.

## The Art of Hydragogy [water flow]

Hydragogy [hydra means "water"] demonstrates the possible ways of directing the flow of Water by Nature's Law [gravity] or by artificial means from any source (a Spring, Running Water, or Standing Water) to any other given location.

Marvelous works using this art have been made for a long time. Not only are they well documented, but their Ruins can be seen today, like the Roman Aqueducts in Italy. In other places Canals leading through the Mainland are Navigable for many miles. In other places, water is forced to Ascend.

Directing water in all these various ways demands great skill of anyone who is to be perfect in this Art. I won't get into details of how much Fall is required for every hundred feet of distance nor of how ventils [man-made sluiceways] should be designed to handle an overflow of too much water.

There are many experts who build waterways, without properly understanding the Geometry involved. Thus, they couldn't easily choose the optimum course leading from a high spring, crookedly down and around (and even over other high areas) to the final low destination. Geometry therefore is essential to Hydrogogy.

Vitruvius, Agricola, (and others) write extensively on the various ways to force water to ascend like a Tympane mill or a Kettle mill [types of windmills that pump water], the Archimedian Screw, or Ctesibius' water pump. [Ctesibius also invented the clepsydra or water clock (see Vitruvius, Book 10, Chapters 4-7); The Tower of the Winds in Athens was based on his design (see Vitruvius, Book 1, Chapter 6)].

So, its quite evident how the Arts of Pneumatithmy, Helicosophy, Static, Trochilike, and Menadry aid the art of Hydrogogy, and also how useful it is to the Commonwealth.

## [The Art of Horometry] [time]

Horometry is a Mathematical Art which demonstrates how, for any given location, the exact designation of time may be known. This definition sounds simiple, but is has much deeper meaning than you might imagine. In antiquity, part of this Art was called Gnomonice. More recently it was called Horologiographia. And in English, it is called Dialing.

Ancient is the use, and more ancient is the Invention. Its use appears at least 2300 years ago when King Achaz invented a dial that worked by the Sun during the day and the Moon and Stars at night.

To graphically design various kinds of Dials requires not just skill in Astronomy, but also Elemental, Spherical, Phenomenal (observational), and Comical Geometry.

It takes more than a talented Painter to prescribe the path of the Sun's shadow, (down to a hair's-width) for any regular surface in any given location. In my youth, I invented a way to accomplish this feat of determining how, using any Horizontal Dial, Mural Dial [wall dial or vertical dial] or Equinoctial Dial [tilted dial], at any given hour (provided the Sun is shining), to determine the Sign and Degree ascendant. These things are essential to predict the Rising of those fixed Stars whose Influence is mighty. But I won't delve into that here.

Man's affairs often require knowledge of Time at Moments when neither the Sun, Moon, or Stars can be seen. So industrious Mechanics invented a way to keep track of time using a consistent flow of Water. Vitruvius rightfully praises to the skies the famous Inventor Ctesibius. Later, hours were measured by running Sand. Then, using the Art of Trochilike, by weights. And lately by Trochilike without weights, using a Spring instead.

But all these methods require corrections over time not only because of the heavenly Equinoctial Motion [the Great Year], but also because of the inaccuracy of their own Operation.

There remains (and I'm not speaking figuratively here) among the Philosophers, a more excellent, more commodious and more marvelous way than all these to Imitate the motion of the Primovant (or the first equinoctial motion) by using Nature and Art, which you shall understand more of by further search in weightier studies. [Dee seems to be hinting about a camera obscura solar disc sundial here].

And so, it is time to finish this Note about the delineation of Time, for our common and private affairs. Any man that wants to know how to spend his time, needs to know how to tell time.

## [The Art of Zography] [painting from life]

Zography [in Greek, Zoê means life] is a Mathematical Art which teaches and demonstrates how the intersection of all Visual Pyramids, made by any assigned plane (the Center, distance, and lights having been determined), may be represented by lines and proper colors. To explain all the properties and ensuing benefits of this notable Art would really require a whole Book. An expert Zographer must be skilled in Geometry, Arithmetic, Perspective, Anthropography and many other Arts. For the most excellent Painter (who is but the proper Mechanician and sensible Imitator of the Zographer) [Dee is referring to God, the Zographer of the Universe], is so skilled that Man and beast have thought that his paintings were really natural things and not artificial, that they were alive and not dead.

This Mechanical Zographer (commonly called the Painter) is marvelous in his skill and seems to have a certain divine power as he can depict absent friends as present and even give dead friends a continual silent presence not only with us, but with posterity for many Ages. Moving on, Consider how in Winter he can show you the lively view of Summer's Joy and riches. And in Summer exhibit the countenance of Winter's naked and doleful state.

Cities, Towns, Forts, Woods, Armies, indeed even entire Kingdoms (no matter how large or how far away) he can bring home with ease (to any Man's Judgment) as lively patterns. In one little house he can enclose (with great pleasure to the beholders) the lively portraiture of all visible Creatures, either living on earth, or in the earth, or lying in the waters, creeping, sliding, or swimming of any fowl (or even a fly) that is in the Air flying. He can most nearly match the Judgment of our eyes in respect to the Stars, the Sky, the Clouds, indeed even the show of the very light itself (that Divine Creature). What an amazing thing this is. He can represent things that don't event exist yet. In a sense, his Picture seems to have Created them.

To a skilled craftsman, isn't a Picture a great pleasure and useful commodity? Which of these would refuse the Direction and aid of a Picture? To the Architect, the Goldsmith and the Arras [tapestry] Weaver, a picture is extremely valuable. Is it not by Picture that we get great pleasure when we behold books on Herbs and Plants, portraits of birds, beasts, fish and even our own curious Anatomy?

And if Picture (by the skillful work of the Painter) is this commodious and marvelous, what shall we think of Zography, the Schoolmaster of Picture and its chief governor?

Though I don't mention Sculpture in my table of Mathematical Arts, all men can see how Picture and Sculpture are connected like Sisters. And both are extremely profitable in a Commonwealth. Excellent craftsmen have written great books commending both Sculpture and Picture, for example Giorgio Vasari, Pietro Aretino, Pomponius Gauricus and others.

In addition to these two Arts (and others) there is a certain odd Art called Althalmasat. It is much more beholding and useful to his Art than the common Sculptor, Entailer, Carver, Cutter, Engraver, Founder, Painter, (etc.) realizes.
[An Entailer is an Intaglio artist, a Carver makes figurines, a Cutter cuts in wood block, an Engraver engraves in metal more deeply than an Entailer, and a Founder is one who casts metal].

## [The Art of Architecture]

Many might consider it improper to include Architecture among the Mathematical Arts because it An is not worthy enough. To them I will provide good reasons why I dare do so. They might point out that I have defined Mathematical Arts as not dealing with material or corruptible things, but dealing with things which can be expressed using Number and Magnitude. They will claim Architecture unworthy because it deals with such gross, material works like the building of a house, Palace, Church or Fort.

First, remember that I include Architecture among the Mathematical Arts which are Derived from the Principal arts of Arithmetic and Geometry. Realize that some of these arts deal more with Natural things and matter perceptible by the senses, while others draw nearer to Simple and absolute Mathematical Observations.

The Architect prepares, informs and guides the Mechanician who does the actual handiwork of building a house, Castle or Palace. He is also the final Judge in any decisions that must be made. As the chief master, the Architect is responsible for the Demonstrative reason and cause of the Mechanician's work. Working in Line, Plane, and Solid the Architect's work must be solidly based on the principles of Geometry, Arithmetic, Optics, Music, Astronomy, Cosmography -indeed all the Mathematical Arts in this Preface, as well as other Natural Arts.

As it is based on the principles of all these Arts, you can see why it should be include as its own Mathematical Art.

Let's hear from the two men I consider to be the two most perfect Architects:
One is the Roman Vitruvius who wrote On Architecture [ca. 25 BC]. He dedicated the Ten Books in this work to Emperor Augustus who ruled Rome at the time our Heavenly Archmaster [Jesus] was born. The other is Leon Battista Alberti of Florence, who also published Ten Books on Architecture [in 1452].

Vitruvius writes: [in his first sentence of Chapter 1, Book 1]
"Architecture is a science involving many disciplines and various kinds of specialized knowledge. All the work done by the builders is guided by the seasoned judgment of the architect. His expertise grows from practice and reasoning. Reasoning is what declares the final proportions of the work."

Vitruvius continues:
"In all things, but particularly in Architecture, there are two aspects to be considered, the significant and the signifier. The signified is the object spoke about [like a building]. The signifier is the reasoned demonstration based on established principles of knowledge. They are two aspects of the same thing."

Further along in Book 1, Chapter 1, Vitruvius writes:
"An Architect must be familiar with various Languages, skillful in Painting well instructed in Geometry, not ignorant of Perspective, equipped with knowledge of Arithmetic, familiar with History, a diligent student of Philosophy, have skill in Music, be not ignorant of Medicine, understand rules of Law, and have a firm grasp on Astronomy and the courses of Celestial objects."

Vitruvius clearly explains why an Architect must be familiar with all these Arts and disciplines:
"It is important for an Architect to have knowledge of Painting so he can more easily illustrate the work he proposes.

Geometry offers many aids to Architecture. First among them is the use of the Rule and Compass to facilitate drawing the building plans. On-site, this geometry is carried out using squares, levels and plumb lines.

Likewise, by Perspective, the Lights of heaven are well-led in the buildings, from certain quarters of the world.

By Arithmetic, the cost of the building is summed up, the measurements are calculated, and the important issues of Symmetry are resolved using Geometric principles and methods.

It is essential to thoroughly study Philosophy because it deals with many varied natural problems about the "Nature of things," which the Greeks call physiologia.

One example of this is conducting water through Aqueducts. Parts of the course are downhill, but some are level, and some must actually go over high ground. In each of these situations water pressure will vary. Problems like this can only be solved by someone who has learned the natural causes of things by studying Philosophy.

In addition, anyone who has read the books of Ctesibus and Archimedes (or others who have written down such Rules) will not be able to fully appreciate their meaning unless he has been trained in these subjects by the Philosophers.

And an Architect must know Music in order to understand both Regular Music and Mathematical Music. This will help him fine tune the springs of Balists [which shoot heavy darts], Catapults, and Scorpions [a smaller catapult operated by one person].

Likewise, in Theatres, Bronze Vessels are placed in niches beneath the seats using mathematical principles. The Greeks called the echeia.
[êxô means "a returned sound or a ringing sound," from which we get the word echo].
They are distributed in various places throughout the circular Theatre according to the Musical Harmonies of Diatessaron, Diapente, and Diapason.
[The musical fourth, fifth, and octave or the ratios 3:4, 2:3, and 1:2]
The actor's voice, projected from the stage, would be amplified when it strikes these vessels, allowing the audience to hear a richer and more pleasing sound.

As for Astronomy, the Architect must know East, West, South and North, and the design of the heavens, the Equinox, the Solstices, and the course of the stars. Anyone who lacks knowledge of these matters will be unable to understand the Art of Horology.

As this worthy profession is garnished, beautified and stored with many varied skills and fields of knowledge, I do not think that someone can just suddenly proclaim he is an Architect. One must start from childhood and slowly climb the steps of these studies. Only after being trained in Languages, Arts, and Sciences will be able to reach the high Temple of Architecture.

But to those whom Nature has bestowed such ingenuity, skillfulness, and a good Memory that they have mastered Geometry, Astronomy, Music and the other Arts, and who have surmounted and passed the calling and state of Architects can finally become Mathmeticians. Such men are rarely found,

A Mathmetician but here are a few examples from times past: Aristarchus of Samos, Philolaus and Archgas of Tarentum, Appolonius of Perga, Eratosthenes of Cyrene, and Archimedes and Scopinas of Syracuse. Using natural laws and mathematical principles they invented many kinds of Machines and Sundials, which they described in their books for the posterity."

These words (paraphrased in places) can all be found in one chapter in the Ten Books by the Incomparable Architect Vitruvius. [that is, Chapter 1, Book 1] If you were able to take this book in

Vitruvius. your hand and glance through it you would immediately agree: This is a Storehouse of all workmanship. It incorporates the Arts of Geometry, Arithmetic, Astronomy, Music, Anthropography, Hydragogy, Horometry and more.

Now let's listen to our other Judge, the Florentine Leon Battista Alberti, and briefly examine his views on Architecture [in his Prologue to Book 1]:
"Before proceeding, I must describe the man I would consider to be an Architect. As other Arts have Chief Masters, you might think the Carpenter to be the Chief Master of Architecture. But this is not so. The Carpenter is but an Instrument of the Architect.

I consider an Architect to be that man who (by sure and marvelous reason and method) has the skill to devise (using his own mind and Imagination) and accomplish by, the movement of weighty material and the joining and framing together of bodies, that which is most beneficial for the worthiest needs of Man.

To be able to perform these things, he must have an understanding and knowledge of the highest and most worthy disciplines."
[In Book 1, Chapter 1, Alberti continues:] "The whole Feat of Architecture in building consists of Lineaments [its distinctive lines] and Framing [structure]. The whole intent and purpose of Lineaments lies in determining the best way of coordinating and joining all the lines and angles that define all the faces of the building.

The function of the lineaments is to prescribe an appropriate location, precise numbers, proper scale, and elegant order for the whole building as well as for its various parts. Thus the entire form* and appearance of a building may depend upon the Lineaments.

Lineaments have nothing to do with the particular material the building is made from. Building made from different materials can have the same lineaments if they share similar siting, order, and all the lines and angles are similar.

Thus, Lineaments are all the precise and correct lines and angles of a building, first conceived in the mind, and then perfected by inspired vision and learned intellect."

We thank you, Master Alberti. By setting aside the material stuff of the building, you have appropriately given your Art (and your description of it) a Mathematical perfection that involves thinking about order, number, form, figure, and symmetry.

Now, Gentle reader, it is evident why I consider Architecture to have been born and raised in the Dominion of the incomparable Princess Mathematica and to be one of her natural subjects. The word "Architecture" itself helps describe what distinguishes this Science from all the other Arts.

As Plato affirms, the Architect is the Master of all other workers. He is neither a Smith or a Builder or any other Craftsman. He is the Head, the Provost, the Director, and the Judge of all Artificial works and of all Artificers. The true Architect is able to teach, demonstrate, administer, describe, and Judge all works made. And only he searches out the causes and reasons of all Artificial things.

Thus, Architecture is so excellent that, in our days, few endeavor to undertake it. But it should only be thought of as a virtuous pursuit.

Just because we have scarce few Artificers these days doesn't mean we should imperfectly redefine the ancient Arts anymore than we should pinch in the Definition of Wisdom, Honesty, Friendship, or Justice. No more will I consent to Diminish, in anyway, the perfection and legitimate dignity given to absolute Architecture.

Under the direction of this Art are three important Mechanical Arts, Housing, Fortification, and Naupegie [ship building].

Housing incorporates buildings made for Divine Service and for Man's common usage, whether public or private.

Strange matters might also be explained about Fortification and Naupegie. But perchance some will be weary of all this Bede-Roll [lengthy listing or cataloging]. Others might prefer I nicely nip my bulky and unrefined discoursing with you, made in post-haste. I wouldn't want you to lose interest in this true and friendly sampling of Mathematical Power. Life is short and uncertain. Times are perilous. And the Printer is waiting for my pen to stop. So let,s proceed to the remaining Arts with all speed possible.

## The Art of Navigation

The Art of Navigation demonstrates how a seaworthy ship may be conducted between any two given places by the shortest route and in the shortest amount of time. And, in the instance of storms and natural disturbances, the best possible revised route.

It is obvious that the Master Pilot requires knowledge of the Arts of Hydrography, Astronomy, Astrology, and Horometry, as well as the common Base and foundation of all Arts, Arithmetic and Geometry.

Thus he will be able to read the necessary Instruments, whether he has constructed them himself or they have been skillfully crafted by experts. He should be able to use the following:

> The Quadrant, The Astronomer's Ring, The Astronomer's Staff,
> The Universal Astrolobe, A Hydrographical Globe, Hydrographical Charts
> (true ones, not those with longitude lines that are parallel)
> The Common Sea Compass, The Compass of Variation
> The Proportional and Paradoxical Compasses
> (which I invented* at the request of two Master Pilots of the Muscovy Company) Clocks with springs
> Hour, Half-hour, and Three-hour Sandglasses and various other Instruments

He should learn the different ways the Paradoxical Compass can be used on a Globe or a flat map and also to be able to Calculate the Positions of the Planets at any given time.

In addition, he should know the exact Longitude and Latitude of his port of departure so when he pinpoints his existing location, he can keep a record of it in his ship's logbook.

By observing certain tempestuous fixed Stars, (and their Conjunctions, and their angular relationships with the Planets), and where these fixed Stars rise set (and their locations at Noon and Midnight) he should be able to predict Storms, Tempests, Waterspouts, and other Meteorlogical effects that are dangerous at Sea. For, as Plato says, the ability to change course when the times warrant is no less important in the Art of War than it is in Husbandry and Navigation.

Besides all these clever techniques, the Navigator can look to the Sun and Moon for clues about weather, for example, as Virgil teaches us in Georgics:
"The sun, too, will give signs when rising, And when setting into the waves.
The surest signs are provided by the sun.
Often we see various colors pass across its face.
Dark blue tells or rain; fiery-red means wind from the east.
But if the fiery-red is mingles with spots. Then a riot of storm-clouds and wind is on the way.
Let no man set sail on such a night. Or even untie his ship's ropes from shore.
The sun will show you all these things. So who dare call the sun untrue?"
Likewise, there is great pleasure and profit in seeing certain symathetical forewarnings (both at sea and on land) by carefully observing the Moon, Stars, Water, Air, Fire, Stones, Birds and Beasts.

So by all these examples, it's clear how much the Art of Navigation needs and uses the other Mathematical Arts.

There is no need to elaborate on all the ways this country and others benefit from Ships and Navigation. But I feel obliged to discuss this.

And now, if I was to explain the many all the benefits coming to this Land (and others) because of Ships and Navigation you might think I'm using this occasion to use too many words when its unnecessary. But let me make this one important point:

In Navigation, none ought to take a greater interest to be skillful than our English Pilots. Perhaps many more men would be willing to come to the aid of our country if they had skills in Navigation. What a Privilege God has bestowed upon this Island by Situating it in a location most commodious for Navigation to Places most Famous and Rich.

And though lately* a young Gentlemen and Courageous Captain was in great readiness, and with good hope, and with great motivation to have ventured for a Discovery. Either westerly (by way of Cape de Paramantia) [searching for the North West Passage around the tip of Greenland] or easterly (by way of Nova Zemla and the Cyremisses) [searching for the North East Passage above Russia].

But near his departure date he* was called into the good service of his country, as the Irish Rebels have tasted. [Sir Humphrey Gilbert was still fighting in Ireland in 1569].

If this Gentleman is too engaged to make a voyage of Discovery, someone else should study the matter, listen to my advice, and consider venturing forth themselves.

Little by little we should becoming more knowledge able of the advantages that Trading Voyages can bring. I would be disheartened if, because of through indifference, inadequate Skills and lack of Courage, this opportunity was lost.

Half of the challenge is mustering enthusiasm. The other half is educating people about its wonderful advantages. It would bring great riches and worldly Treasure, mostly to this Land, but also to the rest of the Christian Commonwealth.

## The Art of Thaumaturgike [Wonderworks]

Thaumaturgike is that Mathematical Art which gives certain order to make strange works that can be perceived by the senses but are greatly wondered at by men

These Wonderworks are made in various ways. Some by Pneumatithmie, as in the Works of Ctesibus or Hero [using water pressure or steam pressure]. Some by Weight, as Plato speaks of in Timaeus. Some by the Tension of strings. Some have lively Motions caused by tightly wound Springs. Some by other means, like the Images of Mercury or the brass head sculpted by Albert Magnus, which seemed to speak [around 1250, Albert Magnus made a robotic head that could answer questions].

* In the Year 1551

An Account of Extraordinary Events of this World,
Chapter 8

Tusculan
Disputa-
tions.
Chapter 1

A Digression Apologetical

Cassiodorus [ca. 550 AD ] writes that Boethius was skilled in inventing such devices:
"Your purpose is to know profound things and to show marvels. In the presentation of your Art, you have made Metal burn ablaze. You have made Diomėdes [mythological warrior] out of Brass which blows a loud Trumpet, a Bronze snake that hisses and birds which sing sweetly. These are but a few of the things we remember you for, you who can Imitate the heaven."

At Saint Denys, in Paris*, I (along with Oronce Finé and others) [French mathematician and cartographer 1494-1555] witnessed a strange self-moving several times. Others have written about it, and I hope it is still there to be seen.

Strange things can be done using the Art of Perspective, as I partially explained earlier. For example, to see aloft in the Air the lively Image of another man, either walking to and fro, or standing still. Similarly, to enter a house and see the lively show of Gold, Silver or precious stones, then attempting to grab them with your hand, only to find nothing but Air.

Some men, though wise in other matters, have shamefully overshot themselves by misjudging the means used to create these wonderworks. As Claudius Celestinus writes:
"Nowadays, some Men, even of great learning and reputation, have Judged certain works to be so marvelous that they are above the power of Nature. But anyone skilled in the Art of Perspective could easily have explained the Cause."

Marcus Tillius Cicero, recounts the very strange Sphere designed by Archimedes "When Archimedes fastened the movings of the Sun, Moon and the five other Planets in a Sphere, he made the world, just as the God did (in the Timaéus of Plato). By turning one crank, they all moved at various rates, some slow, some swift."

Even more amazing is that Claudianus reports it was made of Glass.
Angellius writes that the Mathematician Archytas made a Dove out of wood that could actually fly.
Plato writes about strange Images in Dadalus. Homer writes about Vulcan's Selfmovers which moved by means of secret wheels. (Aristotle mentions both of these in his book Politics.)

Much of the workmanship in days long past was simply performed by cleverly using the principles of Trochilike and related Arts. In Nuremburg, a fly made out of Iron, being let out of the Artificer's hand, flew about all the guests at the dinner table. After a while, as though it were weary, it returned to its mater's hand again.

Also an Eagle made from wood flew out from Nuremburg a long distance to salute Emperor Maximillian, then returned again, waiting from him at the city gates.
[Dee's friend Peter Ramus wrote about the Iron Fly and the Wooden Eagle made by Regiomontanus around 1471].
*Thus, you can see that what wonders Mathematical Art can perform when Skill, Will, Industry, and Ability are duly applied to proof.

## [Dee's diatribe against malicious accusers]

For these and similarly marvelous Acts and Feast that are naturally, Mathematically and Mechanically contrived and made, should any honest student and Modest Christian Philosopher be called a Conjurer?

Should the folly of Idiots and the Malice of the scornful prevail over He who seeks no worldly gain or glory from them , but only seeks from God the treasure of heavenly wisdom and knowledge of pure truth.

Should he that seeks (as St. Paul describes it) in Creature's Properties and wonderful virtues to find just cause by which to glorify the Eternal and Almighty Creator be robbed and pillaged of his honest name and fame?

Should that man be (in hugger mugger) [clandestinely] condemned as a Companion of the Hellhounds, or a Caller and Conjurer of wicked and damned Spirits? Some claim they don't have time for all this learning, but its the only way to Godly Wisdom and Truth.

It takes a long time to absorb all the delights of Godly Wisdom and Godly Truth. Do you think such a learned man would waste his time with the Chief enemy of Christ our Redeemer, the deadly foe of mankind, the subtle and shameless perverter of Godly Truth, the Hypocritical Crocodile, the Envious Basilisk [serpent] who continually desires, in the twinkle of an eye, to destroy all Mankind, both in Body and Soul, forever?

Surely (to speak for myself) I have not learned to make so brutish and so wicked a Bargain. I have suffered in many ways in order to attain good Learning and Wisdom. In the past 20-25 years of Study I have spent 2-3 thousand marks, traveled 7-8 thousand miles, in all kinds of weather, using all kinds of transport, early and late, in danger of violence by man, in danger of destruction by wild beasts, in hunger, in thirst, in perilous heat by day, walking on foot in dangerous damps of cold by night, and risked my life by lodging in unsafe places.

Why (I pray you) for all this (safely, by God's mercy) should I have fished with a net so large and costly, and that has taken such a long time to draw up (with the help of Lady Philosophy and Queen Theology), only to catch* a Frog? Nay, only to have caught a Devil? This is what the Common peevish Prattler Imagines and Jangles about. This is what the Malicious scorner says, so brazenly, behind my back. Ah, what a miserable kind of Man this is. He is bold, but blind to the Multitude of things above his Capacity.

What a Land. What a People. What Manners. What kind of times are these? Have these men become Devils themselves? By bearing false witness against their neighbors, will they also become Murderers? Perhaps God has forgiven them for this horrible slandering of the guiltless, but then they continue to do it. Why do the Innocent obtain from enforcing the full extent of the Law?

Why do the Innocent bystanders disregard the Charitable patience of he who has been slandered? Why do they not help enforce the full extent of the Law against these men as they continue to forge, fable, rage, and raise slander in Spoken Word and Print? Do they fear their Names will also be Noted to the World in word and Print with various devices, fables, beastly Imaginations and unchristianlike slanders?

Well, Well, my unkind Countrymen. O unnatural Countrymen. O unthankful Countrymen. O Brainsick, rash, O spiteful and Disdainful Countrymen. Why do you violently oppress me with your slanders, contrary to Truth and contrary to your own Consciences?

In word, deed, or thought have I ever been hurtful, damaging, or injurious to you and yours in any way? I have so long, so dearly, so carefully, so painfully, and so dangerously sought and travailed to learn Wisdom and attain Virtue, and in the end (in your judgment) I am worse than when I began.

Worse than a Madman. A dangerous Member of the Commonwealth. Not a Member of the Church of Christ. You call this Learned? You call this being Philosophers or lovers of Wisdom? To forsake the straight heavenly path and wallow in the broad path of damnation? To forsake the light of heavenly Wisdom and lurk in the dungeon of the Prince of darkness? To forsake the Truth of God and his Creatures? To flatter the Deceiptful, Crafty, Obstinate Liar an continual disgracer of the ultimate power of God's Truth? To forsake Eternal Life and Bliss and cling to the Author of everlasting Death, that Murderous Tyrant who most greedily steals Man's Soul?
*From the proverb, "He had fished well, but caught a Frog."

Well, I thank God and our Lord Jesus Christ for the Comfort I get from the Examples of men who have lived before my time. Though I am unworthy of being compared to them in godliness of life or in perfection of learning, but they sustained the very same (or rather greater) Injuries that I have had to withstand.

Plato's Apology of Socrates (that patient man) will testify to this. The Apology written by Apuleius reveals the Brutishness of the Multitude. Pico de Mirandola's Apology will teach you of the Raging slander of the Malicious Ignorant against him. In Johannes Trithemius' Apology you can read his public Prostetation against the Rude Simple, some of whom were considered to be the wisest sort of men. There are so many more I can't count them all.

I loathe the Foolishness and Malice of my Native Countrymen who cannot digest any extraordinary course in Philosophical Studies that does not fall within the Compass of their Capacity or where they are not made privy to the true and secret cause of such wonderful Philosophical Feats.

These men generally fall into four categories: The first I call Vain prattling busy bodies. The second, Foolish Friends. The third, Imperfectly zealous. And the fourth, Malicious Ignorant. Let me briefly say a word or two to each of these, then I will return to my Preface.

Vain prattling busy bodies: Use your idle assemblies and conferences for something useful instead of talking of matters too difficult for your Capacities or contrary to your Consciences of what you Know is True.

Foolish Friends: Depart, rather than shower someone who is not really your friend with blind affection. Just because he knows more than the common student you declare that he must be a skilled Conjurer. By advancing his fame this way you make other men marvel at your good fortune to have such a talented friend.

Cease to spread Irreverence while you pretend Amity, pretending your tongue to be true while really being an Untrue friend (to God and his Dominion as well). Such Friends and Foolishness I shake off. I renounce you. Shake off your Folly.

Imperfectly zealous: Perhaps you mean well, but you miss the Mark by far if you kill a Lamb to feed his blood to the flock. Lamb's blood provides no natural sustenance to Sheep. Christ's flock is not nourished by your horrible slanders, nor are your pretenses well-graced at all by your rash ragged Rhetoric. Those who use me this way will find a foul Crack in their Credit. Speak only about what you know. And learn what you know. Don't believe heresy which endangers someone's life. Search to your heart and let Charity be your guide.

Malicious Ignorant: What shall I say to you? "Prohibe linguam turam a malo. A detractione percite lingua." "Cause thy tongue to refrain from evil. Refrain your tongue from slander." Though your tongue is sharp like that of a Snake and the poison of an adder lies on your lips, think first and take heed of what you say.
"Vir linguosus non stabilietur in terra. Virum vilentum venabitur malum, donec praecipitetur. For, sure I am, "Quia faciet Dominus ludicium afflicti: \& vindictam pauperum."
"A talkative man will not be stable [or firm] on earth. Trouble will hunt down a violent man, until he is taught." For, sure I am, "Because the Lord will bring about judgment for the afflicted, and protection for the poor."

Thus I ask my true friends, and Countrymen (you Mathematicians, Mechanicians, and Philosophers, both Charitable and discreet) help me silence the untrue tongued, my envious Adversaries and all false Foolish friends.

Furthermore consider how Basilius Magnus presents Moses and Daniel before the eyes of those who consider Philosophical Studies like mine to be ungodly or unprofitable.

Weigh well what St. Stephen says about Moses: "Eruditus est Moses omni Sapientia AEgypyioru \& erat potens in verbis \& operibus suis." "Moses was instructed in all manner of wisdom of the Egyptians and he became powerful both in his words and works."

The Philosophical Power and Wisdom of Moses was not unlike that of the Holy Ghost. Yet Pliny called Moses a wicked Magician.

Moses might have learned his Philosophical wisdom before leading the Children of Israel or perhaps afterwards, when he performed wonders for the King Pharoh. Saint Stephen holds Moses' Philosophy in high esteem in his Recapitulation of the Old Testament at his martyrdom (when he was full of the Holy Ghost). Basilius Magnus avouches that Moses' wisdom served him well (not to mention how it served the church of God).

Regarding Moses’ wonders done before the King Pharoh, God himself said: "Vide ut omnia ostenta, quae posui in manu tua, factas coram Pharone" Which translates, "See that thou do all those wonders which I have put in thy hand before the Pharoh."

You can see how rashly Pliny has slandered Moses, accusing him of vain fraudulent Magic saying: "Est \& alia Magices Factio a Mose, Iamne, \& lotape, ludaeis pendens: sed multis millibus annorum post Zoroastrem. etc." "There is also another sect of magic, deriving from the Jews-Moses, Iamnes, and Iotape, but this was after Zoraster by many thousands of years."

Let all who are even Inferior to Pliny in Judgment and skill of Philosophy take heed, lest they overshoot themselves rashly in judging Philosopher's Strange Acts and the Means by which they were done. Furthermore, beware of faking, scheming or imagining monstrous, unnatural feats when none were actually done (especially if there is not a spark of truth to it).

But most of all, those that Foolishly and Maliciously devise, then devilishly attribute their new found Monsters to me, let them be ashamed in front of their fellow Men. Let them dread and fear the Just Judge. I hope that time will show that I am Innocent in hand and heart and have not trespassed against God or Man in any of my Philosophical and Mathematical Studies and Exercises.

## The Art of Archemastry

[Experimental Science, certifying something by experience]
Now I end with Archemastry. This art is rare, but the name is not new. Another Art under this one has been imbued with this English name before. [Nicholas Clulee notes that the English alchemist Thomas Norton uses the term, which means "full of mastery"]

This Art teaches how to actually experience all the worthy conclusions proposed by all the Mathematical Arts and by true Natural Philosophy and put them in a broader scope in terms of these same arts. Also, by using proper methods, and in peculiar terms, it helps these Arts to become complete Experiences which cannot be challenged.

If you recall how we put the Art of Architecture above all common handiworks, you might have some idea of the powerful authority of this Science. I sometimes call it a Science rather than an Art because of the excellency and Mastership it has over so many mighty arts and sciences. And because it starts with Experience and then searches forth the causes of conclusions (and applies them to the Experience) it is called Experimental Science. This is what Nicolas Cusanus [Nicholas of Cusa, 1401-1464] calls it in his Experiments Statistical.

Another Philosopher, Native to this land (and whose flower of worthy fame can never die or wither) wrote extensively about it at the request of Pope Clement VI.

The Art carries with it a wonderful Credit. Using reason, it certifies to all the senses, fully and completely, to the utmost power of Nature and Art. It certifies by complete and absolute Experience.

The other Arts have Arguments and Demonstrations that persuade and, in words, prove their Conclusions* very well.

Words and Arguments do not certify things like our senses do. They are not the full and final fruit of Sciences that can be practiced. And though some of the Arts incorporate Experiences, they are not complete, not brought to the ultimate test: the senses.

For example, the Natural Philosopher debates issues and tries to draw the best conclusion. The Astronomer and the Optical Mechanician learn some things by observable Experience, but not everything.

This is where the Archemaster steps in and pursues more Experience by using his Experimental doctrine. This makes Archimastery the chief and final power of the Natural and Mathematical Arts. I have read and heard of the two or three men who left good record of this Description of Archemastry.

This Art involves fantastical Imagination. Some Sophister might, cum suis insolubilibus [by his riddles], claim something to be irrefutable with a flourish and dazzle your Imagination and destroy your honest desire and Courage from believing these things, so unheard of, so marvelous and such Importance.

Well, do as you will. I have forewarned you. I have done my part as a friend. I have discharged my Duty to God and at his most merciful hands received my final accomplishment.

The Science Alnirangiat does Archemastry great Service. Muse nothing of his name. This is its proper name, I have not changed it. It has been used and published in Print by other men. Under this comes Ars Sintrilla which was briefly discussed by Artephius. But the chief Science of the Archemaster (in this world) is another (as it were) OPTICAL Science, whose name shall be told (God willing) when I shall have some (more just) occasion to Discourse upon it.
[Nicholas Clulee writes that these two arts with Arabic names refer to the art of divination and suggests that the "optical" art is scrying.]

Here I must end abruptly Gentle friend and undaunted lover of honest and essential truths. For those who have (for your sake) requested me (an old forewarn Mathematician) to take pen in hand (through the confidence they had in my long experience and tested sincerity) for declaring and reporting the benefits of the Mathematical Arts. To satisfy the Printer's request, forthwith I will end this new attempt (and so costly) in a matter so slenderly (up till now) considered or esteemed among the common Sort of Students.

## [this book is intended for scholars who are not necessarily University students]

I have been asked to explain why this book on the Principle Science of Geometry, entitled Euclid's Geometrical Elements is written in our vulgar Speech of English and is intended for people who don't know Latin and are not University Scholars. (Truthfully, I think such an explanation is unnecessary.)

My intention is not to diminish the Honor and Esteem of University Students and those who have Graduated. You too will Benefit from this work, even though it is intended for those who are not as privileged.

The whole Mathematical Quadrivium exists in French, but the Universities of Paris or Orleans (and others) are not offended.

Nor in Germany have the famous Universities been at all discontent with Albrecht Dürer's Geometrical Institutions written in Dutch, or with Gulielmus Xylander's learned translation of the first six books of Euclid into high Dutch. Nor with Gualterus H. Riffius' Geometrical Volume, very diligently translated into the high Dutch tongue.

Nor do the Universities of Spain and Portugal consider their reputation decayed or suppose any of their Students hindered by the Mathematical works of the Excellent Pedro Nunez written in his vulgar language. Neither will be Studies of University Students be hindered by it.

The students at the Italian Universities (like the Academies of Bologna, Ferrara, Florence, Milan, Padua, Pavia, Perugia, Pisa, Rome, or Sienna) do not find themselves disgraced nor are their studies at all hindered by Luca Pacioli or by Nicolaus Tartaglia who have published Eudlid's Elements, some of Archimedes work, and large volumes of Arithmetic and Practical Geometry, all in their vulgar language, Italian.

Indeed, how the Common scholar (or even Grammarian) who will be shortly attending a University can now be sufficiently instructed in Arithmetic and Geometry (as Plato recommended) and be better prepared for all kinds of Academical [Platonic] or Peripatetical [Aristotelian] Philosophy. Thus, he will proceed more cheerfully, more skillfully, and more speedily forward in his studies to be learned there. Saving time, he can profit in other ways.

Also, many young Gentleman or fertile English wits who never intended to meddle with the profound search and study of Philosophy (generally learned in the Universities) may now more easily sharpen their wits where otherwise they might be spending their time in foolish exercises that serve neither God, the Commonwealth, or their families.

And the Universities may have great Comfort with good hope that because of this English Geometric and Mathematical Preface, they will now be more esteemed and necessary. For when it becomes well-known that such great commodities result from the study of the Mathematical Sciences and the unlatined students have tasted such rare fruit (that heretofore has not been so fully clarified), all men will realize that far greater assistance in understanding the Perfection of all Philosophy may be had in the Universities (the Storehouses and Treasury of all Arts and Sciences essential for the best and most noble State of Commonwealths).

Aside from this, how many Common Craftsmen are there in the Realms of England and Ireland who deal with Number Rule and Compass, who, with their own Skill and experience will be able (by this good information) to figure out and devise new works and exceptional new Machines and Instruments of use to the Commonwealth, private pleasure, and the better maintaining of their own prosperity.

I will not (therefore) fight against my own shadow. For no man (I am sure) will open his mouth against this Enterprise. For no man who has Charity towards his brother's furtherance in virtuous knowledge, no man has any care and zeal for the bettering of the Common State of this Realm, no man who cares not what wise men (either Sages or those fixed in their ways) thinks of him, no man (I am sure) will open his mouth against this Enterprise.

Nor will I make an Apology to anyone for doing this virtuous act, for setting forth Profitable Arts to the Englishman, in the English tongue. But unto God our Creator, let us be thankful that: three principal Instruments. I have given you abundant proof that these Means are the Mathematical Arts and Sciences.

In my Mind there is so much more I would like to write about then matters, but I am pinched for time. But I have no doubts that if you are provoked by virtuous zeal and honest Intent to read and study this Compendious treatise, its fruits will give you great pleasure. ["Compendious" means essential facts presented concisely].

So you can more easily perceive and better remember the principal points of my Preface, I have summarized it in a Groundplat or table (in the order in which they were presented)
If Haste has caused my poor pen to stumble anywhere, surely you will forgive me,
(as it is my earnest and sincere intent to please you). Consider the
huge rocky mountains and the perilous unbeaten pathways which this pen has toiled and labored through (both
night and day, for a while) to bring you this good News and Wonderful proof of Virtue's fruit.
For the rest, I entrust you to God's Merciful direction, heartily beseeching him to help make your studies and honest Intents flourish, for his Glory, and for the Benefit of our Country. Amen.

Written at my poor House<br>$\frac{\text { At Mortlake, }}{\text { In the Year 1570, February } 9 .}$



## PARALLATICAE Commentationis Praxeofq; <br> Nucleus quidam. <br> Authore foanne $\mathcal{D}_{\text {ee }}$, Londinenfi.



LONDINI
Apud fobannem Dayum $T^{\prime}$ ypo $=$
graphum.eAn. 1573.

olumine explicatos, dicari debere, agnofoo: tùm ropter multa, magnaq; erga me eiufdem merita (quax in hominé ingratum, immemoremue contulife, haud videbitur) rum ob maiores alias, iultilfima/q; caufas. Quoniam denigue res Parallaticx (yt fapra dixi) max-
ina ex pirte, ad hune fcopum reduci folent, yt yel compoits, feparenter, in fuas partes : vel Parallaxiun data differentia, vtrafg; reddat notas: Quantüm (urater plurimes ciufdem alios vfus ) in veramq; iftius jarallaticinegotij partem, hoc noltrum valeat Theore wa tertium, prelletq; fubfidij, omnes facillunce intelliailt. Vnde, cum circa hoc Theorema breuiffimum, tain frequeds verfetur, Parallazition difcurfas: pramittantior vero, que \& 1 aboris \& difficultaris habeant nó-
 tiocinationibus Mathematicis) quibus fuperatis, iv, $\boldsymbol{j}_{-}$ gaam Nucis fractis teftis, ad Nucleum fructuofum, finemp; laborum iam peruenimus : in ipfius videlicet laxium compofitarum feparationem : vel ex differetria data, ad datas puocuelipfts reddendas reatia data, ad datas quoque iplas reddendas
Parallares: Igitur, Nuclei cuidfam in.
ltar, hunc haudabfurde cenferi poffe Libellum, fatis iam oftendimuy e-
uidenter. Eodem itaque vasmini fruaninig:, Amici mei, veritatifi; fcru-
duftrij.
Martherenghas maitnis annacribibe Munfir. Marry. 5. An. 1573.

## Optimarum veritatis Artium  xondin

为On melater, varias effe vias, ad Darallaxes crâ in Sublimiapparentium intelligêdas aos escogitavimus aliguot) gar val folo intoitu, velabig; aliquo Logittices auxilio, nobis exa Ged veritatem referrequeant. Negue habent Mathemstici omnes, eam, quä habuit Proleuizus, loe opportonitatcor ( circa maximama Lunalatitadiné eli ciendam) ot verticibus, pene, Phatoinena femper intnoftrarumparte, vel duss diverforum fupra nottrum horizont élocorum, recipimus fimnt vnitas Parallaxes: ed deinde, ratiociondo, feparamas artificiofe: Vel ex duarum diuct(arum Parallaxium (artea)içua) cruta differentia $\div$ ad integras feparation cognofecndas, Ma romaticennofipet accingimus. Iftas duas vias (aliafq alignot) diligenter, ingenioféé; ( 50 o quidem \& pro priomodo) nupertione tractauit, charilnanus mini Iu mas Diegents. Arex ifto noftro Theoremate terno, ne halungonideon recepitaoxilii. Com ante vltimam tiegr, Febrastij parteriti, prorías illi incogoitum \& natiditumerat. Licet antea quidem, tüm fua [oontc ruma meaceerfitus, aliquoties mini adfuifers dum da to:ohoc noftro (veritatiselicienda amore, fofcepto) dilererenus negotio : dede optimis obseruandi moes nooasjnire gatueremus rationes. Regiomontani fítuto nofloo, haud fatis fidelifer inferuire potoiffe Mé Ţue cnixiffioué hortatus eft, accuratios, quam nolti fecetiont maiores, de iffis meditari : dum interim ipfe divifdent, fuas [corfin confuicret Mufas, Vide pra-

## Parallaticus $\mathfrak{N}$ (ucleur.

Tbeorema. $t$.
Inter duas quarcunq; , ealdem omnino, \& homogeneas magnitudines, vnafolum exiftit ratio.

Vanquam cömani amnium ferc̀ hominnm inducias, Goc jic fe habere indicetur: tamin,vt vel quabw (ai clarize illailtrarc hanc veram fententani : vel alyt, contraethdí canillandi, occafioně ommt pravipcre pefimist pö inatile confori deber, fiexenplari quadà demenitrati-
 de.Breanf/culas ithes primim confideremus defonptioner.


 ies fuperficiebwe serfana couparabus - Smi igisur dae mag. nitudimes, ommine esilom, $\&$ bomogend $A, C$ \& $D$ itro rationew visam folim efle, ipfus $C$, ad D. Si veronolix quir adueryari velib, Co exproere $A$ ad $B$, in cadem rati ome, qua oft ipfins C dad D : Praticea of Edd Figes. dem ratione, ques eil asfire C.
ad i d afferre donique, now $\quad \underbrace{\mathrm{A} \quad \mathrm{B}}$ andem e/fe rationem vipfoss A rrà quidem (artí prafidiürva. rrd quidem (artu prajidis va.
Iidif (imin adimet) dimicabimes. Ex definitione mion : Reatio,


Edefinitione vinh : Ran,
 un renven quamistri, haibiado : relpotium mannum, fune x dons of Oraci Mathematici logummizr. Sed, ex hypethefi, me.

## Parallaticus $\mathcal{N}$ Nucleus.

 Cuns cminv, ex by poitoff, arcui $X T$, ơ $A I$, fint Similes arcus: per Similiin arcair definitspoci, angulas $X B T$, equadis eit angulo $A$ a 1 . Sed C Noti) jumum ert, angalom



nis Srpothofins, Duare, per 32 .primi, Elementorumi, of religuisanguluy $M X$ B, (ja triangnle $B M X$ ) equaliseil religne $O$ A $B$, in triangulo $B$ O $A$. sa nianguli igi-
 do $B A_{f}$ fint powalgga: (nimirai ipfe femidiamerin infirttum circulorum.) Et $X M$, d AO (videlicet finusredi) amolog 4 ernat. Et BM, $M B O$ (finmfocumdi) atians
diata Februarii die, humaniter me \& perofficofe inuicons, foas ofiteodit, quas (interim ) de Parallaxibuse Typograpticum, propit, pararas habebat : adiecicgi editionis fux havd minimameffic caufam, vt ca the hi berares (haiufinodi feribudi) molettia: Blisque pramitteret, quas, prelfies i me icriptis (de ithis, finill búfoe rebus ) Jucearaliquam, hac fua adfercens in dultria \& quò plures, interea, inftuereatur, red
derenturg: tefles, maiori fide digni cuma $\&$ ipft, doo tioribus \& Mathematicis oculis, iffud artificiofeolferuaredocerentur, quod calo adhuc fulger, ratifinum Speateulam. Qgod cius inntitutum, tamill honorilicum (ex Mathematici fai ingeni), tam ills Itri edito acuminis (pecimine) tump nilh gratum (ol am ) tựù tudialis optabile ( extor, tian opportunc, timq:expedité, publicatis phinofophiz colettis documentis ) norl potai, tion approbare, laudare, amare veritatíqsinuchigatoribus, fanftum \& falix fore, tum prare, rum fecrare. Et ne ipfe, laudator fotum, yideripoftht, laboruas, quos nobis commanicant alij)
\& no atte facilismeornm aliguot erogator Jnuento rum, qua multim, has tempeflate, ad mirabilis veritatis agnitionew, ov illuffrationeal facere queant Noftro proinde diatios inclufa ergaftula (vbi nupe nats fant ) hatc nolui detinere Theoremata : fed er, Aitum porius, in poblicume enittere : vo fractuon havd uarounin Mathenaticis reportent, donec alia noftra in hoc Ptilofophandi geuere) (cripta, tempore fon prodiegra opargon. Qogod \& rólabentius feci, quium admanas Illufitifiaii illius Herois, huac nolframit ellum, ham jeraentarumintcilicsincin, cumpario admirabilitatem, Cuietian, iure meritifino, illos noftros gazatofconq: in hoc Portento confiderando examinandoq; labores exantatos, iufogs aliquando

Parallaticus $\mathcal{V N u}^{\text {ncleus. }}$
Fluarï duarimagnizulinŭ, $C$, of $D$, bomagenceriü, exdicm nashent, quantitatet, nullo filli.
licet, vel aucte, vel imminishe nodo quare, alia, aliag, now e- $\underbrace{\text { C——D }}$ omparatarum, refultans babjo.
 udeo: $\operatorname{ced}$ vna, eademp $)_{i}$. Prainde tiam, ciuns focsmdums comparationem quatutitatio $C$, ad quantitateno D, vefullans habitado, inueniatur eadem in $A$, sum B, collata - (inxta adarefarimm) Similiticr fa candum comperationem quantitatis $C$, ad quantitat't $D$, cefaltans habitado, inwentatur endens, ex quanritate Eya $F_{\text {seompurata : ( } 2 i}$ adrerforias ip/e concedit) . Nect/Jo rio co illa que inter A \& $B$ deprebenditar, efs eadem om-
 modo, diucerfa. Inter dana jigitur qualconq; eaddeni omnino, \& fic evel illuilralfes, vel demenfitrad/e opportuit.

Alicer.
Praterta: fi quis naflrum bec T betrems,vel /u/pecis habcre cellet, vel lablefathare tomaretar: parivatione,它 wndecinamm quinti Elementerum Euclidir, vel is diso' qudecinam quinti Elenenteraun Eucher, molidar:: Que bium wovart, wel tangua falfam encrere, molidfar: 2ine
haec eft, Quz tiden rationi, fuot exdem rationes, adiuticem fant exitem. Ectheforvero, \& Dierif puas eiuffem propofitionis, fic fe habent, verbaltm. Sint esine,firat Ad ad 'B,

 interino Eachdirs Theomifuc adloareaf demonsitrationi.

Theorend.

Parallaticus D ucleus.
 permintatim (per decimam fextam Euclidu) vt is $X$, ad A: fic $X M$, ad A O. Simili argiswento conuincemur, vt $B X f e$ habet ad $B$ if fic X L, fohaberead A $N$ : as trian-


 Elenventorï̈ Enclidus,eadem efl ratio inter $X M, \delta A O$, quare (t inice $X L, \notin A N$. Quanebrom of permuiatim (per decimam fextaw quintr Elomentorwm Enclidis) wf $X M$ ad $X L_{2}$ fic d $A O$ ad $A N$. Sedper Conflrachiphens, $X N, d X \mathcal{L}$, funt finus redi, $X T, O X V$, arcuin: fimiliter \&b $A O, \& \in A$, relft, jimue funt relli, $A I$ \& $A K$ arcuam, illis fimilisen . (Sine autem B. $A$, maier fit quitm $B X_{3}$,vel minour, volilli, cigualiu, idem arie demponfrations is orde, ơ eademeveritas. I Igitur Omnium daorum, eiardè Circuliascuum, finusreati, candem inver le raiost habentsquam aliarum dunnum, hijs fimilium, zecuum, fiuus refli, inter fe habent : five is zquali, Gine maiori, five ninoriacceptornin cirulo. Leod densonElrafle opertuit.

Porifma. $\quad$.
Hinc manifetta fit, omnium duorŭ Similium arcuum finus rectos primos, fecundof $q_{5}$, eandeminter fer rationem habere, quam ipfar femdiametri circulorû, ex quibus ipfifimiles defumtuntur arcus.

Porima. 2.
Aquè etiam clarum,reddi poreft exiftis: Omniû milium arcuum, eam mter fe rationem effe, quar eft femidiametrorum refpondentum, ive finuum fuorum rectorü primorum, fecundorumúe, inter 1 lc


Parallaticus $\mathcal{D}$ Vucleus.
ad E, candem habef rationem, quanm $D$, ad $F:$ (gnis If ob D fint arcios fimiles, ex hypertbefi) Erge pormatation, $B$, sd
 omdectman, ightur, quinti Enclidis, eadem erit ratio ba a
 metraramp fillicet, inter fe, Sicep.prima Qhefiti pari con-
 Jinum redum ipjow D,eflfcut And C.Simetia, ratione
 candam, ipfras D, per radem Port ma. Sed per friorem tum domenitratame purtem, wh $A$ ad $C$, fic $B$ ad Diergoper von decimant quint Elementornm, vo $G$ ad $H$, fiwe finns for
 Onaium proside finditium arcuem, cadem eff inter le ratio, que femidianectaró refpondentía, Give finuum fuara rectoro prime


Theorema. 3 .
In duabus quibufcunq; diucrifs, ciufdem Stelle fimilfue Pharnomeni, Parallaxibus (modòinte rex, diurno Totius folum ferri concipiaturmotu) dem ratio crit,finus tectu,maioris Parallaxeos, ad finum rodum minorisa que eft finus recti,maioris a vertice diftantix apparentis, ad minoris diflantix apparentis, finum rectum.
 catur inter do $n$, relas limea d $B$. 这: in contran. sen \& direalum, verfus partes B, estevdatar. Is qui accipisar prathamen, protlo qued dicitur Zenith noitrum

 B.if. Dullatz

Parallaticus $\mathfrak{X}$ (uccens.
ABO, conflarepoteli (percenffrultionem, co diäam vi-
 num reflum, ffearcus Al: Fiuc anguli AB O, ani (per Is. primi Elementerui) ) eqqulia eif sotirapofitus, CB EF Apparcutì nimirim maierir diflasilia verticalts, akgulus. Qeare arcwi illine diffastie verticaliu maieris, fimilus orit arcuif dl:por connerfiowem definitionìs,Similuym ar-

suam . It $\triangle N$ (fimilo argumento) finum redium effe, certum ifl, ipfow $A K$ arcui : fiwe $A R S$, angult: baic efs
 Dinoris dipantie apparemt a vertice. 2 sark, per comper. ticalii, arcom habet, fimilom igfi AX arcui, Ilaque (per

pareatia

Pavallaticus $\mathfrak{N}$ Mclens. sifus in dues arcas $A G, b G A$. Sitritrreportie fisar arco AG,ad finmmariki G B,data. Dice guad itere, ariasm putialium $A G, \delta G E$, datus habetar Subtemdeter esime arsili $A G B$, Chords fsa, $A B$. Ducaturs per panditum $G$ of centrum tircult, $Z$, diameter circulí i fesami Chardam $A B$, in panilo $D$. Ex pinnziu astem $A, \& B$ (arcium $A B$ arminantibus) dua ritiade fendent, perpendiculares ad liametrums : que fint $A E O B R$. Quarä viramg. cev. flat eff fimam roilum arcos fibi conier minalis, $A$ E qui-

 porit aquas.
litatis axant itatits crint
dacoscus $A$. dagonces $6,0,6$ B,
quater,$~ P e r$ quatar
commumpm
foientid. $5 i$. nabus fais aqualibur ex. Citentibut: Cunge toting
arens $A G B$, arrus $A G B$
fir molias, erit it malas, erit faum A $G$, $A$ GB, netust
 ropartip aqualmini, eris altcr dervim, altere maior, si tuqui $A E$, manginine $B H$ : onde of arcis $\Delta G$, matior
$\mathcal{P}$ arallaticus $\mathcal{X}$ Whclens.
Dubla if fit retha $B H$, angulum cum $A B$ lines, coprefoce. den rifium. Sit verè Phanonernial aliqued, quad in Subla.
 Invgiori a wertice diflintia Apparenteco in D_(Pacio Ap. parcanteverticalis mineri a fat vy por nullam interas, tre ter Tatias motum, agitari ipfium admithtmus Phanome-


terreno arbi comentrisatex folins diurni motps byputhefi)
 circwmorentia, in punclo E. Ita tudd pundia $A, E, E$, in





## Paiallaticus SMarcoas.

parenis maier's dijfastie verticalio, ad finum reantiflinu ocus, minaris vertizalio diflantie Apportstit zeandem

 ownino livcam © 10, simum reffum effemainis mofire Parallixesos, ad C procrats : of samdem Linzam C $i N$, fidian rothum effe, mineris mofles Parallaxess, add D pre. wenichis - Quare (per primam Threvena nefrwm, o vndecumam quinti Elementeramm ) Eanden omning has. bebitr rationtm, finus reitus Partllaxees maieri, ad finum thasm Parallaxees minaris, quam babel finus reflum ma. iaris dyflamizi verticalis dppartatis, ad finusen relitionimerir chpparentio difthentia. Freinde, In danlus quibuis


 Quad dompnifrafle epertaif.

Admonitio.


 verice

 tale $A B I$, of hinca $A B E$. Sndem alip plano. Sofler $A D S$
 (Tonima,

Hinc manifeftum redditur : Sidaarum verticali um Appanenticm diftatiarumalicuius Phanomen C.)

## $\mathcal{P a r a l l a t i c u s ~} \mathcal{V}$ (ucleus.

 mit arcu G B. Chm antem, prapertio $A$ E $A d B H_{3}$ fit nota oporict eam in terminis notis reperiers per definitienen roportionis date. Etideoper quintam primi hains, in

 gull, deqs angulor upud constrapofiter, of ( $j$ er 3 a.primi $E$. (cmontrouns) duas relignes habeans aqades, crunt ipf (ise neiangali. Et ides, per of fexti, praportio $A E$, ad $B H, j i$ iat $A$ D, ad D B. Proportio ailtena $A$ E, ad A Hh, exit tan.
 ad DB, Ch Elati R ad S. Etcarnme$\operatorname{sim}, A B, A d$ BD, ficut $R$
S, adS. Tres , ads. Tres wit buram guatiostinm, atie fump. Primim, $R$
S, quidem, s, quadem,
prepter dess prepicr deses $R$, \& $\delta($ ex qui. but compofi. out compofio R
the oft ne:
tos mamerras
antem $S$, ex ert quef futradiltia unt, motes ein. Cherda de weque $A B$, mosa $+f$ f proptor excimp. $A G B$, notim $;$ interce dente tabulasinumm, ant yberdarwom, Quarla igitury fol

$\mathcal{P a r a l l a t i c u s \mathcal { X }}$ Incleus,






 tropertioncon, quan arima $\sigma 2$, ad sutam Circomfinenti-


















Parallaticus $\mathfrak{V}$ (ucleus.
portione finuum fuorum, vterquis corum cognirus habebitur.
Duadrow $A G$, ó $G B$, centerminales intelligan. Nr : minorgíquiefl G B, pors maturis, AG. 2virü̈ diffoentid fit data -arcw videliset AB. Eerump, Finser, he-

 indeffinits idismatrum tamen cirizuli $G T$, complecticms. Educutaryif fenidiameter $Z M$. fecant chardant $A B$, erthogenaliter in pantio L. A pumctis A of $B$ (chordA $A B$, terminamilibue dius perpendicnlores id D, \& E E, ad di.
 $1 G_{1}$ d $G B$, sitataque ipfifuerint squales: boe efl, pre-
 commump
fciontioms,
 Corentia nutd : refidavi wedictes, arcar faliect $B G$, miner sognitus crit. Caif farcmm AD, nather, adieteris prodibin arcut $A G$, mator, iegsitus. of $S i$ vird alter finnumg 1G. finss, maier fiew arcul mineris, BG. Abfowdatury exfinm A D, linearrla K $D$, aqualis iffi B E. Duda hime

Parallaticus $\mathcal{X}$ Kicleus.









Parallaticur $\mathfrak{V}$ (inclews.


Paraliziticus Dinetcons:









 Mancriscan rypribust: fer Cirollariver quipse prion

 $\| E(\delta)$

## Parallaticus $\mathfrak{D}$-uiclens.

vel quacunq; aliz, dana Parallaxi, cum Apparente diftantia verticali, ciufdem Parillaxeos propriat: non cognita quidem, Phanomenià terra ditan-

A/jendix. $s$
Hinc Peurbachij votis fatifficerepoffumus: qui-30. iminutorí Chondan, veraciecrnon haber, qquerebatar, in fine libellifui,deSinubus \& Chordis. Que (mquitille) fi baberetur, omnes Chordas arcuumalioruin, veraciver effentnote,

Appendix. 2.
Similiter, exproprictatibus hifcefie (in Trimgulis $\mathrm{ACB}, \mathrm{ADB}, \mathrm{ABO}, \mathrm{ABN}$, \& alijs Schematibus)demonftratis:qualia infern, demonftranque alia pollint, tum Theoremata, num Problemata bimus , in co, no iffomirabili,edere flatuimushbro.







 feriontio Paraliavilatr.
$\mathcal{P a r a l l a t i c u s} \mathcal{X}$ (ucleus.






 radix quairata, eh, for ssosg (imis. 1 Dande ( aide per radirem formatam $[16659$-rianirem hivine $D Z]$


 Live gradidar ze, masent gradul ra. Gompulo prine te,

 forvpela prian
arras $A G$.

Porijuma. s.
Siduarum pradictarum Parallavium differentiafoJuin fit data, cognitioc, \&e doaruin diflantiaruma vertice Apparentiumareus,etiam cognia, Pariatifque, illarum diftantiarum proptras, fatis eftmanifftam.



Propof. xxyy.
Si dan fuerit differentia duortom arcuum caro pro-

Parallaticus $\mathcal{X}$ (uclear.

 aras, dimidiane arye diasm misse) of nlanwiter do
















Prifma. 1
 thematicis compohitos, corrigi polfe allasluna

## Parallaticus $\mathcal{V}$ (uclens.

Adntonitio
Cancent antom amnes qui vel ambitionii alliry per.
 nilitats, predentrex csammasta, /wa and cants in dello.


Epilogus-


# A Certain Essence of <br> PARALLAX 

Commentary and Practical Application

Written by John Dee
London


LONDON
Printed by John Day
In the Year 1573

## Definition of parallax

Parallax is the angle between the lines that join a heavenly body to two different points of observation.

Geocentric parallax is the angle between the line joining one's location and a heavenly body and the line joining the center of the earth and that heavenly body.


## Synopsis of: A Certain Essence of Parallax

Dee's work on the mathematics of parallax was often put in a single binding with the work of Thomas Digges's entitled Alae seu scaleae mathematicae, meaning "Mathematical Wings or Scales" (how he graphically visualized his trigonometric theorems).

The famous mathematician Leonard Digges (1520-1559) died when Thomas (1546-1595) was only 14 , and Dee had become Thomas' "mathematical father."

Both Dee and Thomas Digges were inspired to write about Parallax when a "new star" (or supernova) appeared in the sky in 1572. But Robert Goulding and Stephen Johnston assert that these two friends had different motives for writing about parallax.

Digges was a Copernicus enthusiast and wanted to use his mathematical findings to promote Copernicus' heliocentric ideas.

Dee steered clear of the controversial Copernican theories and emphasized how understanding of parallax was was important in the astronomy involved in astrology.

[^6]

## A neceffary Aduertifement,

by an vnknown freend, gruen to the modert, and godly Readers: who alfo carefully defire
the profperous State of the Common wealth,
of this BRYTisu KinGDOM, and
the Politicall Sacverixis
thereof.


Amentable and irkeforne, 1 are thefe our drery dayes: vinumprame (my welbeloued Cuntriman ) Seeing the conditions of to to many, are become fuch, as, to be to to curious of other * Mens *ar dooings: As though, they them Jelues, were fuperhabundantly perfect: or dwelt in Security, of not beyng at any tyme, hereafter, either furueyed, or controlled for their own.
Nay, feeing the fubuity and impudency of $*$ fome, 2 . is fuch, that they can, and dare, cunningly and craftily, conuey to them felues (or, to whom they lift) the Title and Intereft of the thanks and commendation, due to other Men: who are not of fo brafen ${ }^{t}$ vifages, as to practife fuch ambitious fatches for them felues, or to procure fuch malitious Difgraces, to o- Jmein ther : But are of that myldenes of Spirite, as, $\mathrm{P}_{\mathrm{A}}$ tiently to attend the end, which fhall reueale the Verity : when, iuft gwerdon, fhall to euery Man be diftributed, accordingly.
And thirdly, Seeing, fome are fo doggedly vio-3. lent, and vaynglorioully doting, that they can not $\Delta . \mathrm{ij}$. like,

Dee's wordplay on his friend's name, Sir Edward Dyer

$$
\begin{aligned}
& \text { TO THE RIGHT WOR SHIPFVL M. CHRISTOPHER } \\
& \text { Hatton, Elquyer, Capitayn of her Maiefties } \\
& \text { Garde, and Ientlemans of her Priny Chamber. } \\
& \text { YF Priuat wealth, be leef and deere, } \\
& \text { To any VVight, of Brytifh Soyl: } \\
& \text { Ought Publik Weale, baue any peere? } \\
& \begin{array}{l}
\text { Ought Publik, Weale, baue any peere } \\
\text { To that, is due, allWealth and Toyl. }
\end{array} \\
& \text { istro. Wherof, fuch Lore as } I \text { (of* late, } \\
& \text { Haue lernd, and for Security, } \\
& \text { By Godly means, to Garde this State, } \\
& \text { To you I /end, now, carefully. } \\
& \text { Unto the Gardians, most wife, } \\
& \text { And Sacred Senat, or Cbief Powr, } \\
& \text { I durst not offer this Aduife, } \\
& \text { (So bomely writ,) for fear of Lowr. } \\
& \text { But, at your will, and difcreet choyce, } \\
& \text { To keep by you, or to imparte, } \\
& \text { I leaue this zealous Publik voyce: } \\
& \text { You will accept fo fimple parte. } \\
& \text { M' Inftructors freend did warrant me, } \\
& \text { You would fo do, as be did bis: } \\
& \begin{array}{l}
\text { Hatton, Elquyer, Capitayn of her Maiefties } \\
\text { Garde , and Ientleman of her Priuy Chamber. }
\end{array} \\
& \begin{array}{l}
\text { YF Priuat wealth, be leef and deere, } \\
\text { To any VVight, of BrytifhSoyl: }
\end{array} \\
& \text { That*Redy freend, can witnes be, } \\
& \text { For Higher States, what written is: } \\
& \text { Of Gratefulnes, due Argument. } \\
& \text { If greeuous wound, of Sklandrous Darte, } \\
& \text { At length to cure, they will be bent, } \\
& \text { M'Inftructor, then, will doo bis parte, } \\
& \text { In erneft wife, Iknow right well: } \\
& \text { No Merit fball forgotten ly. } \\
& \text { Tbus much, I thought, was good to tell: } \\
& \text { God graunt you Blis, aboue the Sky. }
\end{aligned}
$$

temq́; Publicam procurandam, ac promouendam, expeditifsimè \& potentifsimè. VVbich, God graunt,


The Epistle in Meter, (annexed in the end of tbis Book,) was by the Mechanicien fent, after that the vnknown Freend bad (at bis own charges, and with bis careful Trauail concurrent, ) put the forefayd two Treatijes, in Print: © deliuered again into the bands of the fayd Mechanicien, the whole 1 mpreffion therof.
The diuers Intents and purpofes of which Epifle, are eafily to be perceiued. Therfore, yf to baue Jayd tbus much, was
neceffary, the fame alfo may $\mu$ uffice.

\&TO THE RIGHT WOR-
Thipfull, difcrete, and fingulerfauorer, of all
good Artes, and Sciences, M. Chriflopber Hattoin Efquier: Capitain of her Maiefties Garde, and Ientleman of her priuy Chamber.

3) Ot onely my dutfall good will toward your Worhip, and my great defire, to doo fome Cobing beneficiall to this myNatiue Cuntry; But 3) allfo, a cerrain ftinging Indignation, agaynt V. the Impudent Attempt of fuch, as yfe, wrong50 Trauailes, (and nor hable to yeld any Ingeni2 ous Intention of their own) hane, at this *prePfent, forced me, to doo my Indcuor, for the *An. $577^{\circ}$ 7) publighing of this ftrange Inftrument, with the And humbly to dedicate my firmple Induftry herein, to your worfhips prorection. Truftyng you will the rather accegt thefame, beyig (is it were) a Crum, tomygreat Contentation, faln from hisplentifill Table, whom (I aim aflured) you doo derely and fincerely, both loue and eftane as well, of your own moft curteons difpofition toward all men, with whom your worthip hath to doo: as alfo, for fundry his vertues, and excellent Skill, in many Arts, and Sciences, Wherewith the highelt hath very gracioully blefled him. For which his habilitic, and Talent, he is al wayes molt humbly thinkfull, to the oocly Author, and giuer, of all goodnes and witedome. Verely, tor thele 24 ; yercs ( at the leatt) I hauc had the Ienteman in great admiration : As well for his forefayd excellencie in good learning (foiadged of, Jong fins, by the learned, in fundry Nations) As, for his moft ready Curtefie in Communicating or conferring to and widl fuch, as duly require his Aduife, Opinion, of Iudgenent, in any Science, Arre or Practile, wherein he hath had aty fpeculation or exercife, Such Commendations, as thefe, allthough they be great, (and rate, in any Studious Ientieman of this Kingdom, els; ) Yer, neither the fame, nor ten trymes as great (fownding lowd abour his eares, for thele many yeres palt) baue at any tyme, or yet
doo, any one pyns point, puf vo his hart, vayngloriouly: but haue, doo, any one pyns point, puf vp his hart, waynglorioully: but haue,
and doo make him more Ioyfully thankfnh, to the kingly and free efuer, and doo make him more Ioyfully thankfnh, to the kingly and free geuer, of foch his great Talent : So great, as, 2 sibur Res nole funt, of qui illt
 nem, (As that prudenr Athenienfien Gouetoor, Parictes, fayd, In oratione Funebri; Commending them, that manfully had feent their

 dicantar, Inuident, non credunt.

Therfore, pardon me (I befoceh your worfhip) Yf in rehearfing here, and there (glaunfingly) ) fome points of his due Commendation,
A.I.
I/peak

I fecak far fhort of that, which (farder) your worfhip and other, doo, or may know, and more apdy can expres, to Gods glory: for his graces, on that Ientleman, fo abundandy beftowed : Who (he Iuntice of duvifull
doth make nio les account of your Worfhip, then the doth make no les account of your Worthip, then thic indice or auren and perfect Amitic requireth. Which is a thing, very rarect now dor serter proof of the Premiffes, (by your any where to be found. And for better proof of the Preminfes, (by y our
leaue, and with your patience) I will, here, truly and briefly Note fuch leaue, and with your patience ) I will, here, truly and briefy Note fuch
matter vnto you, as neither (Withall) is impertinent to this Paradoxall Inftrument, now, firtt publifhed : nor mete to be let pas (in a manner) vnknown, and vterly vnrecorded.

For, whereas, about, 3 . or 4 . monthes laft paft, 1 vertuous * Ienteman and Marchant, with zealous Intent, for the Auauncement of God his glory, and the great Commoditie, and honor of this kingdom, frocth Ships, for 2 Northweft Difcouery: And fhortly after, there came furth Ships, for a Northwert ilicoucry: And anter in Print, a little Englifh book, containing fome probable reaabrode, in Print, a little Englifh book, containing fome probable reaEns, tending to the perwairon of mall pece of Credit (for the Attempt Epittle of which little book, no imall pece of Credir ( ) to be liked of was actribed to M. Dee has
to be fene) fet down, in his Mathematicall Praface, with the En glifh Euclide, publifhed : So it came to pas, that it was his wurf fhipfull freend (CM. Edward Dyer) his fortune, Firft, to Aduertic him (as he told me) both of the fayd book, by the Tite therof: and of his Name, in the forefayd Epiftle ( to good purpofe) vfed. Whereupons he, calling to Remembrance his old Atlanticall Difcourfes, to the felf fame purpofe (at the fayd $M$. Dyer his requeft) almolt ten yeres fins, fer down in' writyng : And periuing throughly all realons and aliegations (boch Pro and Contra) now, in the fayd Pamphlet expreffied : did, furthwith, by euery Article therof, in the Margent, Note their value, or, imperfetion. And, ftraight way, after that, made a new Collecaion, for the fame voyage, very probable. And thirdyy (the fame cay , writ, 18. new Conficerations of his own: very pleafant, in probabilitic, , for
an other voyage of Difcouery: (in refpect of Safetie, Nerenes, and Coman other voyage of Difcoucty: (in refpect of Safetie, Nerenes, and Com-


And , M. Dee , being thus furnihed, afwell to maintein probably his former Iudgement (by cM. Gafoom recited, in the forefayd Epifte ) and intending to geue thofe his, 18 . new and very fraunge Articles of Confideration, to him or them, whom he fhould deme apt and def;
firous to furder the fayd Difcouery (no les then this was by a difictete, firous to furder the fayd Difepuery (no les, then this was by a difcrete, carefull, diligent, and conftant Procirfer, follower and furderer, brought to the prefent execution): And alfo, purpofing freendly to examin, ;and faithfully to Inftruet $<K$. Capitain Frobijloir, and $M$. Chrijfopher Hall, and other, that fhould haue the chardge about the fayd Northweft Dif couery ( As he was, , partly by the tigho worfhipfail ' Sir Leonell Ducket Knight, and partly by $M$. Frobilher mintryelf, before that, requefted to doo ) made, then, no delay, to repays to the Mofchouy houfe :

Where,

## The Brytij)

Pag. 4 :
ted, chroughly manned, and fufficiently vittailed The Publik Commodities wherof, enfuing:art, or would be,

 vireorticPVE. Nucligood and politik Order, was (in fo good Time and Opporrunitie) fucligood and politik Order, was ( at so good not onely mal worthy and Royall Counfailers, bue allo Fleroicall Magiferates, who have had fo Eatherty Care for the Comomaltic: and mott wifly, procered fo Oenceral


- That, henceforsvard, neither Frame, Dommerk, Scetland, spaine, nrot any othet Cunry, can haue foch libery, for Inuafion, or their milwoll Confpiracies, or Ayds, any way, Traniporting: to annoy the blefled Sraxe of our Tranquillitic: as, either they baoe (in tymes palt) had: Or侯 els, may haue, whonfocuer they will forg
- Befides that, I report me to all Englifh cataribanti, (Sayd he) of how great value to them, and Confequently, to the Publit-Wente, of this Kingdom, fuch a Necm tute wect? Wher Ships (many or few, great or ward (continually ) their Marchantuke farder, pas quictly vnpilled, vofoyled and vntiken, by Pyrates, or other, in time of Peace.
The wifedom and purpofe of that moff politik Lawnaker, King, Minos, may, herein, to vs, be a fufficient Adueruicement. For, * Ninol, mati. quaformai reram, de quathes cadnamis, Cliffom habait. En doninat ue off pe maxi-




What Abundance of Mony, now, folt by Affurance, ginen, or takep, would by this theanes; alfo, be greatly out of danger?
FAnd Thirdly, how many men (before time of vigent nede) wold, thus, be made very skilfull, in all the forefayd Seas, and Sea Coafts:in their Chanels konowing, in Soundings all ouer, in good marks raking, their Channels knowing, in Souncings all ouct, in good marks then
for auoyding daygets, ingood Harboroughs urying our, in good Ians for auoyding daygers, ingood Farboroughs trying out, in good wars
dings aftaying, linthe order of Ebs and Fluds obferning, ani all other
poines ailuifedly learning, which to the Pofoff Ant of Navigation, are veprings alluicdy learning, whicm the be the beter hable to be diuided and
 thabuted, in a greater Namy , witrelarge of Mainterthip or Pylotage in tyme of grear nede?
Gaberaukl. For, this Art of Natigttion, requirech a great skill and indultry \& And, Yr, zo00 yeres liace, it was found crue, arnong the Grecigts, that, Ars
 nobin mots, now, in our dayes, may is be truly affirmed When, is ts ite twames more, (is particular skill (And infenious feats.) augtpented then it was, in thofe dayes ?. They of this Naus, fhould ottentymes efpy or diece- fie Ptiny Sowndens and Serthers of our Citiantells,

Monarchie.
Pag. 3.
Where ; he found him felf courteoully arid very worfhipfully cuteftcined.
And at that time of his abode there , and ftrer And at that tyme of his abode there, "and after that, at fundry other tymes, of his Reforrs, thither, and to their Ships', he proceded Io with chem, according to his Intent: and pleafured them, Io much according
totheir defire : That he finding them, quick of apprelienfion, and likely totheir delire :That he finding them, quick of appretienfion, and likely to

 truating of them: And they, finding him (aboue their expectation) ikil for) Carefull, for their well doing for) Carefull, for their well doing,
in this their commendable and hono. rable Attiempt: both the one and the rable Attempt:both the one and the other, became very forry of their fo
late acquaintance and conference? for thefe their waighty affaires furdering: And greatly mifliked their want of tyme, fufficient for the Complemet
The Compleor tyme, lufficient for the Complemet menomploget
and principall pointes of the Perfoct Art foen At ot Na of Nsuiggtion learning at his hands, wigtion.
 Yourrocommond
$C b i j i t i p h e r ~ H A l$ either great knowledge in the Sciences Mathomaticall'; and 'Arss. Mechonicall: or expert Skill, of many Caysos and effectis Naturatl: Such points ( 1 fay) to their affaires', and the Peifect Art of Navigation, incident: he very aptly, could; \& right ivillingly wold haue dealt with them in: Yf that pinch of tyme, wold haue fo permitted. For, it is very cuident, by his defcription of the Perfot Art of Nawigation (in his forelayd Mathematirall Prefaces; declared) and alfo, common reafon, and dayly experience, will confirme the fame: that, not onely, fuchfill and furniture, as both here is refiearfed, and in that Praface is fpecified : But, other allo, is moft nedefull for him to be fraught withall, that fall be allowed, for an exact Hydrognsphor, Plyt-Mator, Arche-P Plot, or Grwid-Pylot-Geverall of fuch an Incompa.
 it, yet, is: or, rathet, is it may, 8 sc (of right) ought to be: As Ihaue的

W
 hartily Wifh, That all manner of perfons stanimiun paffing or frequenting any our Seás, appropriate: and many wayes, next enuironing England, frelanda; and Scotland, might be, in conuenient \& horiorable fort (are all tymes, ) at the Commándement
 A4ts of Three fore Tall Ships,' (or more: ) but in ino chale, fewer: :and they, to be very well appoyn-
A.ij. ted,

## Monarchie.

Pag. $5^{\circ}$
flats, banks, Pyts, \&cc. And fo, very diligently, deciphting our Sea Coafts : Yea and in the Ryuer of Thames allo: ocherwhile, vp to the Station of the Grand Nauy Royall. And likewife, very ofiten, mete with the abhominable Theues, that feale our Corne, and vitailes, froinf fundry our Coalts: to the great hinderance of the Publik plenty of England. And thele Theues, are; borb Subiects and forreyners : and very often, and to to evidently fene : and generally murmured at : but, as yet, not redreffed : for all the good \& wife Order, by the mott honorable Senat of the Priny Counfayll, taken thercein,
${ }^{5}$ Fourthly, how many Thoufands, of Soldyers, (of all Degrees, and apt ages of nien) wold be, by this meanes, not only hardned, well ro broke all rage and difurbance of Sees, and endure healthfully all hardnes of lodging and dyer there, but alio wold be well practifed, and eaffSeruice at Sea ? So that, in time of great nede, that expert and hardy Crue of fome Thoufands of Sea foldiers, wold be to this Realme a Treafor incomparable. And, who knoweth not, what daunger it is, in time of great nede, either to vie all frefh water Soldyers: Or, to be a fortuight in prouiding a litele Company of ommigatharimus : taken vp, on the fudden, to ferue ar Sea? For, our ordinary Land multers, are generally intended, or, now may be fpared, to be employed otherwife, if nede be . I think, 1 hate fo hard, out of fome book, written $\mathcal{D e}_{e} \mathfrak{R e}^{-}$ publica.
\#How many Hundreds of lufty and handfome Men, wold be (this way well occupied : and haue needfull maintenance : Which, now , are
either Idle, or, want fuftenance : or, both : In to to many places, of this renowmed Monarchy ?

IMoreover, what a Cumfort and Sauegard, will it, or may it be, to the whole Realme, To have the great Aduantage of fo many warlike Ships, fo well manned and appointed ( for all affayes) at all houres, ready to affrone ftraight way, fet on, and ouerthrow, any fudden or priuy forreyn Trechery : by Sea (directly, or indirectly) attempted agayntt this Impire : in any Coaft or parte therof ? For, fudden forrein Artempts (that is to fay, vnknowen or vahard of to vs, before their Readynes) can not be done, with great power : For, great Nauies, moft commonly, are efpyed, or hard fomwhat of, and that very certainly, while they are in preparing : though in the meane while (politikly) in diuers places, they diftribute their Ships, and their preparations appertaining.

And, by reafon of the forefayd Pety Nauy Royall, Yt thall, at all tymes, not onely lye in our hands, greatly to dippleafe and pinch the Pety forrein Offender, at Sea : but alfo (yfiuft occafion begeuen) A.iij.
(note the triangular island pointing towards a river that heads northeast and opens into a circular gulf)



Calendar Treatise,
Written at the request of Queen elizabeth
and The Privy Council.
Hand Written by John Dee.
(Courtesy of the Bodleian Library, University of Oxford











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reproduction of Dee's original Dial of Time
(Courtesy of the Bodleian Library, University of Oxford MS Ashmole 1789 fol. 11r)

## Calendar Treatise

A Plain Discourse and humble advice for Our Gracious Queen Elizabeth, her most Excellent Majesty, to praise and consider the needful reformation of the Vulgar Calendar of Civil Years to reconcile the Days in accordance with the time which has truly been spent.

In the Method of this present consideration of time, the true place of any planet or other Star is determined by a straight line Imagined to pass from the Center of the Earth through the Center of the body of the planet or other Star, up unto the first and highest heavenly Convex Superfice [surface].

And wherever the upper End and Mathematical point of that imagined line is, there the true place of the Star or planet is esteemed and reckoned to be.

As any Planet or other Star moves either forward, backward or sideward, so continuously the upper End of said line determines the true place of that planet or Star.

The Sun has such pre-eminence that the Uniform and constant trace of the continual course of its line in the heaven is the Principal circular circumference to which the motions of all the other Planets and Stars are compared (their distance away from the Sun's course in latitude).


＊As may here be understood by the circle noted by the letters
$\mathrm{A}, \mathrm{B}, \mathrm{C}$ ，and D．

## $\Delta$ Noted here by the Red Circle A I B K

The north Pole is signified here by the prick at the letter E and the south Pole by the Prick at F．

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 And they are noted by the letters G and H ．
\(\nabla\) Designated by the two letters A and B ．
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That imagined Circumferential trace of the Sun＇s way in the heaven is called the Ecliptic＊，which very anciently has been called the Bias line．This Bias line is considered in respect to another great circumferential line in the heaven called the Equinoctial line or some－ times the Aequtor（in Latin）or Equicialis $\Delta$ ．

The Aequinoctial line is the very Middle circumference be－ tween the two known Poles of the World $⿻ 丷 木$（or of the most Uniform and Unalterable daily Motion of the heaven westward）．But the Poles of the one other motion of the Sun＇s Circle（besides the Ecliptic circle） are somewhat distant from the known Poles of the World．

The Poles of this other due Motion（besides the Sun＇s Circle or Ecliptic circle）are somewhat distant $\bowtie$ from the known Poles of the World，presently by about 23 degrees and 28 minutes．

Thus the Sun＇s circle or Ecliptic is Biased to the Equinoctial Circumference，and they cross or cut each other in two places（or op－ posite points）．These opposite places（or Mathematical points）we call the Equinoctial pricks or Points $\nabla$ ．

Throughout the world，the Sun rises and sets in 24 hours（and a few minutes more）．When the sun is at those two said Points，Days and nights are Equal．The Sun is under the Horizon for as long as it is above the Horizon（over the course of a whole Day）．When the Sun comes to either of these Equinoctial Points there is no difference between the lengths of Day and Night．

Just as these two great circles cut each other in two places, so also do they part or run from each other on both sides of these Equinoctial Points. (I mean on the North Side and on the South Side.)

The greatest distances that these two circumferences are from each other is called the greatest Declination $\Delta$ of the Arc of the Sun (either northerly or southerly).

In Common Astronomical speech (and for good reason), we say the Sun's circle (or the Ecliptic Circle) declines and is Biased from the Equinoctial. (We don't say the Equinoctial declines from the Ecliptic.) The Pricks or places of the Ecliptic that are most distant from the Equinoctial are called the Tropic or Turning $\square$ pricks. [in Greek, trope means turning]

When the Sun has digressed (as it were) from the Equinoctial as far as it can to these uttermost Points, it seems to turn again toward the Equinoctial. (The Sun goes so in his own course and circle, and it always moves forward in a perfectly circular circumference.)

Of those two Equinoctial points, the one the Sun approaches in March is called (in our Region) the Spring :: Equinox or the Vernal Equinox or Vernu 米 Punctum Aequinoctiale or the beginning of the Sign or Dodecatemorium of Aries.

The point which is opposite to it is called the Autumnal Equinox or the beginning of a Libra $\bumpeq$.

Each of the two Tropic Pricks are also called Solstices, which means "the Sun's stay." (the declination increases no longer.)

One we call the Solstium Aestivale or Solstiale Punctum Aestivale $\Delta$ or Tropicum Punctum Cancri $\sigma_{0}$ [the sun reaches the Tropic of Cancer].

The other we call the Solstitium Hiemale or Tropicum Punctum Capricorni $\mathbf{Z}$ [the sun reaches the Tropic of Capricorn]

This Summer Sunstay prick, which the Sun enters in June, we also call Initium Cancri ${ }^{\sigma}$.

The Wintery Sunstay point, which the Sun enters in December, we call the beginning of Capricorn.
$\Delta$ This is shown as Arc CI or Arc KD

「 Noted by the Letters C and D .
$\because$ Noted by the letter A

* From which prick begins continually the division of the Ecliptic into Equal parts called degrees of which 30 make a sign or a Dodecatemorium. - Noted by the letter B.
$\Delta$ To be understood by the letter C.
$\mathbf{Z}$ Understood by the letter D

Those who are not well-acquainted with these terms should remember or make note of them. These speculations are the reason for the matter at hand:

## The due Reformation of our Circle year according to the true and Natural year.

Thus we may begin.
There are two sorts of years to be considered here. One is the Annus Solaris or Annus Vertens [in Latin, verto means to turn] Annus Tropicus. The other is called the Annus Civilis or Annus Julianus.

We will start with a description of the Annus Solaris.
A Sun Year $\simeq$ is that Periodical space of time which is spent in the Sun's motion along the Ecliptic between that Moment of time when the Sun is deemed to have a place in any prick or point of the 360 degrees of the Ecliptic line and that other Moment in time when it is reckoned to come again to the first prick or point. (These pricks can be either the Equinoctial or Tropical pricks or a prick at any given distance from the four principal pricks.)

The Annus Civilis is also called Annus Julianus because Julius Caesar was the first to order the civil year and establish it by public edict.

Here is its definition:
A circle or Vulgar year is the space of 365 Nightdays and six usual hours. I call them Nightdays imitating the apt Greek name Nycthemere
~- or Nycthemeros [Nyct means "night" and emeros means "day"]
Jointly between both the time of the Dark and the time of the Light is about 24 usual hours. Mention is made of this at the Creation: Est Vespere et Mane Dies Unus. [And there was evening, and there was morning, the first day. Genesis 1:5]

Every since Creation, that Light has been given the name of Dies [Day] by God's own appointing, as Moses was taught to Record by the Holy Ghost. Appellavit Lucem Diem, et Tenebros Noctem [Call the Light Day and the Dark Night].

Thus you see (in this way), how this double Manner of terming Day is anciently grounded. But only one manner of Night is Ordained. At the Creation, there were not two darknesses noted.

The pre-eminence or priority in time assigned to the darkness or evening time is called Night.

Likewise, the morning celebrated that which was called Day.
Thus, Vespere and Mane made Dies Unus.
["Evening and Morning" made "One Day"]
And one Nightday (the Nycthemere or Nycthemeros) is comprised of this dark Night and the light Day $\sim$.

Thus, it must be admitted that these names are not of our Novelty.
Julius Caesar, with the help of the Mathematician Sosigenes, commanded and established the Quantity of the Civil year to be 365 days and 6 hours.

They verily thought that this Quantity of time answered to the true and heavenly year of the Sun's course (not a minute more or less). So, they made an adjustment to account for those odd six hours.

In our Civil Acts and Affairs these odd hours can not be utterly neglected, or unreckoned or not considered). In four Civil Years, these 6 hours amounted to 24 hours, the Quantity of a usual NightDay てー.

So every fourth vulgar year, a NightDay was added in the month of February of the Roman Calendar, so that fourth year contained 366 days. We commonly call this a leap year by reason of the Dominical letter (Ecclesiastially ordained), leaping or changing only one certain day in February.

Julius Caesar placed the day at Sexto Kalendas Martiy or the sixth of the Kalends of March. The month of February that usually had 28 days was made to have 29. Thus, a leap year was called Annus Bisixtilis.

> The Romans used distinct Names for days of the week.
> Dies Solis (or Dominiea) [Sun Day]
> Dies Luna [Moon Day]
> Dies Martis [Mars Day]
> Dies Mercurii [Mercury Day]
> Dies Jovis [Jupiter Day]
> Dies Veneris [Venus Day]
> Dies Saturni [Saturn Day]

They did not note the days as we do with A, B, C, D, E, F, G.
The Romans divided their day into Calends, Nones, and Ides.
I set forth these Days for a better understanding of the Roman Custom. But the Resolution to have Septenarie of Days (that is, the account of time by weeks) is of much greater antiquity (in this World of continuance).

The first Chapter of Genesis sufficiently declares the beginning of this orderly accounting by Seven. In the Scriptures it is very often expressed. In the Judaical month this week of Number of Seven days has been used by the phrases:

| Teria Prima, | or Prima Sabbati, |
| :---: | :---: |
| Teria Secunda, | Secunda Sabbati, |
| Teria Tertia, | Tertia Sabbati, |
| Teria Quarto, | Quarta Sabbati, |
| Teria Quinta, | Quinta Sabbati, |
| Teria Sexta, | Sexta Sabbati |
| and Teria Septima | and Sabattium. |

Dies Solis, Dies Lunas and the other Dies with Planetary names came to Christian knowledge by the use of the Doctrine of the Chaldeans.

Note
Long after the time of Christ, men have labored to compare the two kinds of years previously described.

It was found by the records of two thousand years that Annus Julianus (365 days and 6 hours) actually exceeds and has exceeded the length of the true natural Sun Year by some minutes of an hour.

Though these various ages the length of the Sun's Year did not, does not, and will not be the same length of time for any two consecutive years, the yearly difference is quite small (in our age, as well as in Ptolemy's time), being less than 15 sec onds of an hour.

This is a very small portion of time when to be reckoned with the Artificial or Mechanical breadth of an hour line drawn on a Sun Dial. No mortal man's eye can discern this Quantity of a Mechanical time breadth of the moving or shifting of the place of the Indicating Shadow. But it actually does move and shift....
[...Over time] any man can discern and no man is so void of Reason to deny the Motion passed to have been great...
...Yea (as I said before) the Arithmetical and proportional account can be given of the Motion passed various uses of this can be devised consequently or Porismatically (as the Greek word is porismatikos).
[porisma means a deduction or corollary from a previous demonstration]
This Dial (which is divided into 360 equal parts) shows the time spent since the beginning of all time and the creation of time. Every one of these Astronomical Philosophers I have shown here have studied the length of the year.

The Astronomical observations of one man might easily be doubted, but of diverse men's observations (diligently made) in great length and distance of time (as in Centuries of years or more), very certainly, it is now demonstrable so to be.


Clarifying Notes for Dee's "Dial of Time"
The "Dial of Time" goes from Adam, Enoch and Noah,
through the founding of Jerusalem, the Greek era, the time of Jesus and Ptolemy, then highlights several famous astronomers of the Middle Ages and the Renaissance.
It ends with Queen Elizabeth who Dee touts as the "Reformatrix" (female Restorer) of the Year,
thereby introducing the next great Christian epoch.
[if she reforms the calendar, as Dee is heartily encouraging her to do]

Genesis $5: 5$ says Adam lived for 930 years
Genesis 5:23 says Enoch lived for 365 years
The Atlantic War took place in the mountains of Northern Africa.
Meton and Eucteman were famous Greek Astronomers who lived around 400 BC.
Hipparchus lived around 150 BC .
Ptolemy lived around 140 AD.
Al Kindi lived around 850 AD .
The English astronomer Simon Bredon (from Oxford) lived around 1350 AD.
Copernicus lived around 1525 AD.

Phaedo, a follower of Socrates, opened up the Elian School around 450 BC
(in his home town of Elis, Greece, about 125 miles west of Athens)

## There's lots more...

Dee continues with over 50 more pages of technical astronomy relating to how the Julian Calendar has fallen out of line with the calendar of the heavens. He provides detailed data from all his main sources; Meton, Euctemon, Hipparchus, Ptolemy, Al Kindi, Simon Bredon, and Copernicus.

He warns that, without reform, Easter might be celebrated on an incorrect date. And he shows how the great astronomers like Regiomontanus of Konigsburg [Prussia] had come to the same conclusions.

Dee delivered his 62 page proposal to the Court on February 26, 1583.
Upon reading Dee's proposal the Privy council was enthusiastic about the calendar reform. Walshingham responded to Dee expressing his appreciation. Even the skeptical Cecil was on board. All that was needed was the approval of the Archbishop of Canterbury, Edmund Grindal.

Wooley reports that Cecil insisted a decision be made promptly, before November of 1583.

Grindal (who was at odds with Queen Elizabeth regarding other issues) probably never properly digested Dee's technical report.

He wrote the whole idea of calendar reform off as a "Papist" and said the matter must first be approved by all the Protestant Churches throughout Europe. Grindal knew full well this would never happen, especially in a matter of months, so he had effectively quashed the whole idea.

Dee was furious that Grindal couldn't see what was so blatantly scientifically accurate and obvious. Nonetheless, England did not reform its calendar. It wasn't until until 1752 that England finally adopted the Gregorian Calendar. During those 170 years, communications and trade agreements generally had two dates: Old Style (OS) and New Style (NS).

Had Grindal been a little more open-minded, it would have saved 170 years of communication aggravations. But to Dee, even more exasperating was the fact that England's "Civil Time" remained out of sync with the "true" time of the cosmos.

Cecil might have been in a rush to settle the matter before November so that Englandwould stay in step with the rest of Europe. Italy had changed in October of 1582 (October 4 became October 15), France followed on December 9,1582, and Holland on January 1,1583.

However Cecil might have been anxious to have England's change calendars to coincide with the settlement of the Gilbert/Peckham//Dee colony at the John Dee River and port. Perhaps, following Dee, he wanted the New Colony in the New World to commence in the New Time.
(Anthony Brigham's mission (with its two ships and a pinnace) had departed from England in April of 1582. Gilbert's delayed mission (with 5 ships) finally depatrted in June of 1583.)

## Dee the poet

There are two other noteworthy parts of the Calendar Treatise: two poems penned by Dee. As a introduction, Dee wrote four couplets to Lord Burghley. Perhaps he is referring to them in the title of this illustration (which preceeds them). Dee's depiction of the universe is clearly Trinitarian. YHWH (Jehova) radiates from three corners of the equilateral triangle, governing the earth, the 7 planets, and the fixed stars.

Along the edges are three biblical quotes that relate to Time. The title and the graphic are a curious mix of Quaternary and Ternary (particularly the three strange asterisks after the title).


TO OTI, and TO DIOTI,
I show the thing, and reason why.
At large, in brief, and middle wise, I humbly give a plain Advice.

For want of time, The Time Untrue, If I have missed, Command anew.

Your Honor may; So shall you see, That Love of Truth, doth govern me.

To conclude, Dee writes this poem comparing himself and Elizabeth to Sosigenes and Caesar.

As Caesar and Sosigenes, The vulgar calendar did make. So Caesar's Peer, our true Empress, To Dee, his work she didt betake.

To find the Days superfluous, (Which Caesar's false hypothesis, Had Bred, to Nature, odious) Wherein, he found eleven amiss.

For he, from Christ, Chief Root of time The time did try, by heavenly writ: No Council can deem this a crime From Christ, to us, true time to fit.

Elizabeth our Empress bright, Who in the year of eighty three, Thus made the truth come to light, And Civil year with heaven agree.

But eighty four, the Pattern is Of Christ's birth year, and so for ay? Each Bissext shall fall little miss, To show the Sunn of Christ's birth day.

Three hundred years, shall not remove, The Sun, one day, from this new match. Nature, no more shall us reprove Her golden time, for all to watch.

The God of might, our father dear, Whose reign no time can comprehend, Good time our Elizabeth grant here And Bliss eternal, at her end

Amen

The Compendious Rehearsal, of John Dee, his dutiful declaration and proof of the course and race of his studious life, for the space of half of a hundred years, now, by God's (favor and help) fully spent, etc.<br>(THE COPY OF THE FORESAID SUPPLICATION TO HER MOST EXCELLENT MAJESTY)

Crossley's

Most gracious Queen,
Forasmuch as the intolerable extremity of the injuries and indignities, which your most excellent Majesty's faithful and dutiful servant, John Dee, has for some years last past endured, and still endures, is so great and manifold, as cannot in brief be expressed to your Majesty, neither without good proof and testimony have credit with your Majesty.

And because also, without speedy and good redress therein performed, it is to be doubted, that great and incredible inconveniences and griefs may ensue thereof in sundry sort; (which yet may easily be prevented) your Majesty's foresaid most humble and most zealously faithful servant beseeches your Majesty to assign two or more meet and worthy persons, nobly and virtuously minded, who may and will charitably, indifferently, advisedly, and exactly see, hear, and perceive, at the house of your Majesty's said servant in Mortlake, what just and needful occasion he has thus to make most humble supplication to your Majesty.

And so of things there seen, heard, and perceived, to make true and full report and description unto your Majesty. And thus your Majesty's foresaid most dutiful servant beseeches the Almighty God most mercifully, prosperously, and always to bless and preserve your most excellent Majesty royal. Amen.

November 9, 1592.
Be it remembered,
That this Supplication being exhibited unto her Majesty by the honorable Countess of Warwick on November 9th and read by her Majesty's self. Thereupon her Majesty immediately appointed the honorable Mr. Secretary Wolley, and Sir Thomas Gorge, Knight, Gentleman of her Majesty's Wardrobe, to be the two Commissioners, according to the tenor of this Supplication.

And so, the foresaid two honorable Commissioners came on November 22nd, 1592 to my house at Mortlake to see, hear, and perceive some things, according to the intent of the former Supplication. To whom being set at one table in the middle of my late library-room, and next before them two other great tables, being covered.

One, with very many letters and records of fifty years course, and testimonies of my studious life, in and from the most famous places and parties of all Christendom.

And the other with such diverse books of my making, printed and unprinted, as I had in my foresaid time written or devised: then I did begin my declaration, concurring orderly with the text of this book, purposely and by the Commissioners' advice, in some order of method most briefly and speedily contrived against this day.

## CHAPTER I. <br> THE ENTRANCE AND GROUNDPLAT OF MY FIRST STUDIES.

In November of the Year1542, I was sent by my father, Rowland Dee, to the University of Cambridge, there to begin with logic and so to proceed in the learning of good arts and sciences (for I had before, in London, and at Chelmisford, been properly well-furnished with understanding of the Latin tongue): I being then somewhat above fifteen years old, as being born July 13, 1527.

In the years $1543,1544,1545$, I was so vehemently bent to study, that for those years I did inviolably keep this order; only to sleep four hours every night; to allow to meat and drink (and some refreshing after) two hours every day; and of the other eighteen hours all (except the time of going to and being at divine service) was spent in my studies and learning.

After I was Bachelor of Art, I went beyond the seas (May, 1547) to speak and confer with some learned men, and chiefly mathematicians, as Gemma Frisius, Gerardus Mercator, Gaspar à Mirica, Antonius Gogava, \&c.

And after some months so spent about the Low Countries, I returned home, and brought with me the first astronomer's staff of brass, that was made of Gemma Frisius' devising, the two great globes of Gerardus Mercator's making, and the astronomer's ring of brass, as Gemma Frisius had newly framed it; and they were afterward left by me for the use of the Fellows and Scholars of Trinity College. Some proof hereof may appear by the letters of Mr. John Chistoferson, who afterward was Bishop of Chichester elect.

In this year of 1547, I began to make observations (very many to the hour and minute) of the heavenly influences and operations actual in this elemental portion of the world. Of which sort I made some thousands in the years then following: as may appear by my own writing in my Ephemerides, and in sundry other books purposely recorded and here lying before your Honor.

After St. John's College, I was chosen to be Fellow of Trinity College, at the first erection thereof by King Henry the Eight. I was also assigned there to be the Under-Reader of the Greek tongue, Mr. Pember being the chief Greek Reader then in Trinity College. Hereupon I did set forth (and it was seen of the University) a Greek comedy of Aristophanes, named in Greek Eì $\dot{\eta} v \eta$, in Latin, Pax; with the performance of the Scarabeus his flying up to Jupiter's palace, with a man and his basket of victuals on her back: whereat was great wondering, and many vain reports spread abroad of the means how that was effected.

In that College also (by my advice and by my endeavors, diverse ways used with all the other Colleges) was their Christmas-Magistrate first named and confirmed an Emperor. The first was one Mr. Thomas Dunne, a very goodly man of person, stature, and complexion, and well learned also. They, which yet live, and were hearers and beholders, they can testify more, then is meet here to be written of these my boyish attempts and scholastic exploits.

In the Year 1548, I was made Master of Art, as may appear by the University's testimony under their scale, lying here on the table.

In the year 1548, I went over beyond the seas again, and never after that was I any more student in Cambridge: as may appear by the whole course of my life after that, manifestly testified by the letters and other records here before you.

I became a student at Louvain in 1548 at mid-summer, and there I made abode until July 15,1550 , as appears by the notes of my Ephemeredes, and diverse letters sent to me from diverse parties, as being known to be at Louvain then.

## CHAPTER II. HEREUPON FOLLOWED MY GOOD ESTIMATION AND CREDIT IN MATTERS OF GOOD LEARNING, BOTH ABROAD AND AT HOME IN ENGLAND. ABROAD AS FOLLOWETH:

Beyond the seas, far and near, was a good opinion conceived of my studies philosophical and mathematical. First, from Louvain did the favorable fame of my skill in good literature so spread, that thereupon diverse noblemen (Spaniards, Italians, and others) came from the Emperor Charles the Vth, his court at Bruxelles to visit me at Louvain, and to have some proof of me by their own judgements: So came the Duke of Mantua to me: so came Don Luys de la Cerda, afterward Duke de
Medina Coeli in Spain, unto me: so came to me, after them, from the Emperor's court at Brux-

Crossley's page 7 ells, the honorable Sir William Pickering, Knight, and there with me remained some time, and of me was instructed in logic, rhetoric, arithmetic, in the use of the astronomer's staff, the use of the astronomer's ring, the astrolabe, in the use of both globes, \&c.

Then came some out of Bohemia to me, with strange and no vulgar opinion, settled in their imaginations, of my skill, as may appear by the Record of some part of the History in my Ephemerides noted.

Then came some out of Denmark to me, as Mathias Hacus, Danus, Regis Daniæ Mathematicus; Joannes Capito, Medicus Regis Daniæ, and a good mathematician also; as by letters lying on the table is evident.

There, for recreation, I looked into the method of the civil law, and profited therein so much, that in antimonies, imagined to be in the law, I had good hope to find out (well allowed of) their agreements; and also to enter into a plain and due understanding of diverse civil laws, accounted very intricate and dark. Of that my study in the law your honor hath on the table the testimony of the University of Louvain; and by other letters unto me about that time it may appear.

From Louvain I took my journey toward Paris on July 15, 1550, and came to Paris the 20th day of that month. Where, within a few days after (at the request of some English gentlemen, made unto me to do somewhat there for the honor of my country) I did undertake to read freely and publicly Euclid's Elements Geometrical, Mathematicè, Physicè, et Pythagoricè; a thing never done publicly in any University of Christendom.

My auditory in Rhemes College was so great, and the most part elder then my self, that the mathematical schools could not hold them; for many were glad just to be able to peer in the window of the school the windows, to be auditors and spectators, as they best could help themselves thereto.

I also dictated upon every proposition, beside the first exposition. And by the first four principal definitions representing to the eyes (which by imagination only are exactly to be conceived), a greater wonder arose among the beholders, than of my Aristophanes Scarabeus mounting up to the top of Trinity-hall in Cambridge ut supra. Of this mathematical reading very many testimonies lie here before you.

In that University of Paris, were at that time above forty thousand accounted students; some out of every quarter of Christendom being there. Among these very many of all estates and professions were desirous of my acquaintance and conference, as Orontius, Mizaldus, Petrus Montaureus, Ranconetus, Danesius, Jacobus Sylvius, Jacobus Goupylus, Turnebus, Straselius, Vicomercatus, Paschasius Hamelius, Petrus Ramus, Gulielmus Postellus, Fernelius, Jo. Magnionus, Johannes à Pena, \&c. as by letters lying on the table may partly appear.

There I refused to be one of the French king's mathematical readers, with 200 French crowns yearly stipend offered me, if I would stay for it; I refused likewise a good stipend of Monsieur Babeu; and a better than that, of Monsieur de Rohan; and a better than that, of Monsieur de Monluc, who was then sent ambassador to the Great Turk.

And not only in Louvain and Paris Universities has God sent me good credit and estimation with the favor and love of very many (noble lovers of good learning, or well learned themselves), but also iin Orleans, Cologne, Heidelberg, Strasburg, Verona, Padua, Ferrara, Bologna, Urbino, Rome, and (to conclude herein) in many other universities, cities, and towns of Christendom; as may appear by the multitude of letters and other records lying here to be seen and perused in this case; from the year 1547 till and in this present year of 1592.

A sufficient proof of my great foreign credit

To be most brief concerning my foreign credit, it may suffice me, a poor studious gentleman, for my foreign credit for ever; that in this tract of my studious race I might have served five Christian Emperors; namely, Charles the Fifth, Ferdinand, Maximilian, this Rodulph, and this present Muscovite: of every one their stipends directly or indirectly offered, amounting greater each, then other; as from 500 dollars yearly stipend to a 1000, 2000, 3000; and lastly, by a Messenger from this Russian or Muscovite Emperor, purposely sent, with a very rich present, unto me at Trebona castle, and with provision for the whole journey (being about 1200 miles from the castle, where I lay) of my coming to his court at Moscow (with my wife, children, and my whole family) there to enjoy at his Imperial hands $£ 2000$ sterling yearly stipend; and of his protector yearly a thousand rubbles; with my diet also to be allowed me free out of the Emperor's own kitchen: and to be in dignity with authority among the highest sort of the nobility there, and of his privy-counselors, \&c.

Of this last great preferment offered, many Englishmen, yet living, and in this kingdom, be witnesses: the Landgrave of Hesse-Cassell his letter is ready to be showed, and other letters of men of credit can be sufficient testimony; besides the forerunner to seek me, and the ambassadors or messengers, their own writings thereof rest here before you.

Note: the Commissioners jointly read two of the testimonies of the Muscovite's great offers and promise.

## CHAPTER III. <br> MY CREDT AND ESTIMATION IN ENGLAND, FOR THE MOST PART OF THE FORMER WHOLE RACE.

That may also appear evidently even from the beginning and original of it, with the increase thereof ensuing:

1. In the year 1547, by the letters of Mr. John Christopherson, afterward Bishop of Chichester, elect.
2. In the year 1548 , by the University of Cambridge their letters testimonial, with their seal annexed.
3. By Mr. Cheke (afterward knight, and one of King Edward the Sixth's schoolmasters) whose good liking of me declared to Mr. Secretary Cecill (now the right honorable Lord Treasurer of England) was notified unto me by the letters of Mr. Peter Osborne, late Remembrancer of the Exchequer; and by the same I was sent for to come to the speech of the said Mr. Secretary on December 12, 1551, which I did, and yet I remember whereof his discourse with me then.

Crossley's
page
10
4. By King Edward his voluntary gift of a pension on a hundred crowns yearly; and after that, bettering that pension with bestowing on me (as it were by exchange) the rectory of Upton upon Severn; a sufficient testimony of his Majesty's presenting me to that rectory lay here, with an authentic seal annexed to it. May 19, 1553.
5. Mr. Secretary Cecill,now Lord Treasurer, his testimony by letter of my well bestowing of my time beyond the seas on May 28, 1563, is here.
6. I must highly esteem her Majesty's most gracious defending of my credit, in my absence beyond the seas, as concerning my book, titled Monas Hieroglyphica (dedicated to the Emperor Maximilian, in the Year1564) against such University-Graduates of high degree, and othere gentlemen, who therefore dispraised it, because they understood it not. Whereupon her most excellent Majesty (after my coming home from beyond the seas; when also I brought the Lady Marquess of Northampton from Antwerp by sea to Greenewhich) did vouchsafe to read that book obiter, with me at Greenewich.
7. Of the University of Oxford, some of the chief students (Doctors of Divinity and Masters of Art) caused a yearly good stipend to be offered unto me to read the mathematical sciences there. Mr. Doctor Smith of Oriel College, and Mr. Dr. Bruarne fo Christ's Church, were chiefly agents in that cause: In the Year1554.
8. Mr. John Wolly his very courteous letters to me on June 8, 1568, who is now even your honor, the only Secretary for the Latin tongue to her most excellent Majesty, and one of her Majesty's privycouncil; and here this day the chief Commissioner in my present most lamentable case of distress.
9. Mr. Secretary Cecill, now Lord Treasurer of England, his honorable offer of his courtly friendship by a letter written with his own hand on August 20, 1568.
10. The honorable Earl of Oxford his favorable letters in 1570.
11. Her Majesty's very gracious letters of credit for my marriage in 1575.
12. The right honorable Earl of Leicester's letters for the same.
13. Mr. Christopher Hatton (afterward Lord Chancellor of England) his letters for the same.
14. Her Majesty's favorable license and passport, with my two servants and our geldings in 1571. Two other Kings, their ambassadors (Leidgiers here) their passports at the same time, for free and safe traveling in their Prince's dominions, etc..
15. Sir Henry Sydney's honorable letters to me, while he was Lord Deputy in Ireland. Sir Henry Sydney's letters unto me, when he was Lord President in Wales.
16. The honorable Lady Sydney's most courteous and many letters to me, and inviting me to court, etc. in 1571.
17. Mr. Doctor Julius Cæsar's letters to me (who now is Judge of the Admiralty, and one of the Masters of Requests extraordinary) in 1577.
18. Sir Francis Walsingham his passport for my winter journey, in her Majesty's weighty affairs in 1578.

Omitting herein very many letters, and other things, testifying my honest credit here in England (with all degrees of the Nobility, Gentlemen, and University-Graduates), in and for the most part of all my studious race, these may suffice.

## CHAPTER IV <br> SOME OTHER OF HER MAJESTY'S SPECIALLY GRACIOUS AND VERY BOUNTIFUL FAVORS TOWARD ME.

1. At her most excellent Majesty's first coming to Somerset house, her Majesty was willing, that, after Dr. Mallet, I should have had the Mastership of St. Katharine's, wherein Dr. Willson politically prevented me.
2. Her Majesty very graciously took me to her service, at Whitehall before her Coronation, being to her Majesty commended by the right honorable Earle of Pembroke, and the Lord Robert, after

Crossley's Earle of Leicester. At which time her Majesty used these words unto the said Lords, "Where my brother has given him a crown, I will give him a noble."
3. After this some years, at the Lady Marquess of Northampton her humble suit for me on December 8,1564 , her Majesty granted to me the Deanery of Gloucester, being then void: and a caveat was entered on my behalf; but the same deanery was afterward bestowed on one Mr. Man, who was sent to Spain in her Majesty's service.
(And now this Lent 1594, when it became void again, I made motion for it, but I came too late; for one, that might spend $£ 400$ or $£ 500$ a year already, had more need of it, then I liked; or else my former gift was but words only to me, and the fruit ever due to others, that can detect and catch better than I could do for these thirty-five years.)
4. Not long after, the Provostship of Eaton by some my friends in court, was humbly at her Majesty's hands sued for to my behalf, and favorable answers were given therein.
5. Her Majesty willed Mathew, Lord Archbishop of Canterbury, to grant me a dispensation for ten years, to enjoy the two rectories of Upton and Long-Lednam, and any other within that term, of me gotten. Which dispensation I enjoyed for only those two rectories.
6. After my journey into the dukedom of Loraine in 1571 , in my very dangerous sickness I received chief help and comfort by her Majesty's great favor toward me, not only sending carefully and with great speed from Hampton Court unto me Dr. Apsloo and Mr. Balthrop (who faithfully and prosperously did their parts of skill with me), but also in sending the honorable L. Sidney in a manner to tend on me; to discern, how my health bettered, and to comfort me from her Majesty with divers very pithy speeches and gracious, and also with divers rarities to eat, to increase my health and strength: the most dutiful and thankful memory whereof shall never die.
7. Her Majesty's most gracious offer was sent home to my house by Mistress Blanche à Parry of any whatsoever ecclesiastical dignity within her kingdom, being then or shortly becoming void and vacant, to make me owner: when both bishoprics and deaneries were void, and more became shortly after void: but my most humble and thankful answer to her Majesty by the same messenger, was, that, cura animarum annexa [being responsible for the " caring of souls"] did terrify me to deal with them.
8. Her Majesty not long after, as your Honor, Mr. Secretary Wolley, can well remember and testify, for some better maintenance for me, then of those two rectories only, which I then had, declared her most gracious will and pleasure to be, that I should have of her Majesty's gift other ecclesiastical livings and revenues, (without cure of souls annexed) as in her Majesty's books are rated at two hundred pounds yearly revenue. Of her Majesty's gift, I never as yet had any one penny.
9. Her Majesty (the last day of July, 1583) being informed by the right honorable Earle of Leicester, that whereas the same day, in the morning, he had told me that his Honor and the Lord Laskey would dine with me within two days after. I confessed sincerely to him, that I was not able to prepare them a convenient dinner, unless I should presently sell some of my plate or some of my pewter for it. Whereupon her Majesty sent to me very royaly within one hour after forty angels of gold, from Syon, where her Majesty had recently gone, by water from Greenewich.

What can better witness her Majesties most gracious goodwill and desire to further my studies in her service than this parcel of her Majesties speech uttered the same day to another such a one as you may see in the letter itself he wrote

The great seal by negligence still wanted; for of course it was to have been put to within a certain time after
10. Her Majesty by Mr. Christopher Hatton's letters (afterward Lord Chancellor of England) signified to Edmond, Lord Archbishop of Canterbury, his good grace (in 1576) that her pleasure was, "That, in any case, I should, during my life natural, be dispensed with to enjoy those two rectories of Upton and Long-Lednam," which I then had.

Thereupon at length (later, in 1582) the said Archbishop performed his part and set his seal thereto. But when I should have followed the getting out of the great seal unto it, I was wholly employed (at her Majesty's and the right honorable the Privy Counselors, their commandment) about the Reformation of the Calendar.

Which office anciently did appertain to the bishops, and I would now they had showed their skill therein then; so would they have made more account now to help him up, who fell into the loss of above a thousand pounds since (The loss of the two Rectories is of more loss in rent due and for time of life to come than $£ 1000$ ) for not following his own business, but was occupied to bear their burden; indeed at her Majesty's commandment, and not at theirs. Also I had small thanks at their hands any way, nay, great hindrance; seeing her Majesty's absolute intent and caveat to my benefit was no better regarded among them in due time.
11. Her Majesty most graciously both for my great credit increasing and confirming, as well abroad as at home; and also of the better safety of me and mine to come so long and dangerous a journey and voyage in (as from the farthest parts of the Kingdom of Bohemia, hither); sent her most princely and royal letters of safe conduct for me, my companion, and our families to all foreign Princes and Potentates, etc. in 1588, the copy whereof I received from your honor, Mr. Secretary Wolley.
12. Since which my last coming home into England, her Majesty a little before Christmas in 1590, hearing of my great want of ability to keep house accordingly, as by all reason might be expected at my hands, did presently declare her most gracious good intent and will to help me with one hundred pounds of money out of her Majesty's privy purse.

This intent and promise, some once or twice after, as I came in her Majesty's sight, she repeated to me; and thereupon sent to me fifty pounds to keep my Christmas with that year; but what is become of the other fifty, truly I cannot tell. If her Majesty can, it is sufficient: Satis citò, modò satis bene, must I say. ["enough quickly is just well enough," in other words, getting some of the money promptly was better than getting all of it simply promised at a later date]
13. And shortly after her Majesty very graciously sent her will and pleasure in the right honorable Lord Treasurer his letters to this present Lord Archbishop of Canterbury, his good Grace, that he should "take some order for my present maintenance."

Here is the copy of the very letters, as I had it by my Lord of Canterbury's commandment: but yet no penny of rent, fee, or revenue is bestowed on me, being now almost two years since. (And not it is more than three years and three months since, and not yet any farthing of certain fee or revenue will be found or gotten for me.)
14. Again, seeing no present help was yet come in 1592, in April last, but want and discredit grew more and more upon me: thereupon my friends devised a suit to her Majety for me, by obtaining whereof chiefly her Majesty might be found my gracious and very favorable sovereign Lady.

Secondly I thereby might win some credit; as with all men generally, who should understand of such her Majesty's good and gracious favor toward me, her ancient servant; and especially with my creditors, who would wish that my present little ability should be much amended thereby.

And so it came to pass by her Majesty's very bountiful purpose in giving unto the right worshipful Doctor Aubrey, one of the Masters of Requests, permission to endow me with a rectories, with vicarages, in St. David's diocese, when any of them shall become vacant. Thisindeed would have been only five of her Majesty's gift, and the yearly valuation of them five in one sum amounting to only $74 l, 11 s, 2 d$., and not so much better at this day, than their said valuation, that they may be accounted worth one hundred pounds to any thrifty occupier of them.

And yet some did unduly esteem them to be of great value. Indeed to this hour (April 10, 1594) there never came a penny unto me of them. Nor is it certain, whither ever or never they shall, but I am very certain about the charges sustained about the writings and seals belonging to them.
15. By reason hereof in the last years (1591) progress entering at Greenwich, her Majesty was informed by the honorable and very virtuous Countess of Warwick of my great wants still increasing. Her Majesty was then by the said Countess in most humble manner requested, to grant to me, upon the next avoidance, the Mastership of St. Crosse's by Winchester, being an office and living of much like quality as St. Katherine's.

Where unto her Majesty's most bountiful and provident answer was, "that I should have it, if it were a living fit for me," with which gracious answer I held my self contented, knowing that her Majesty had, or after that might have bishoprics enough vacant. Unto one of which the worshipful Mr. Doctor Bennet (the present incumbent of the Mastership of St. Crosse's) might be persuaded to be promoted unto by her Majesty; especially if the bishopric be of better living far, than S. Cross' or by commendams were hoped to be of better revenue.
(It is to be noted, that about after Doctor Watson: whereupon I hoped to have had that living long since; but at length I found that it was endowed to Dr. Bennet, better speeding than my former grant at her Majesty's hand. Mistress Blanche à Parry and Mistress Skydamore, now the Lady Skydamore, had obtained her Majesty's grant to me so long since.)
16. This year also again (1592 at None-such), the same suite was renewed unto her Majesty by the aforesaid Countess of Warwick: as well in respect of my incredible want of due maintenance, as for that the most Reverend Father in god, this L. Archbishop of Canterbury, his good Grace, very often times, and to diverse affirmed, and still affirms, that this Mastership of S. Crosse's is a living most fit for me, and I fit for it.

And also the right honorable Lord Treasurer, since that time and very lately at Hampton court, is of the same mind herein, as the Lord Archbishop is; as his Honor has very lately to my self declared: and with his hand very earnestly smitten on his breast used these very words* to me, "By my faith, if her Majesty be moved in it by any other for you, I will do what I can with her Majesty to pleasure you therein, Mr. Dee." And so I thanked his Honor humbly, and have great confidence in his Honor's very favorable promise.

* Mr Henry Maynard was by and heard the words at Hampton Court, in my Lord's own chamber, Nov. 6,1592

And the rather seeing her Majesty's last answer at Nonesuch was even as the first, "that I should undoubtedly have it, if it were fit for me;" and moreover willed, that a caveat should be entered for me thereupon, as a most gracious Queen, for the more assurance of her poor servants relief and comfort. Of which her Majesty's most gracious answer, the foresaid L. Archbishop his good Grace being then at the Court at Nonsuch, was made privy presently; and to the right honorable Lord Treasurer I have myself declared it lately at Hampton Court.
17. Since which time I hearing of bishoprics, some void, and some shortly to become void, and hearing of diverse nominated to be promoted to them; but hearing no speech made of Mr. Doctor Benet, a man very worthy and sufficient to be a bishop, I began to doubt, that her Majesty hitherto has not been given to understand fully the truth of my present very hard case and incredible distress, through unseemly want of all things necessary for due maintenance of me and mine, contrary to her Majesty's will.

Hereupon on Wednesday was a sevennight the honorable Countess of Warwick preferred my former supplication (set in the beginning of this little book) unto her Majesty, who very graciously did read it over herself, and granted the petition thereof; and so straight way nominated your Honor, Mr. Secretary Wolley, and you, Sir Thomas Gorge Knight, Gentleman of her Majesty's Wardrobe, as being very worthy and sufficient men, right nobly minded, to be the Commissioners, charitably, advisedly, and exactly to hear and see what I have to say or show unto you, needful to be considered of; so as speedy and sufficient redress and help may be had thereupon.

The Queen's Majesty with her most honorable Privy Council, and other her lords and nobility, came purposely to have visited my library; but finding that my wife was within four hours before buried out of the house, her Majesty refused to come in; but willed me to fetch my glass so famous, and to show to her some of the properties of it, which I did; her Majesty being taken down from her horse (by the Earl of Leicester, Master of the horse, by the Church wall of Mortlack), did see some of the properties of that glass, to her Majesty's great contentment and delight, and so in most gracious manner did thank me, etc.

The Queen's Majesty came from Richmond in her coach the higher way of Mortlake field, and when she came right against the Church, she turned down toward my house; and when she was against my garden in the field, here Majesty stayed there a good while, and then came into the street at the great gate of the field, where her Majesty saw me at my door, making reverent and dutiful obeisance to her; and with her hand her Majesty beckoned for me to come to her, and I came to her coach side; her Majesty then very speedily pulled off her glove and gave me her hand to kiss; and to be short, her Majesty willed me to resort oftener to her Court, and by some of her Privy Chamber to inform her Majesty when I am there, etc.

October 3, 1580. About 11 o'clock before noon I delivered my two Rolls of the Queens Majesty's title to her in the garden at Richmond; when her Majesty very graciously accepting of my endeavor and labor therein, appointed after dinner to hear further of the matter. Therefore between one and two in the afternoon, I was sent for into her Highness Privy Chamber, and whether the Lord Treasurer was also come before.

Then, upon her Majesty's rehearsing with his Honor my endeavors to satisfy her Majesty's desire to understand somewhat effectually of the title to foreign countries, and of my pains taken in those great Rolls penning down, required the Lord Treasurer to consider of the matter, the records, testimonies, and arguments by me there set down.

But thought he Lord Treasurer did seem at first to doubt of the value of the work, or pithiness thereof, her Majesty wished his Honor to peruse the whole thing accordingly, and to make report to her Majesty, what he found therein, etc. The commandment I received from her Majesty for me to certify my knowledge herein, may appear by this letter.

October 10, 1580. The Queen's Majesty to my great comfort (horâ quintâ) [in the fifth hour] came with her train from the Court, and at my door graciously calling me to her, on horseback exhorted me briefly to take my mother's death patiently: and with all told me, that the Lord Treasurer had greatly commended by doings for her title royal which he had to examine.

Crossley's page 19

The which title in two rolls of vellum parchment his Honor had some hours before brought home, and delivered to Mr. Hudson for me to receive at my coming from my mother's burial at church. Her Majesty remembered also then, how at my wife's burial it was her fortune likewise to call upon me at my house, as before is noted.

January 11, 1568, more Astronomico. The right honorable Earl of Pembroke did present my book of Propaedeumata Aphoristica to her Majesty in my behalf, as I was so advised to do by the honorable Mr. Secretary Cecill, now Lord Treasurer, to whom I had humbly given one of them the day before; and likewise one to the said Earl to use or give away at his pleasure, and likewise one to the said earl.

Within three days after the said Earl told me of her Majesty's gracious accepting and well liking of the said book; and he gave me very bountifully in his own behalf xx lib. to requite such my reverent regard of his Honor.

February 16, 1568, (more Astron.). Her Majesty had very gracious talk with me in her Gallery at Westminster (hora 2. vel circiter) [around 2 o'clock] as concerning the great secret for my sake to be disclosed unto her Majesty by Nicolaus Grudius Nicolai, sometime one of the Secretaries to the Emperor Charles the Fifth, etc. What was the hindrance of the perfecting of that purpose on all sides, God best knoweth.

June 14,1564 . After my return from the Emperor's court, her Majesty very graciously vouchsafed to account herself my scholar in my book, written to the Emperor Maximilian, entitled Monas Hieroglyphica. And said, whereas I had prefixed in the forefront of the book: Qui non intelligit, aut taceat, aut discat: if I would disclose to her the secrets of that book, she would et discere et tacere. Whereupon her Majesty had a little perusal of the same with me, and then in most heroically and princely wise did comfort me and encourage me in my studies philosophical and mathematical, etc.
[The axiom reads " He who does not understand should either be silent or learn."
If Dee were to explain it to her, the Queen promised to "learn and be silent,"
meaning she would not divulge its secrets to others.]

## CHAPTER V. <br> SOME MY DUTIFUL SERVICES DONE UNTO HER MAJESTY IN THE SPACE OF THIRTY-FOUR YEARS AND MORE.

1. Before her Majesty's coming to the crown, I did show my dutiful good will in some travails for her Majesty's behalf, to the comfort of her Majesty's favorers then, and some of her principal servants, at Woodstock, and at Milton by Oxford, with Sire Thomas Bendger (then Auditor to her Majesty), and at London; as Mr. Richard Strange and Mr. John Asheley, now Master of her Majesty's Jewell house, might have testified, and as I could have brought to their remembrance.

Upon suspicion of which my service then, and upon the false information given in by one George Ferrys and Prideaux, that I endeavored by enchantments to destroy Queen Mary, I was prisoner at Hampton Court, even in the week next before the same Whitsontide, that her Majesty was there prisoner also. I remained long prisoner, and all doors of my lodgings in London sealed up; and with other circumstances of grief, loss, and discredit for a while endured under the keeping of diverse overseers: as first in Court under Sir John Bourne, Secretary: while by writing I answered first four articles, and thereupon eighteen other, administer unto me by the right honorable the Privy Council.

Then from thence I was sent on Whitesun-even with the guard by water to London to the Lord Broke, Justice of the Common Pleas; from thence at length to the Star Chamber: where I was discharged of the suspicion of treason, and was sent to the examining and custody of Bishop Bonner for religious matters. Where also I was prisoner long, and bedfellow with Barthlet Grene, who was burnt: and at length upon the King and Queen's clemency and justice, I was (on August 19, 1555) enlarged by the Council's letters; being notwithstanding first bound in
2. Before her Majesty's coronation I wrote at large; and delivered it for her Majesty's use by commandment of the Lord Robert, after Earl of Leicester, what in my judgment the ancient astrologers would determine of the election day of such a time, as was appointed for her Majesty to be crowned in. Which writing, if it be extant and to be had, will be a testimony of my dutiful and careful endeavor performed in that, which in her Majesty's name was enjoined by me: in the year 1558 .
3. Her Majesty took pleasure to hear my opinion of the comet appearing in 1577: whereas the judgment of some had unduly bred great fear and doubt in many of the Court; being men of no small account. This was at Windsore, where her Majesty most graciously, for three * diverse days, did use me; and, among other points, her most excellent Majesty promised to me great security against any of her kingdom, that would, by reason of any my rare studies and philosophical exercises, unduly seek my overthrow. Whereupon I again to her Majesty made a very faithful and inviolable promise of great importance. The first part whereof, God is my witness, I have truly and sincerely performed; though it be not yet evident, how truly, or of what incredible value: The second part by God his great mercy and help in due time be performed, if my plat for the means be not misused or defaced.
4. My careful and faithful endeavors was with great speed required (as by diverse messages sent to me one after another in one morning) to prevent the mischief, which diverse of her Majesty's Privy Council suspected to be intended against her Majesty's person, by means of a certain image of wax, with a great pin stuck into it about the breast of it, found in Lincolnes Inn fields, \&c., wherein I did satisfy her Majesty's desire, and the Lords of the honorable Privy Council within few hours, in godly and artificial manner: as the honorable Mr . be seen in the records of the Council Chamber of that year, month, and day, if they be extant. Secretary Wilson, whom, at the least, I required, to have by me a witness of the proceedings: which his Honor before me declared to her Majesty, then sitting without the Privy Garden by
recognizance for ready appearance and the good abearing for about some four months after; which letter of the Council's is in print here to be seen: as the forepart of this narration may the landing place at Richmond: the honorable Earle of Leicester being also by.
5. My dutiful service was done, in the diligent conference, which, by her Majesty's commandment, I had with Mr. Dr. Bayly, her Majesty's Physician, about her Majesty's grievous pangs and pains by reason of toothache and the rheume, \&c. in October, 1578.
6. My very painful and dangerous winter journey, about a thousand five hundred miles by sea and land, was undertaken and performed to consult with the learned physicians and philosophers beyond the seas for her Majesty's health-recovering and preserving; having by the right honorable Earle of Leicester, and Mr. Secretary Walsingham but one hundred days allowed to me to go and come again in 1578. My passport here may somewhat give evidence, and the journal little book of every day's journey or abode for those hundred days account may suffice.

* Of these three days at Windsor Mrs. Skydamor, now
Lady Skydamor, has some remembrance.

7. My great, faithful, and careful attendance about the Lady Marquess of Northampton (in 1564) both beyond the seas, on the seas, and here in England, was performed with her Majesty's good will and well liking of. Whereupon her Majesty was the more willing, at the suite of the said Lady Marquiss, to give to me, for some recompense, the deanery of Glocester; but I was disappointed, as I have before specified, of the enjoying of it.
8. My faithful diligence and earnest labor, with some cost, was bestowed, by her Majesty's commandment, to set down in writing, with hydrographical and geographical description, what I then had to show or say, as concerning her Majesty's title royal to any foreign countries. Whereof, the two parchment great rolls full written, of about xii whole vellum-skins, are good witness here before you. For copy whereof I have refused an hundred pounds in money offered by some subjects of this kingdom: but it was not meet for me to take it.
9. My dutiful labor, commanded by her Majesty, upon the Gregorian publishing of a Reformation of the vulgar Julian year, may here appear to you in these two written books, having been read and examined by learned mathematicians (thereto assigned by the honorable Lords of the Council) and by their skills also warranted; and by the Lords of the Council and by the Barons of the Exchequer well liked off, for the manner of execution of it without any public cumber or damage, \&c. in 1582.
10. I sent very dutifully, humbly, and faithfully out of Bohemia (in 1585) letters to her sacred Majesty, requesting an expert, discrete, and trusty man to be sent to me in Bohemia, to hear and see, what God had sent to me and my friends there at that time; at which time, and till which time, I was chief governor of our philosophical proceedings; and by both our consents, there was somewhat prepared and determined upon to have been sent to her Majesty, if the required messenger had been sent by her Majesty to us. But not long after (so soon as it was perceived, that my faithful letters were not regarded therein) by lithe and lithe I became hindered and crossed to perform my dutiful and chief desire; and that, by the fine and most subtle devises and plots laid, first by the Bohemians, and somewhat by Italians, and lastly by some

Her sacred
Majesty best knoweth my sincere, zealous, constant, and dutiful fidelity toward her. of my own countrymen. God best knows how I was very ungodly dealt withal, when I meant all truth, sincerity, fidelity, and piety toward God, and my Queen and country.
And so to conclude this chapter: if in any other points, besides the forerehearsed, I have done my dutiful service any way to her Majesty's well liking and gracious accepting, I am greatly bound to thank Almighty God, and during my life to frame the best of my little skill to do my bounden duty to her most excellent Majesty.
(Dee's text continues for about 40 more pages.)
[From Autobiographical Tracts of Dr. John Dee, edited by James Crossley esq.,Chetham Society,1851; Courtesy of the Library of Congress, Washington DC]

## Discourse Apologetical

(Dee wrote this appeal for financial assistance to Queen Elizabeth in 1594. It was printed in 1599)


Some of Dee's Greek letters are challenging to read:
$\mu \eta ̀ ~ \sigma \tau \eta ́ \sigma \eta \varsigma ~ \alpha u ̉ \tau o i ̂ s ~ \tau \eta ̀ v ~ \alpha ́ \mu \alpha \varrho \tau i ́ \alpha v ~ \tau \alpha u ́ \tau \eta v$



## A Letter

much, to fop the mouthes, and, at length to ftay the inpudent attemptes, of the rafh, and malicious deuifers, and contriners of moft vntrue, foolifh, and wicked reports, and fables, of, and concerning my forefaid (tudious exercifes, paffed ouer, with my great, (yea incredible) paines, taane's, cares, and colts, in the fearch, and learning of true Philofophic; As, therein, Só, to certific, and fatisfie the godly and vnpartiall Chriftian hearer, or reader hereof: That, by his own iudgement, (vpon his due confideration, and camination of this, no litele parcell, of the particulars of my forefaid fudies, and exercifes phiIofophicall amexed) He will, or may, be fufficie:aty informed, and perfwaded; That I have wondertilly labored, to fiude, lollow, vec, \& haunt the true, ftraight, and molt narrow path, leading alltue, deuout, zealous, firithfull, and contant Chriltian ftudents, ex. valle hate mifcrie,
 iftuss Regni, admontem fanctum Syon, © ad calefia tabermacula. All thankes, are molt due, thercfore, vato the AImighty: Secing, it fopleafed him, (euen from my youth, by his diunc fanor, grace, and helpe) to infinuate into ny hart, an infatiable zeale, \& defire, co knowe his truth: And in him, and by him, inceliantly to feeke, and liften after the fane; by the true philofophicall method and harmony :proceeding and alcending, (as it were) gradation, fron thangs vifible, to coafider of thinges inuifible: from thinges bodily, to conceine of thinges firituall: from things trat-fitoric, \& momentanic, to meditate of things permine:t: by thinges mortall (wifible and inwifille) to haue fone perceimerance of immortality. And to con-


Tothe moft Reuerend father in Good, the Lord Archbifhop of Canturbury, Primate and Merropolitane of all England, one of her Maieflies moft honorable priny Coundaile: my fingular good Lord.
 Of humbly and hartily I craue your Graces pardon, if I offende any thing, to fend, or prefent vinto your Graces hand, fo fimple a difcourfe as this is: Although, by fome fage and difcreet my friends their opiniô, it is thought not to be impertinent, to my moft needfull fuites, prefendy in hand, (before her moft excellene Maiclty Royall, your Lordhips good Grace, and other the Right honorable Lordes of her Maiefties priuy Counfaile) to make fome part of my former Itudies, and ftudious exerciles (within and for thefe 46 , yeeres laft paft, vfed and continued) to befirt knowne and difcouered vnto your Grace, andother the Right honorable my good Lordes, of her Maiefties priny Counfaile: And, Secondly, afterwardes, the fame to be permitted to come to publique view: Not fo

$$
\mathrm{A}_{2} \quad \text { much }
$$

## Apologeticall.

clade, moft bricfely; by the molt meruailous frame of the whole W'orld, philofophically viewed, and circumfpectly wayed, numbred, and meafured (according to the talent, \& gift of God, from abouc alotted, for his diuine purpofes cffecting) moft faithfully to loue, honor, and glorific alwaies, the Framer, and Creator thereof. In whole workmanthip, his infinite goodueffe, vnfearchable wifdome, and Almighty power, yea, his cucrlafting * power, and + Paufe to diunity, may (by innumerable meanes) be manifelted, the Rom. and demonftrated. Tine truth of which my zealous, care- Capp.t.werf full, aud conltant intent, and endenour fpecified; may (I bope) eafilic appeare by the whole, full and due furucy, and confideration of all the Bookes, Treatifes, and dif. courles, whole Titles onely, are, at this time, here amexed, and expreffed: Asthey are fer down in the fixt Chapter, of mother liele ahappodicall Treatife, intitled, The Cöpendious Rebcar/all, és c. wtittéaboue two yeares fince: for thofe her Maielties two honorable Commiffioners; which her molt excellent Maiefty had moft gracioullic fent to my poore Cottage, in Mortlake : to vnderftand the matters, and caufes at full; through which, I was fo extreamely vrged to procure ather Maiclties handes fuch honorable inuruciors \& witneffes to be affigned, for the due proote of the contents, of my molt humble and pitifull fupplication, exhibited vuto her molt excellent Maiefty, at Hampton Court, 14n. 1592 2.Nouemb.g.
Thus therefore (as follow-
ech ) is y faid 6. Chapter
there, recorded.

## $A$ Letter

My labors and paines beftowed at diuers times, to pleafure my natiuc Countrey: by writing of fundry Bookes, and Treatifes: fome in Latine, fome in Englifh, and fome of them, written, at her Maielties commandement. Ofwhich Bookes, and Treatifes, fome are printed, and Fome vnprinted. The printed Bookes, and Treatifes are thefe following:

1. Propedenmata Apliorifica, De prepfantioribusquibufdă Nathre virtutilus.-Aphorifint, 120.-cAmo. iss 8.
2. Monas Hicroglyphica, Mathcmaticè, Anagogicćque expleata; ad Maximilianum (Deigralia) Romanorum, Bobcmice, © Hungarice, Rcgem aplentissimum an. $15 \sigma_{4}$.
3. Ep $\mathrm{I}_{\mathrm{fl}}$ ola ad eximium Ducis Vrbini Mathematicum (Fredericum Commandintm) prafixia libcllo Machomets Bagdedini, De (uperficiernum Dinifonibus; cdito in Lucem, operamea, © ciufdem Commandini Vrlinats; Jmpressa Pidatra-CAnno-1510. 4. The Bryti\% Glonarchy (otherwife called the Petty Nauy Royall:) for the politique fecurity; abundant weallh, and the triumphant state of thiskingdome, (with Gods fimor procuring - anno - 1576.
4. My CMathematicall preface annexed to Euclide, (by the right nor/Jipfull Sir Henry Billingfley Knighe, in the Englifl, language firft publifhed) urvitten at the carneft regucft of jundry right mor/bipf will Knights, and other very well learnedmen. Wherein are many Arts, of me, whocly inuented (by name, de finition, propriety and vfc,) more then either the Grecian, or Roman Mathematio ciens, hauc lefito our kisonledge - Anno-1570. My

## Apologeticall,

My diucrs © many Annotations, and fucentions जent ane maticall, added is fundry places of the forc/aid Engici,h Euclide, after the ienth Booke of thefanse -1s70. Epiffola prefiaia Ephemeridibus Joannis Felde Angli: cui rationem declaraueram Ephemerides conf cribendi.ts57. Paralatica Cómentationis, Praxcofg; Nuclcus quiudâ. If7?

The vaprinted Bookes and Treatifes, are thefe: fome, perfeety finifhed: and fome, yet vifinifled.

THe frift great volume of Famons and rich Difcouerics: wheretn'alfo) is the Hiffory of King Salomon, enery thrce yecres, his Ophirian voyage. The Originals of Preshyter Ioannes:and of the firft great Cham, and his fucceesors for many yceres following: The defcription of diuers wonderfull Iles, inthe Norihen, Scythian, Tartarian, and theorber moft Northen Seas, and neere under the North Pole : by Record, written aboue 1200 . yecres fince : with diuersolfer rarities -_-_Inno 1576. The Bryit') Complement, of the perfect Art of Nauigation; 1 great volame: in which, are contained our Quenc Elizabetb her Arithmeticall Tables Gubernauticke: for Nauization by the Paradoxall compa/fe (of me, inucnted anno 5 557.) and Nanization by great Circles: and for longitudes, and latitudes; and the variation of the compaffe finding mo/t eaflife, and/peedily: yea, (ifneede $b_{c)}$ inone minute of time, and (ometime, without fght of funne, moone, or Star; with manyother, new and needefullinuentions Gubernauticke__-anno-_1576. Her Maicsties Tüle Koyall, to many forrain Cuntries,kingdomes, andprowinces, by good teflimony and fufficient
proofe
prooferccorded: and in I2 Velamskins of parchment, faire written:forber Maicflies w/e: and at her CWaicflies commandement -_- - 1578
De 1mperatoris Nomine, ©Auboritate, © Potentia : dedicatcdioler Maiefly -1579
Prolegoniena of Dictata Parifienfia, in Euclidis Elemen. torum Geometricorum, Librum primum, of /ecundum; is Collegor Rbemenfl_aimo isso.
Devja colobi Calcjlis: ad Regem Edoardum faxtumi I sso The Art of Logicke, in Englsh - anno-1s47. The 13.Sophifficall Fallactās, with ihcir Difcoucrics, nritsten in Englifh metcr-anno- 154 s .
Mevchrius Cele/tis: Ilibri-24, written at Loutayn-1540.
De Nubium, Solis, Lune, ac reliquorum Planctarum, imano ipfrus ffelliferi Cieli, ab infimo Terre Centro, diffantig's, mutuif(q; intcruallis, ó eorsadcmomnium Magnitudine

Cfno - issi.
Cphori/mi Affrologici-300. anno -1553.
The true canfe, and account (not valgar ) of Flnds and Elbs: nvitten at the erequelt of therighishonorable Lady, Lady Iane, Ducheffe of $N$ erthumberland -amo- 1553.
The Pbilofophicall and Toeticall Originall occafions, of the configurations, and names of the beaucnly Aflerifmes wvitten at the reque/f of the fame Duche f/c. Anno. 1 s 53.
22. The Afronomicall, 0 losificall rules, ana Canons, to calcoslate the Ephemerides by, and other neceffary accounts of beancoly motions: writien at the requeft, and for the v/e of that excellent Alechanicien Matiler Richarad Chatuncelor, al his Liff voyage into Mof chouia-anno-1s53.
23.

De Acribologia Mathimulica; volumen magnum : /exdesim continens libros

Inventum

## Apologeticall.

Inuentum Mechanicum, Paradoxwm, De notra ratione delimeandi Circumicrentiam Circularem: vonde, valde rara alia excogstartper frique poterunt problemata. An. is so. De/peculis Comburentibus:librijex - Anno iss. 155.
De Perfpeituanilla, quaperitifsimi vtuntar Dictores. 1 ss7. Spcculum vaitatis: Ime Apologia pro Fratre Rogerio Bachone Aagglo:in gua docetur nibilillum per Decmoniorum feciffe aux:ilia,fcel philo ooplsum fuife maximum;naturaliterque of modis homini Chriftiano licit ts, maximus feciffercs,quas indoctum folet vulgwr in Demoniorum refcrre facinora 1557. De Annuli Affonimsicimultiplicivfin-lib.2-Anno. 1557. Troshilica Inucata lib - $2-$ Anso -1538.
 Detertia o precipua Per/pectimeparte, que de Radiorum frattione tralłat-libri-3-inno-1ss9. $D_{e}$ limere fubterranco-Libri-2-CAnso-1j60. $D_{e}$ Triangulorum rectilincorum c freis-libri-3-demonfrati; ;adexcelleni ifsimum Mathematicum Petrum Nonium confcripti -_Cnno-is Cabale Hebraice compendiofa tabella-e Anno-is62. Reppublice Britannice Synopfos in Englifh-Amno. Is $6 s$ s.
Di Trigono Circinóque Analogico, opufculum, Mathematicum ơ Mechanicum-libri_4-Anno-isos.
Deftella admiranda, in Cafsiopee LIfferijmo, calitus demiffaadorbem v/que veneris: Iterumque in Cali penetraliaperpendiculariter retracitia, post decimum /extum fuec apparitionis menfem -1 - 1573. Hipparchus Rediuius -Trallatulus-Anno, 1 s7s. De unico Mago ó triplici Herode, éóque Anischristiano.
\&nno $\rightarrow$ I570.
Tenfundryand veryrare Heraldical $\underset{B}{B}$ /afonings of one C efft

A Letter
or Cognifance, latfolly confirmed to certaine auncient Armes Lib.r.- Anno-157f. Tartarie litora, Delmeatio Hydrographica: CArthura Pit, ©゙ Carolo Iackmanno Anglis, verfus illas partes Nauigaturis, in manus tradita;cum adnuirandarum quarundam Infularum annotatione, in illis subpolaribus partibus iacentium -anno- 1580.
Hemi/phery Borealis Gcographica,atque Hydrographica defcriptio:long e a vulgatis chartis dituer/a: - Anglis quibuf. dam,verlis A lantidis Septentrionalia litora, nanigationeminftituentibus, dono data _-anno- $\sigma 5 \delta_{3}$
The Originals, and chiefc points, of our auncient Brytilh Hiflories, difconsr/cd vpon, and exsmined -anno 1583 .
Anaduife $O$ difconrje about the Reformation of the vulgar Inlianyeere-niritten by ber Maiesties commandement, and the Lords of the priny Counfaile - -anno- 1582. Certane confiderations, and conferrings together, of the fe three featences, (aunciently accounted is Oracles) Nof $\sqrt{c e}$ te ip/um : Homo Homini Detus: Homo Homini Lupps. Is 92
De hominis Corpore, Sprritu \& Anima:/ive Microcofmicame tosins Thilofoplois Naturalis Compendium-lib.I-Isgr

## A Letter

by his own viskilfalnes in fuch matter:and not vnderftanding my apt application thereof, in one of the very princi-
pal places, of the whole book. And It may now be here allore
membirad, that alimoft three chis booke of mince, (by Gods help yeeres after the writing of and fauour)fhall be dedicated vnthis letere, 1 did fomewhat to her inoft excellent maicfty Roirable fiiend in Courr,by fees all: And this Treatife doth condilie peaning foome rastere tainethree bookes, The fir $f$ inticoncerning her naidertes Sra-
funeraignice :vider this nitic tled, De Horizonte : Liber Mathe-

1. Thatutocrajia Bysunnica maticus of Pbyficus.The Secöd, $D_{c}$ Sine, Acternitate: Liber T'bcologitus, Di Erantico Matio Imprio, CMetaphy fecus or Mathematicus. Colieflanas Extamporsma: 4 . The Thira, De Horizonte Leter-
 uemb: oo , Mancefrie. maticus, \&r Hierotechnicus.

- Truly I hane great caufe to praife and thanke God, for your graces veric charitable ving of me : both infundry points cllc, \& alfo in your faurable yelding to, yea \& notifying the due meanes for the performance of her SacredMaiefties molt gracious and bountifull difpofition, refolution, and very royall begiming, to reftore and giue vito me (her Ancient faithfull feruant) Come due maintenance: toleade the reft of my old daies, in fome quiet and comfort : with habilitie, to retaine fome (peedy, faire, and Orthographicall writers, about mesand the fame skilfull in Latine and Greeke (at the leaft:) afwell for mine owne bookes, and workes, faire and correctly to be written (fitch Lineanc, as either her moft excellent Maieftie, out of the premifles will make choife of, or command to be finifhed or gublifhed: or fuch of them, as your grace fhall thinke


## Apologeticall.

With many other bookes, pamphlers, difcourfes, inuentions, and conclufions, in diuers Artes and matters: whofe names, need not in this Abttract to be notified:The moft part of all which, here fpecified, lie heere before your Honours ypon the table, on your left hand. But by other bookes and writinges, of an other fort, (if it fo pleafe God, and that he wil grant me life, lacalth, and due maintenance thereto, for fome ten or tweluc yeares next enf(uing) I may, hereafter make plane, and without doubt, this fentence to be true, plura latent, quaimpatent.
Thus far (my good Lord) haue Ifet downe this Catabogus, out of the forefaid fixt Chapter, of the booke, whofe title is this:
The Compendions rehear fall of Iohn Dee, his dutifulldeclarationasd proof of the courfe andrace of his fudious life, for the Ipace of halfe an bundred yecres, now (by Gods fautor and helpe)fiully (pcnt, ér c.
To which compendious rehearfall, doth now belongan Appendix, of thefe two lalt yecres: In which I hauchad many iultoccafions, to confeffe, that Homo Homini Dews, and Homo Homini Lupus, was and is an Argumét, worthy of the decyphering, \& large difcufsing:as may, one day, hereafter (by Gods helpe)be publifhed, in fome maner very ftrange. And befides all the rehearfed books, \& treatifes of nyy writing, or handling hitherto, 1 hauc iuft caufe, lately ginen me to write \& publifh a Treatife, with Tite, De Horizontc Ac. ternitatis : to make cuident, that one Andreas Libauits, in a booke of his printed the laftyeere, hath vnduly confidered aphrafe of iny Monas Hicroglyphica: to his milliking: $\mathrm{B}_{2}$

## Apologeticall.

meete or worthy for my farther labor to be beftowed on:) as elfe for the fpeedy, taire, and wue writing out of other ancient Authors their good and rare workes, in grecke or Latine : which by Gods prouidence, hatue been preferued frōthe fpoile made of my Libraric, $\&$ of all my moucable goods here: \&c. Anno. 1583. \% Although wás my laft In which Librarie, were about voyage beyond $\begin{aligned} & \dot{y} \text { Seas, was } \\ & \text { duly vndertake (by her Maz }\end{aligned}$ 4000 bookes : whereof, 700 . were ieftiks good fauour and i anciently written by hande: Some cence) as by the fame words in Grecke,fome in Latine, fome in maytenpeate he riglit honoust, Hebruc: And fome in other lan- rable Lord Threaforer, vino guages(as may by the whole Cata- and hrare mont excellentenalf, mat logus thercof appeare.) But the ieflie willing sis honoror fo to great loffes and dammages which $\begin{aligned} & \text { donnarie. Ano, is } \\ & \text { I } 90, \text { ihe } 20 \text {. of }\end{aligned}$ infiundry forts I haue fiftained, do not fo much gricue my
hart, as the rafh, lewde, fond, and moft mntrue fables and hart, as the ralh,lewde,fond, and moft vntrue fables and reports of me,and my ftudies philofophicall, have done, \&cyet do : which cömonly, after their firt hatching, and dinelifh deuifing, immediatly with great fpeede, are generally all the Realme ouerfpread; and to fome, feeme truc; to other, they are doubtfull: and to only the wife, modeft, difcrect, godly, and charitable (and chiefelie to fuch as hauc fome acquaintance with me) they appeare, and are knowne to be fables, vintruths, and vtterly falfe reports, and felaunders. Well, this fhall be my laft charitable giuing of warning, and feruent proteftation to my Countrimen and all other in this cafe:

Before the Almighty our Gcd, and your Lordfljips good A feruene. grace, this day, on the perill of my foules damnation (if I lie, or proceflaia salke his nanue in vame her cin) Itake the fame God, to be my $\mathrm{D}_{3}$
witneßse,
50.

## A Letter

witnc/fc; 7 lat, with allmy hart, with all my foule, with all ny flecngth, power, and winderflanding (according to the mea/ire thereof, which the Almighty hath giuen me) for the melt part of the time, from my youtb hitherto, I hauc vjcd, and fill of $c$, good, lan foll, honcf, c/rrt/tian, and dininelypreferibedmeancs, to attaine to the knovkedge of thofe truthes, which are meet, and nece/Jary for me to know; and whermith to dohis diuine Maic/fy fach) (ervice, as bec hath, doth, and will call me winto, daring this my lffe: for hes honor and glory aduanting, and for the bencfit, and commoditic publigue of this king dome; lo mush, as by the will, and purpofe of God, Thall lic in my skill, and bablity to performe : as atruc, faithfull, and moft fincerely dutifill feruant, to our moll gratious and incompar able Queene Elizabeih, and as a very comfortable fcllo:1-member of the bodypoliique, gouerned vnder the ficpter Reyal of our earthly Supreame head (Quecne Elizabeth) andas alituely (ympathicall, and true (ymetricall fellow-member, of that holy and myflicall body, Catbolicklic extended and placed (n:herefoener) on the cartbin llo view, knowledge, dirceition, protection, illsmination, and conjoldtion of the Almighty, moft blefed, mofl holy, mofig ghrions, comaicflicall, coicternall, and coiffentiall Trinity: The head of that body, being only our Redecmer, Chriff tefus, perfect Godand perfect man: whofe returne in glory, we faithfully arvite, and daily, do very earnefly cry unto bim, to basten his/econd commang, for bis elecites fake :iniguty doth foon this carth, abound, and preuaile, and true faith with charity, and Enangelicallfimplicity, haue but colde, fender, and vncertaine intertainement, among the worldy-nife men of this worlde.

Therefore (herein concluding) Ibefcechthe Almighty God, moff aborndanily 10 increafs and confirme your graces beauchly

## Apnlogeticall.

beanenly wifdome, and cnduc you with all the reflof his beas wenly if fs for the reliening, refrefling, and comiforting, both bodily and jpiritually, bis liutle lacke of the faithfull yci milstant here on earth. Amen.

## An Epilogue.

Good my Lord, I befeech your grace, to allowe of my plaine and comfortable Epilogus , for this matter at chis time. Seeing, my ftudious excreifes, and comerfation ciuile, may be aboundantly teflified, to my good credit, in the molt partes of all Clriitendome: and that, by all dcgrees of Nobility, by al degrees of the learned, and by very many other, of godly and Chriftian difpofition, for the pace of 46 . yeeres triall: (as appearech by the Recordes lately viewed by two honourable witneffes, by Commiffionfrom her Maie(ty, And fecing, for thefe 36.yecres, laft paft, I hane beene her moft excellent Maicfties very trae, faithfull, and dutifull feruaunt; At whofe royall mouth, I neuer receiued any one word of reproch; but all of fanor, and grace:In whofe princely countenance, I neuer perceined frowne toward me, or difcontented regard, or view on me: but ar all times faurable, and gracious: to the great ioy and comfort of my true, taithfull, and loyall hart. And (thirdly) Sceing, the workes of my handes, and wordes of my mouth (hecre before notified, in the Schedule of my bookes, and writings) may beare linely witneffe of the thoughts of my hart, and inclination of my minde, gencrally, (as all wife men do know, and Chrift himfelfe doth auouch) It might, in manner, feeme needleffe, thus care-
fuilly

## Apologcticall.

otherwife then as it appertaineth to a faithfull, emrefill, funcere, and humble feruant of Chrilt Ieft, That your grace woulde vouchfafe to aduertife me. So , I truit, Vltima refpondebunt primis: infich fort, as this Autheritick Recorde in latine ansexed (ad perpetuam rei memoriam,) doth teftific: hauing neuer, hitherto, hadoccafion to fhewe that, in any place of Chriftendome: to teflific better of me, then they had proofe of me, themfelues, by my conuerfation among them. (The Almighty, therefore, be highly thanked, praifed, honored, and glorified, for ener and euer, Amen.)
Butnowe, in refpect of the generall intent of this bricfe difcourfe, I moft humbly, and reuerently, exhibit to
your graces view, and perufing, the originall monu-
ment, and Authenticke Record, before mentioned, faire written in parchment, with the feale whole, and perfect, duly appendant: as I haue 46 yectes, and fomewhat longer, preferued it. The true copy wherof, your grace doth fee, to be verbatim, as followeth.

## A Letter

fully (though moft briefely and fiecedily) to hane wamed or coufounded the fcornefull, the malicious, the proud, and thic raxh in their vitruc reports, opinions, and fables of my tudies, or exercifes Philolophicall: but that, it is of more importance, that the godly, the honeft, the modeft, the difcrect, grane, and charitable Chriftians (Eng lifh or other, ) louers of Iuftice, truth, and goo! ! learning, may, hicreby, recciue certaine comfort in themelhes to percciuc, that Veritas tandens prenalcbit) and fifficicntly be weaponed and armed with found truth, to defende me againtt flich kinde of my aduerfaries: if hereafter they will begin afreh , or hould on, obitunately, in their former cerors, vainc imaginations, falle reportes, and moft vngodly fclanders of me and my ftudics. ©T Therefore, (to make all this caufe,for euer, before God and man, out of all doubt:) Sccing, your Lordihips good grace, are, as it werc, our high Prieft, and chicfe Ecclefiafticall minilter, (vider our moft dread and Soucraigne Ladie, Qurene Elizabech) to whofe cenfure and iudgement, I fubmit all my ftudies and exercifes; yea all my bookes, pait, prefent and hereafier to be written, by me (of my own skill, iudgement, or opinion,) I do, at this prefent time, moft humbly, fincerelic, and vnfainedly, and in the name of Almighry God, (yea for his honor and glory) requeft, and befecch your Griace, (when, and as contueniently you may) to be well and throughle certified of me, what lam, Intus © os cute : Reuerendijsime in Cbriffo Pater, O Dignifime CArchipraful, cognofee © a agno/ce vultum simintinernum, quamexternum pecoris tui: And wherein I haue vied, doe or fhall vfe , pen, fpeech, or conterfation, otherwile


## Apologeticall.

## Pcroratio.

THe Almightie and moft mercifull God the Father; for his only Sonne (our Redeemer) Iefus Chrift his fake: by his holy fpirit, to direct, bleffe, and profper all my ftudies, and exercifes Philofophicall, (yea, all my thoughts, words, and deedes) henceforward, enen to the very moment of my departing from this world, That I may cuidently and aboundantly be found, and vndoubtedly acknowledged of the wife and iuft, to haue beene a zealous and faithfull ftudent in the Schoole of $\bar{r}$ erity, and an Ancient Graduate in the Schoole of Charity : to the honor and glory of the fame God Almighty, and to the found cöfort and confirming of fuch as faithfully louc \& feare his diune Maieftic, and vnfeinedly continue in labor to do good, on earth : when, while, to whome, and as they may, Amen.

Very fpeedily written, this twelffh euen, and wwelfth day, in my poore Cottage, at Mortake: Anno. i igs. currente à Natinitate Cbrifit: aft, An, 1594. Completo , à Conceptionce eiuldem, cum nouem prateres menfibus, Completis.

Allwaies, and very dutifully, at your Graces commandement:

Iohn Dee.


- AT LONDON Printed by Peter Short, dwelling on Bredftreete hill at the figne of the Starre,

[Dee is kneeling in a burning cauldron of Hope, Humility and Patience.
His is reciting the prayer Stephen made after he had been cast out of the city and stoned (from Acts 7:60.) Up in the clouds are God's all-hearing ear, his all-seeing eye, and his Sword of Justice. The many-headed beast is comprised of Dee's accusers and the rumor mill of the vulgar crowd.]


> To the most Reverend father in God, the Lord Archbishop of Canturbury, Primate and Metropolitaine of all England, one of her Majesties most honorable privy Council, and my singular good Lord.

ost humbly and heartily I crave your Grace's pardon if I offend any thing to send or present unto your Grace's hand such a simple discourse as this is. In light of my petition to her most excellent Royal Majesty, our Lordship's Good Grace, and other honorable good Lords of the Privy Council, my sage and discreet friends though it not be impertinent for me to explain some of my studies and studious exercises for the past 46 years.

Second, permit this to come to public new, not just to stop the mouths and stop the impudent attempts of the rash, and malicious devisers and contrivers of untrue, foolish, and wicked reports and fables concerning my studies, made with great (yea, incredible) pains, travels, cares and costs in the pursuit of true Philosophy.

Let this serve to certify and satisfy the judgement of the godly and unpartial Christian hearer or reader to be sufficiently persuaded that I have wonderfully labored to find, follow, use and haunt the true, straight and most narrow path leading all true devout, zealous, faithful and constant Christian students.
(from this valley of misery and the valleys of that misery, and from the kingdom of shadows and from the shadows of that kingdom to the holy Mt. Sion and to the heavenly tabernacles)
All thanks are most due to the Almighty, as it so pleased him (even from my youth, by his divine favor, grace and help) to introduce into my heart an insatiable zeal and desire to know his truth.

And in him, and by him, unceasingly to seek and listen to the same, by true philosophical method and harmony; proceeding and ascending (as it were) gradation [by steps] from visible things, to consider invisible things; from bodily things, to consider spiritual things; from transitory and momentary things, to meditate on permanent things; by mortal things (visible and invisible) to perceive immortality.

And to conclude, by the most marvelous frame of the whole world, viewed philosophically, and circumspectly weighed, numbered, and measured (according to the talent and gift of God for effecting all this for his divine purpose) most faithfully to love, honor and glorify always the Framer and Creator of it all.

In his workmanship, infinite goodness unsearchable wisdom and almighty power, yea, his everlasting* power and divinity may (by innumerable means) be manifested and demonstrated.

The truth, of which my zealous, careful and constant intent and endeavor is specified here, may (I hope) easily appear by the whole, full and due survey and consideration of all the Books, Treatises, and discourses, whose Titles are annexed here. They have also been set down in the sixth Chapter of another little Rhapsodical Treatise entitled the Compendious Rehearsal.

It was written over two years ago for two honorable Commissioners which her most excellent Majesty sent to my poor Cottage in Mortlake to understand the causes of matter in full. At that time I had been urged to provide her Majesty's honorable Surveyor the proof of the contents of my most humble and pitiful supplication, which had been exhibited to her at Hampton Court on November 9, 1592.

Here is the contents of that sixth Chapter:
My labors and pains have been bestowed at diverse times to please my native Country by writing sundry Books and Treatises. Some are in Latin, some in English and some of them were written at her Majesty's commandment.

## Some of the Books and Treatises were never printed. <br> The following are Books and Treatises that were printed:

## 1. Propaedeumata Aphoristica

On the most superior virtues of Nature, 120 Aphorisms. (Year 1558)

## 2. Monas Hieroglyphica

Mathematically and Anagogically [spiritually] explained to Maximillian, most wise King of the Romans, Bohemia, and Hungary. (Year 1564)
3. Letter to the Most Excellent Mathematician Frederico Commandino of Urbana, prefixed to a small book by Mohammed of Baghdad entitled On The Division of Surfaces. [which wastranslated by Commandino of Urbana and published in Pisa]. (Year 1570)
4. The British Monarchy (otherwise called The Petty Royal Navy) for political security, abundant wealth and the triumphant state of this kingdom (with God's favor). (Year 1576)
5. My Mathematical Preface, annexed to Euclid (for the first time published in the English Language by the right worshipful Sir Henry Billingsley, Knight, ) written at the earnest request of sundry right worshipful knights; and other learned men. Wherein are many Arts wholly invented by me (their names, definitions, properties, and uses). This is more than any Greek or Roman Mathematician has left for our knowledge. (Year 1570)
6. My diverse and many Annotations and Mathematical Inventions, added in sundry places to the tenth Book of the aforementioned Euclid.

## 7. Letter prefixed to the Ephemeris of the Englishman John Field.

8. Commentary on the Reasons for Parallax. (Year 1573)

These are the unprinted Books and Treatises (some complete, some unfinished).
9. The first great volume of Famous and Rich Discoveries which includes:

The History of King Solomon (all three years of his Phirian voyage).
The Original work of Presbyter John (of the first great Cham [Lordship] and his successors for many years following).

The description of diverse wonderful Islands in the North, Scythian, Tartarian and most other Northern Seas near and under the North Pole from 1200-year old Records and other diverse rarities. (Year 1576)
10. The British Complement of the Perfect Art of Navigation. A great volume containing Arithmetical Tables Gubernautic, for Navigation by the Paradoxal Compass (invented by me in 1557) and for Navigation by great Circles. (for longitudes and latitudes).

It takes into account the variation of the Compass to most easily and speedily find true direction (yea, if need be) within one minute of time and sometimes without sight of the Sun, Moon or any Star. Also many other new and needed inventions for Navigating at Sea. (Year 1576)
11. Her Majesty's Royal Title to ManyForeign Countries, Kingdoms, and Provinces (recorded with good testimony and sufficient proof) for Her Majesty's use and at her Majesty's commandment. On twelve vellum skins of parchment. (Year 1578)
12. On Imperial Name, Authority and Power. Dedicated to Her Majesty. (Year 1579)
13. Prologue and Speech to the Parisians at the College of Rhemes on Euclid's Elements. first and second book. (Year 1550)
14. The Uses of the Celestial Globe. for King Edward VI. (Year 1550)
15. The Art of Logic. in English. (Year 1547)
16. The 13 Sophistical Fallacians [arguments containing a fallacy], with their discoveries, written in English meter. (Year 1548)
17. Planet Mercury in the Heavens. 24 books, written at Louvain. (Year 1549)
18. On the Clouds, Sun, Moon, Planets and Fixed Stars in the Heavens. (Year 1551)
19. 300 Astrological Aphorisms. (Year 1553)
20. The True Cause and Account (not vulgar) of Floods and Ebbs written at the request of the Right Honorable Lady Jane, Duchess of Northumberland. (Year 1553) [Jane Guilford Dudley]
21. The Philosophical and Poetical Original Occasions of the Configurations and names of the heavenly Asterisines [constellations] written at the request of the same Duchess. (Year 1553)
22. The Astronomical and Logical Rules and Canons Used to Calculate the Ephemerides. Describing other necessary accounts of heavenly motions. Written at the request and for the use of that excellent Mechanician, Master Richard Chancellor, for his final voyage to Muscovia [Moscow]. (Year 1553)

## 23. De Acribologia Mathematica

a large volume of 16 books. [loosely translated as on "Precision in Mathematics"] (Year 1555)
24. A Paradoxical Mechanical Invention used to find a new way to delineate the Circumferences of Circles, with which other very rare problems are able to be thought out and completed (Year 1556)
25. On Burning Mirrors. (Year 1557)
26. On Perspective, as it pertains to Pictures. (Year 1557)
27. The Mirror of Unity An Apology for English Friar Roger Bacon, the Englishman, in which it is taught that that man did nothing by the aid of the Demons, but was the greatest philosopher, naturally, and by the ways allowed to a Christian man. He did the greatest things, but the unlearned mob is accustomed to attribute them to the evil deeds of Demons. (Year 1557)
28. The Many Uses for the Astronomer's Ring. Two books. (Year 1557)
29. Inventive uses of Trochillica [wheels and pulleys]. Two books. (Year 1558)
30. Peri Anabibasmos Theologikon [loosely translated as "The Theology of Ascendancy"]. Three books.(Year 1558)
31. The Third and Most Excellent Part of Perspective, the Refraction of Rays.Three books.(Year 1559)
32. On Subterranean Tunnels. Two books. (Year 1560)
33. On Right Triangles. Three Books describing a demonstration made by the most excellent Mathematician Pedro Nunes. (Year 1560)
34. Compendious Table of Hebrew Cabala. (Year 1562)
35. A Synopsis of the British Republic, in English. (Year 1565)
36. On the Triangle and the Analogical Compass. A Mathematical and Mechanical work. Four books. (Year 1565)
37. An Unusual Star in the Constellation Cassiopia. Concerning the amazing star in the constellation of Cassiopeia that appeared in the heavens. It was located in the sky next to the orb of Venus, then again drawn back into the inner areas perpendicularly, after the sixteenth month of its appearance. (Year 1573)
38. A Renewing of a tract by Hipparchus. (Year 1573)
39. On one Mage and of Herod. (Year 1570)
40. Ten sundry and very rare Heraldical Blazonings of one Crest or Cognisance (lawfully pertaining to certain ancient Arms). One book. (Year 1574)
41. Atlantidis: a correct water map of the West Indies [North America] (never published by anyone else). (Year 1580)
42. The measure of the Evangelical Jesus Christ. (Year 1581)
43. Navigational maps to Cathay by Way of Northerly Regions, Scythia, and Tartar for Arthur Pitt and Charles Jackman. (Year 1580)
44. A Land and Water Map of the Northern Hemisphere [polar projection]. (Year 1583)
45. The Original and Chief Points of our Ancient British History. Discussion and Examination. (Year 1583)
46. An Advice and Discourse about the Reformation of the Vulgar Julian Year written by her Majesty's commandment and the Lords of the Privy Council. (Year 1582)
47. Certain considerations and conferrings of the three ancient sentences: Nosce Teipsum [Know Thyself], Homo Homini Deus [Man is a God to Man], Homo Homini Lupus [Man is a Wolf to Man]. (Year 1592)
48. On Body, Soul, Spirit in the whole Microcosm of Natural Philosophy. One book.(Year 1591)

With many other books, pamphlets, discourses, inventions and conclusions in diverse Arts and matters
which need not be listed in this Abstract.

Those which I have listed are piled here before you (on your left hand side). But I will make plain other sorts of books and writings (if it so pleases God that he will grant me life, health, and due maintenance for the next ten or twelve years) and without a doubt show that this sentence is true: Plura latent, Quam patent [Slow, but steady].

Thus far (my good Lord) I have set down

It should also be remembered that (three years after writing the Compendious Rehearsal) I satisfied the request of an honorable friend in the Court to specifically write about her majesty's Sovereignity of the Sea under the title:

Thalasttocratia Brittanica
[British Sovereignty of the Sea]
regarding Britain's Imperial
right to the seas.
(collected without haste and written with swift pen in the space of 4 days, completed on September 20, 1597, in Manchester)
this Catalog of the aforementioned sixth Chapter of this book:

The Compendious Rehearsal of John Dee, his dutiful declaration and proof of the course and race of his studious life, for the space of half of a hundred years, now, by God's (favor and help) fully spent etc.

Here now is an Appendix to this Compendious Rehearsal regarding the past two years.
I have had many just occasions to confess that Homo Homini Deus [Man is a God to Man], and Homo Homini Lupus [Man is a Wolf to Man] was and is an Argument Worthy of deciphering and discussing at large. It may (by God's help) one day be published, in some very unusual way.

Besides all the books and treatises I have written, I have lately had reason to write and publish a Treatise entitled On the Horizon of Eternity. I have done so to make evident that Andreas Libavius (in one of his books printed last year) has unduly considered a phrase of my Monas Hieroglyphica, a mistake made because of his own unskillfulness in such matters, and not understanding my apt application of it in one of the principal places in the whole book.
[Dee only uses this expression in his "Thus the World Was Created" chart.]
This new book of mine (with God's help and favor)
shall be dedicated to her most excellent Royal Majesty
and will contain three books:
On the Horizon, a book on Mathematics and Physics
On Eternity, a Theological, Metaphysical, and Mathematical book.
On the Horizon of Eternity, a book on Theology, Mathematics and Hierotechnics [Sacred Art].
Truly I have great cause to praise and thank God for your grace's very charitable using of me, both in these sundry points and in others. And also for your favorable yielding to (yea, and notifying) the due means for the performance of her Sacred Majesty's most gracious and bountiful disposition, resolution, and very royal beginning to restore and give unto me (her Ancient faithful servant) some due maintenance.

Thus, I might lead the rest of my old days with some quiet and comfort, with the ability to retain some speedy, fair, and Orthographical [those who can spell correctly] writers about me who are skilled in Latin and Greek (at the very least).

And also so that my own books and works can be copied fairly and correctly (I mean those that her most Excellent Majesty may choose and command to be finished and published, or those your Grace shall think fit or worthy for my labor to be bestowed upon).

And also for the fair and true transcribing of other good and rare works of other Authors (in Greek or Latin), which by God's providence have been preserved after the spoiling of my Library and all my moveable good here in the Year 1583.

In my library there were about 4000 books, 700 of which were anciently written by hand (some in Greek, some in Latin and some in Hebrew, and some in other languages (as can be seen in my Catalog).

But the great losses and damages of various kinds that I have sustained do not grieve my heart as much as the rash, lewd, insipid, and most untrue fables and reports about me and my philosophical studies (those I have done and have yet to do).

Usually, after their first hatching and devilish

My last voyage beyond the Seas was duly undertaken (by her Majesty's good favor and license) as can be seen in the Letter written by the right honorable Lord Treasurer in my behalf, as her most excellent majesty willed his honor to do.

January 20, 1590. devising, they immediately, with great speed, spread throughout the Realm.

Some believe them, some are doubtful, but the wise, modest, discreet, godly and charitable (and generally those who have some acquaintance with me) know they are fables, untruths, utterly false reports and slanders. Well, this shall be my last charitable warning and fervent protestation to my Countrymen (and all others).
[Dee concludes with a short invocation, an epilogue, and a peroratio (the finishing up of a speech)]


[^0]:    "Citizen of the World"
    (COSMOPOLITE, IS A WORD COINED by John Dee, from the Greek WORDS COSMOS MEANING "WORLD" AND POLITÊS MEANING "CITIZEN")

[^1]:    [The 1691 Anonymous author translates S.D.P as "Wisheth much Health." The 3 letters. might be an abbreviation of Salutare (Health or Prosperity), Desidero (to Wish), and Praebo (to Offer, Make, or Grant)] [Often the initials S.V.B.E. were used as a salutation for "si vales bene est." I hope you are in good health. -Smith's English Latin Dictionary, "health" p. 366]

[^2]:[^3]:    

[^4]:    A figneor point is of Pithagores Scholets after this manner defined: 1 poynt is an unitie whach hath pofition. Nübers are conceaued in mynde without any forme $\&$ figure, and therfore without matter wheron to receaue figure, \& confequently without place and pofition. Wherfore vnitie beyng a part of number, hath no pofition, or determinate place. Wherby it is manifeft, that number is more fimple and pure then is magnitude, and alfo immateriall: and fo vnity which is the beginning of number, is leffe maretiall then a figne or poynt, which is the beginnyng of magnitude. For a poynt ismaterially and requireth pofition and place, and therby differeth from vnitic.

    > 2. A line is lengtb without breadtb.

    There pertaine to quantitie three dimenfions, length, bredth, \& thicknes, or depth: and by thefe thre are all quătities nieafured \& made known. There are alfo, according Bei. 5 ¢

[^5]:    Perspective (Optics, or the properties of Direct, Bent, and Reflected Rays)
    Astronomy (Distances, Magnitudes and all natural Motions of the planets and fixed stars)
    Music (judging and ordering the many varieties of Sound)
    Cosmography (describing of the Heavenly and Elemental parts of the World)
    Astrology (the secret Influence of the planets and fixed stars in every elemental body)
    Statike (Weighing things, the properties of heaviness and lightness of all things)
    Anthrography (number, measure, weight, figure, situation and color of Man)
    Trochelike (the properties of all Circular motions, in devices using wheels and pulleys)
    Helicosophy (the designing of all Spirals, like a screw or a spiral stairway)
    Pneumatithme (air or water Pressure, in things like bellows and pumps )
    Menandry (Multiplying of a force used for lifting, pulling or pushing)
    Hypogeiody (mapping Tunnels under the earth's surface)
    Hydragogy (Directing the flow of water, like in aqueducts and canals)
    Horometry (determining the exact Time, with sundials or various inventions)
    Zography (Painting from Life, using lines and color to represent what you see)
    Architecture (the Reasoning for the Lineaments and Framing of a house, building, fort, or ship)
    Navigation (finding the shortest Route between two places over the seas)
    Thaumaturgike (Wonderworkings that can be perceived by the senses)
    Archimastry (certifying something by experience, Experimental science)

[^6]:    [Robert Goulding, Wings (or Stairs) to the Heavens, The Parallactic Treatises of John Dee and Thomas Digges. Stephen Johnston, Like Father, Like Son? John Dee, homas Digges And the Identity of the Mathematician In
    John Dee: Interdisciplinary Studies in English Renaissance Thought, edited by Stephen Clucas, pp. 41-84]

